

# **BLAST FURNACE OPTIMISATION BY LINEAR PROGRAMMING**

*BY*

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**(MME/91/2956)**



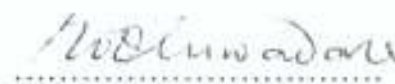
**AUGUST 2002**

## CERTIFICATION

I certify that this work was carried out by ABOGINJE Peter Apata of the Department of Metallurgical and Materials Engineering, Federal University of Technology, Akure, and that the work has not been submitted elsewhere for the award of a degree.

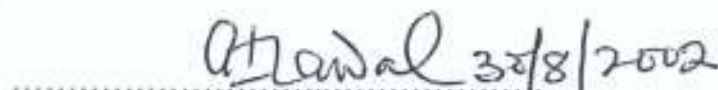


  
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## DEDICATION

This work is dedicated to God Almighty who teaches my hands to war and fingers  
to battle



## ACKNOWLEDGMENT

I foremost, give thanks to almighty God whose enabling grace has seen me through, frustrate every plan of the enemy during this work, and made his peace which passes all human understanding multiplied unto me.

My profound gratitude goes to my project supervisor, Dr. Oluwadare G. O. for his inspirational assistance, encouragement and supervision of this work. I am also grateful unto him and his family for making available most of the literature used. I also appreciate my co-supervisor Professor Oni A.

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To God Be The Glory, Great Things He Has Done!

THE LORD IS MY ROCK.



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## ABSTRACT

The model used for optimizing the blast furnace input parameters is described. It is based on the mathematical description of the stoichiometric and enthalpy balances of blast furnace process, and quantifies the amount of fuels required for producing a specific amount of pig iron and the effects of varying these inputs. The models were communicated into a linear optimisation Computer program written in MATLAB.

The designed operating data obtained from the Nigerian blast furnace at Ajaokuta steel complex, and the parameters of various fuels used were input into the program. The outputs generated were analysed.

## 1.0 INTRODUCTION

Over the years, the steel industry has played a major role in the development of our industrialized society and still remains an important factor for the industrial growth of both the developed and developing nations. The Blast furnace has been the link in the chain processing of iron ores into a finished steel product (Poos 1986). It is an economic and reliable mass producer of liquid iron. During the last century, productivity, efficiency, and reliability of Blast furnace process have attained levels no iron makers would have dreamed of a few years earlier. From the point of view of energy requirement, this process has shown a very great flexibility and accepts a great variety of fuels. The type of fuel used varies from country to country and depend mainly on the relative abundance and cost of the different types of fuel.

The blast furnace (Fig 1) makes use of mainly coke for the production of the reducing gas necessary for iron ore reduction, and production of heat for the melting, and provision of support for the burden inside the furnace. The recent economic upheavals, double energy crisis, persistent recession of the economy in general, and the steel industry in particular, sky-rocketing costs, interest rates, and financial shortcomings in many steel industries have slashed the steel industry into a mood of uncertainty and pessimism (Leone and Meyer 1980, and Luersseen 1981). Of all the Blast furnace charge, Metallurgical Coke has the highest cost, and the possibility of the price of blast furnace coke declining is ruled out (Nashan 1996).

Obviously, there is a decline rate of coke production yearly. In Africa, most of the coal are not coking, especially the Nigeria coal.

Improvements being made in the blast furnace operations so far are aimed at the following;

- (1) Better and smoother operation of the furnace.
- (2) Increase in productivity to reduce production cost and meet increasing demands
- (3) Reduction in coke consumption, which is very expensive due to diminishing reserves of coking coal.

In order to achieve the above objectives, the following steps are to be adopted.

- (i) Injection of hydrocarbon liquids, gases or solids through the tuyeres, which has led to lowering of furnace requirement for coke.
- (ii) Injection of these alternative fuels with the use of hotter blast.
- (iii) Enrichment of blast with pure  $O_2$  leading to increased flame temperature in front of the tuyeres thus permitting increased injection of hydrocarbon and increased rate of CO production.
- (iv) Higher top pressure, which increase the residence time of reducing gases within the furnace.
- (v) Better burden distribution in the furnace by the production of novel top charging devices such as the Paul Wurth Top and movable armor. The Paul

Wruth top in addition to better burden distribution permits the use of higher top pressures.

- (vi) Better process control through the use of computerized instrumentation and installation of process control computers.

The use of computers in the optimization of the furnace permits the prediction of the total raw material combination to be used in the production of liquid steel at the minimum cost, and the thermal effect of such combination. Several optimization work have been used extensively for controlling blast furnace performance, deciding the composition of furnace charge, and neural network application to blast furnace burden, top gas, and heat distribution control ( Inkala et al 1995, Iida 1995, Augstenberger 1996, Deitz 1997, and Zuo et al 1998).

This work shows that the flexibility of the blast furnace process is such that it can be adapted to a wide fuel combination and consumption, and the different aspect of the optimisation procedure are discussed.

The iron blast furnace has developed from the earliest production of liquid iron in shaft furnace in 14<sup>th</sup> Century (Cottrel 1975), to the replacement later of charcoal by coke, which has led since to the blast furnace over increasing in size. Figure 1 depicts steel-making process in a modern blast furnace. The iron blast (Fig.2) furnace is a tall, vertical shaft furnace, which employs, mainly in form of coke to reduce iron from its oxides.

The foundation of a blast furnace carries a heavy load. It constitutes piles driven to the bedrock, over which a huge reinforced concrete structure is constructed. The steel column mounted on the concrete ring support the mantle ring. The blast furnace shell and the inside brickwork are supported by the mantle ring.

The hearth bottom consisting of courses of fireclay bricks and carbon blocks is laid out within the concrete ring. The hearth is a cylindrical portion where the Iron notch, slag notch and tuyeres are located. The bosh is the section that slopes outward just above the hearth. The body is again a cylindrical portion above the bosh. The shaft, which is in the form of a cone, comprises the portion above the body. The throat, cylindrical in form is at the top of the shaft.

There are box type coolers within the refractory lining of the throat and shaft through which water circulates. The coolers are mounted to the shell of the Blast furnace. The bottom of the hearth and sidewalls are having plate type coolers.

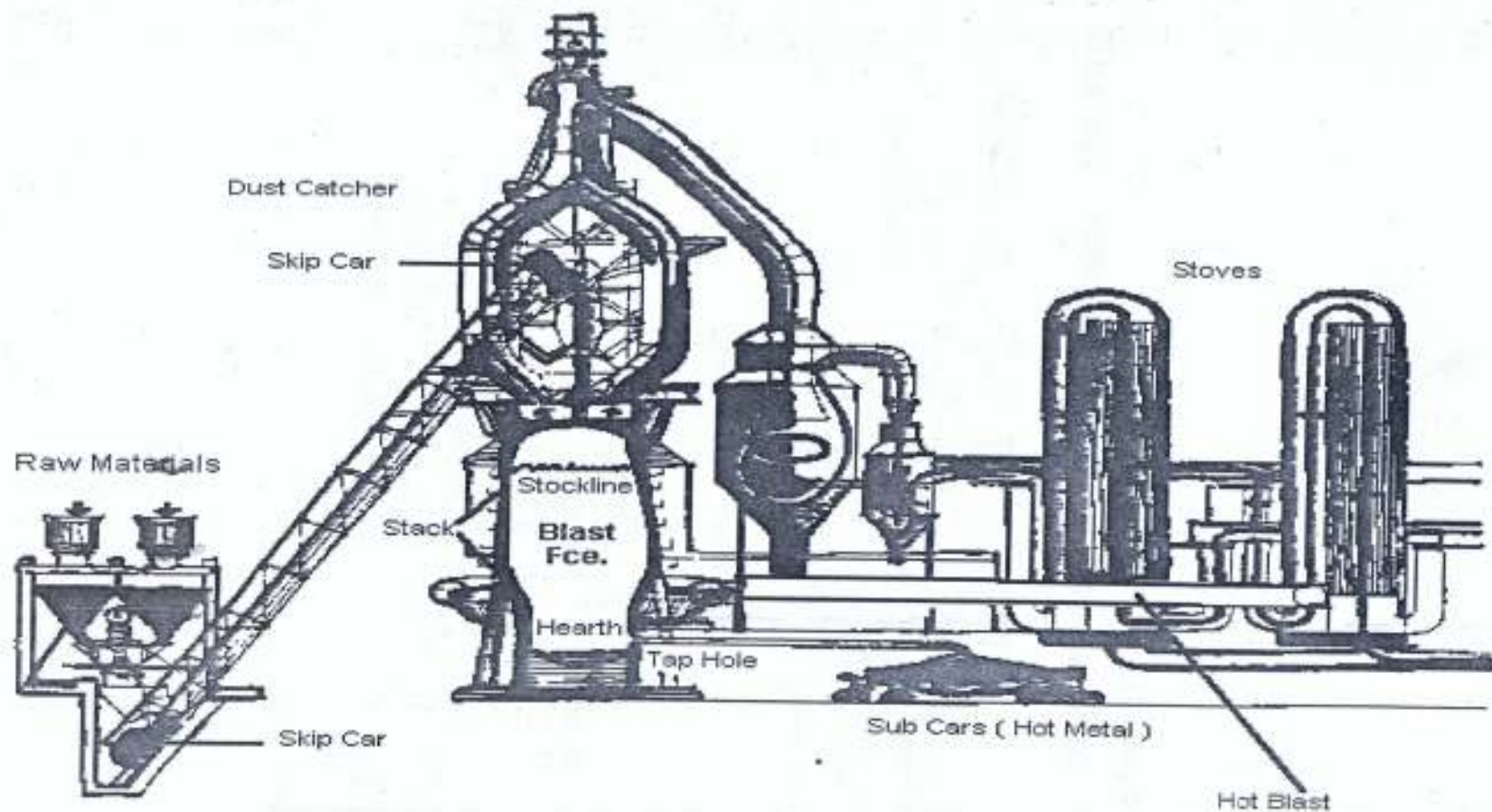


Figure 1 - The Modern Blast Furnace\*

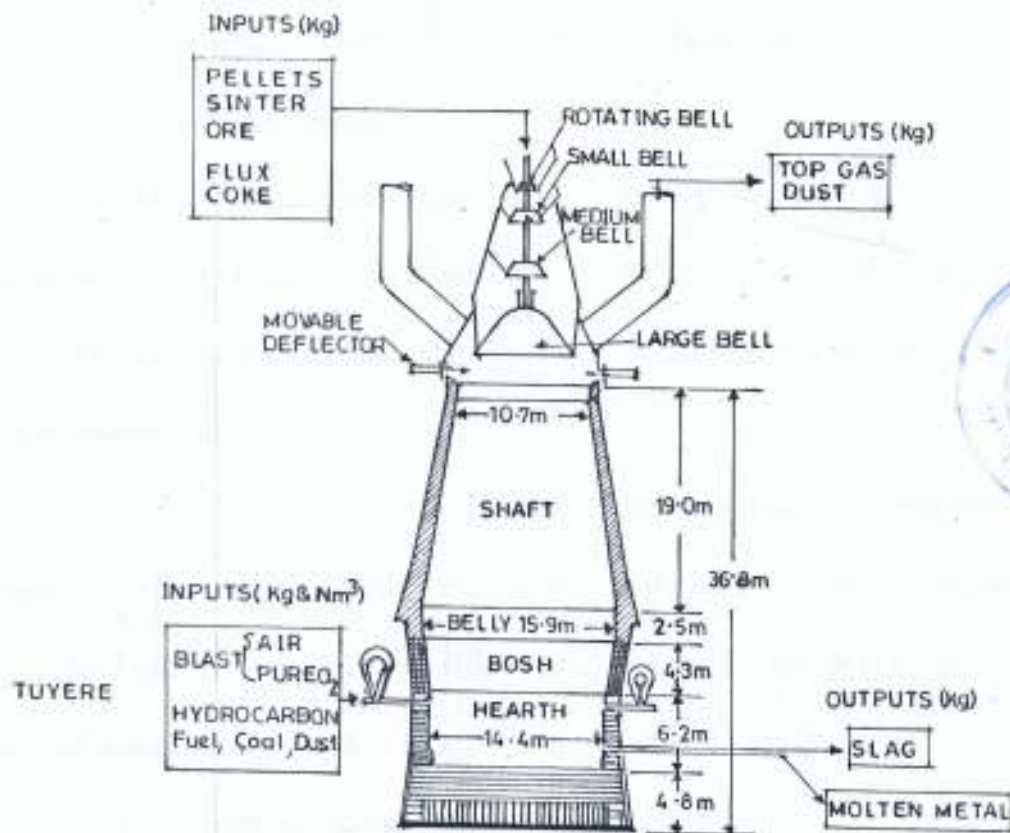


Fig 2 : Vertical profiles of a blast furnace showing its materials balance.

In a typical blast furnace, the Iron notch is situated at a height of 1.1m above the hearth bottom. The slag notch is located at a height of 1.8m above the Iron notch while the tuyeres is located at a height of 3.4m above Iron notch. Hot blast from stoves passes through the bustle pipe situated at bosh level. The bustle pipe is however located at a height of 5.5m above Iron notch.

The principal objective of the furnace is to produce molten iron of constant composition at a high rate. The furnace is of self supporting, free standing design in which the furnace shell from the hearth base to the furnace top ring is carried on a base ring at foundation level.

Many efforts were made in the 20<sup>th</sup> century towards the improvement of the operations of the furnace which were aimed at; Better and smoother operation of the furnace; Increase in productivity to reduce production cost and meet increasing demands; Reduction coke consumption which is very expensive due to diminishing reserves of cooking coal. These improvements are discussed in section.

## **2.2 BLAST FURNACE OPERATION**

In modern blast furnace, the charge; coke from the coke over plant, flux, and sinter ore from the sintering plant, are conveyed through conveyor belts, and discharged into the receiving hopper of the blast furnace. In the conveyor system, one belt conveys sinter and flux, and the other conveys coke.

The charge is received by the hopper, and falls into the small bell. After each feed, the hopper revolves through an angle and the small bell opens, the charge is evenly distributed over the by bell. As the small bell closes, the by bell lowered, and the charge falls into the throat of the furnace.

Hot blast is supplied form the hot stones to the bustle pipe, and is blown through the tuyeres at the bottom of the furnace. It enters at a velocity of between 200 to 300mws-1 and a pressure of 2 to 4 atmosphere, so as to push the reducing gasses through the solid burden and to overcome the top pressure of the furnace.

According to Peacey (1979), the high velocity of the blast clears a raceway of gas and rapidly hurtling coke in front of each tuyere (Fig. 3). The bottom-most of this zone periodically fall into the raceways to be consumed by the incoming air, and hence the whole bed is always gradually moving down to be re-supplied at the top with coke from above. The hot blast reacts with the coke and the injectant in the belly and bosh of the furnace to form a mixture of carbon monoxide and nitrogen. The combustion of coke at the tuyere level raises the temperature to between 1800 and 2100<sup>0</sup>C (Coudrier 1985).

This mixture ascends in the furnace while exchanging heat and reacting with the raw materials descending from the furnace top. The gas is eventually discharged from the furnace top. The gas is eventually discharged from the furnace top materials and recovered for use as fuel in work. During this process, the layer-thickness ratio of iron-bearing materials to coke charged from the furnace top and their redial distributions are controlled so that the hot blast can pass with appropriate radial distribution. During the descent of the burden in the furnace, the iron-bearing materials are indirectly reduced by

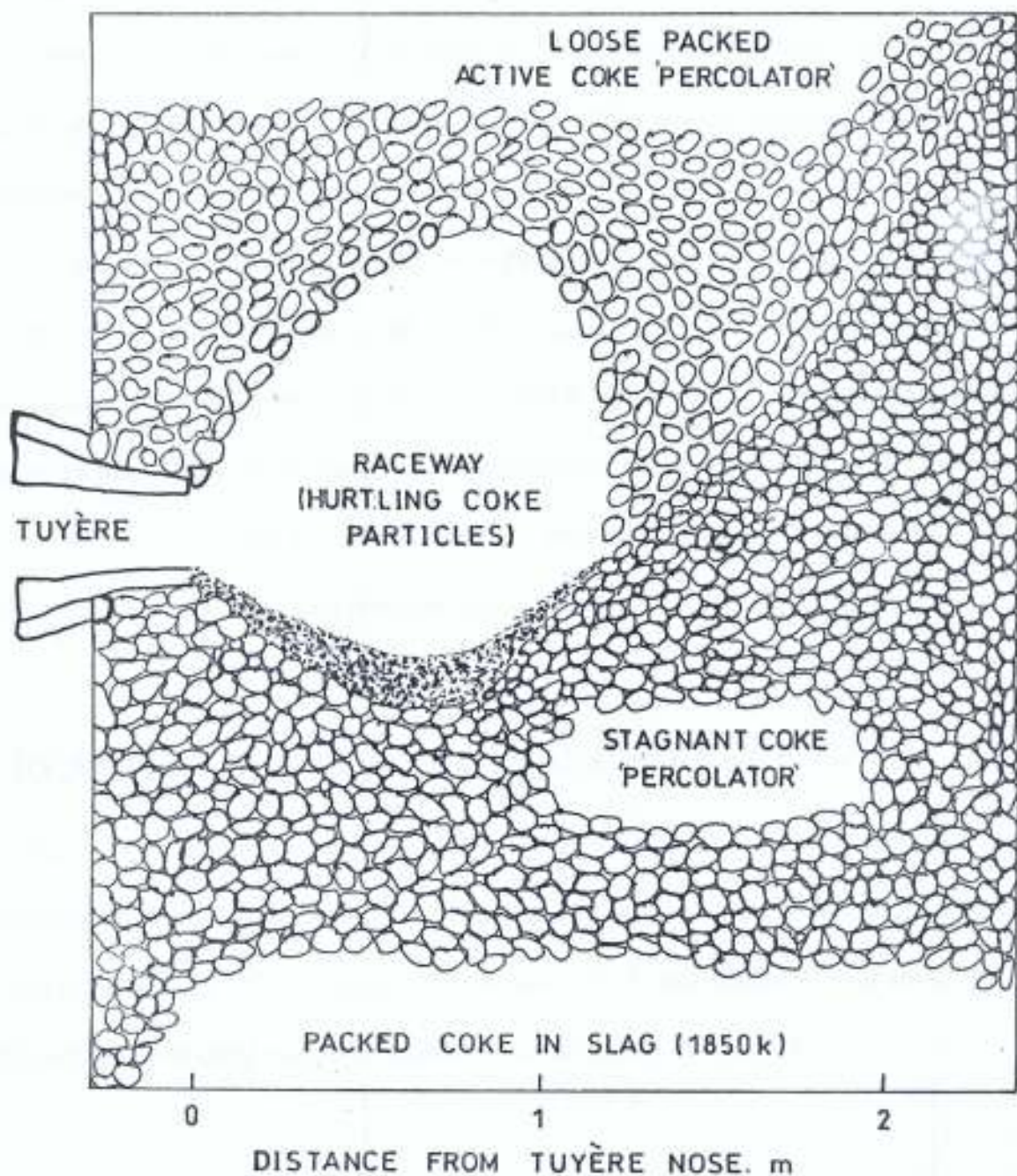


Fig.3 : Schematic view of tuyère region of the blast furnace.

carbon monoxide gas in the low-temperature zone of the upper furnace. In the lower part of the furnace, carbon dioxide, produced by the reduction of the remaining iron ore by carbon monoxide is instantaneously by coke (C) into carbon monoxide, which again reduces the iron oxide. According to Ghosh and Ray (1991), the CO becomes more stable at higher temperatures whereas all metal oxides generally less stable.

The overall sequence can be regarded as direct reduction of iron ore by solid carbon in the high-temperature zone of the lower furnace. The reduced iron simultaneously melts, drips and collects as hot metal at the hearth. The hot metal goes downward to the bottom of the hearth and the slag produced floats on top of the molten metal. The hot molten metal is tapped at regular intervals (usually 2-3 hours) from the iron notch while the slag is tapped from the slag notch.

## **2.3 REACTION ZONES IN THE BLAST FURNACE**

The blast furnace is a packed bed reactor in which there is a counter current flow of solid materials from top and gases from bottom. The results the dissection of quenched blast furnace (Kanbara 1977, Yasuto 1977, Minoru 1977, and Kojiro 1977), show that, the blast furnace is divided into five reaction zones as shown in Figure 4.

### **2.3.1 LUMPY ZONE**

The materials here are solid and gases. The solid are sinter, fluxes, and coke, while the gas is a mixture of CO, CO<sub>2</sub>, N<sub>2</sub>, and H<sub>2</sub>, which have taken part in reduction reactions

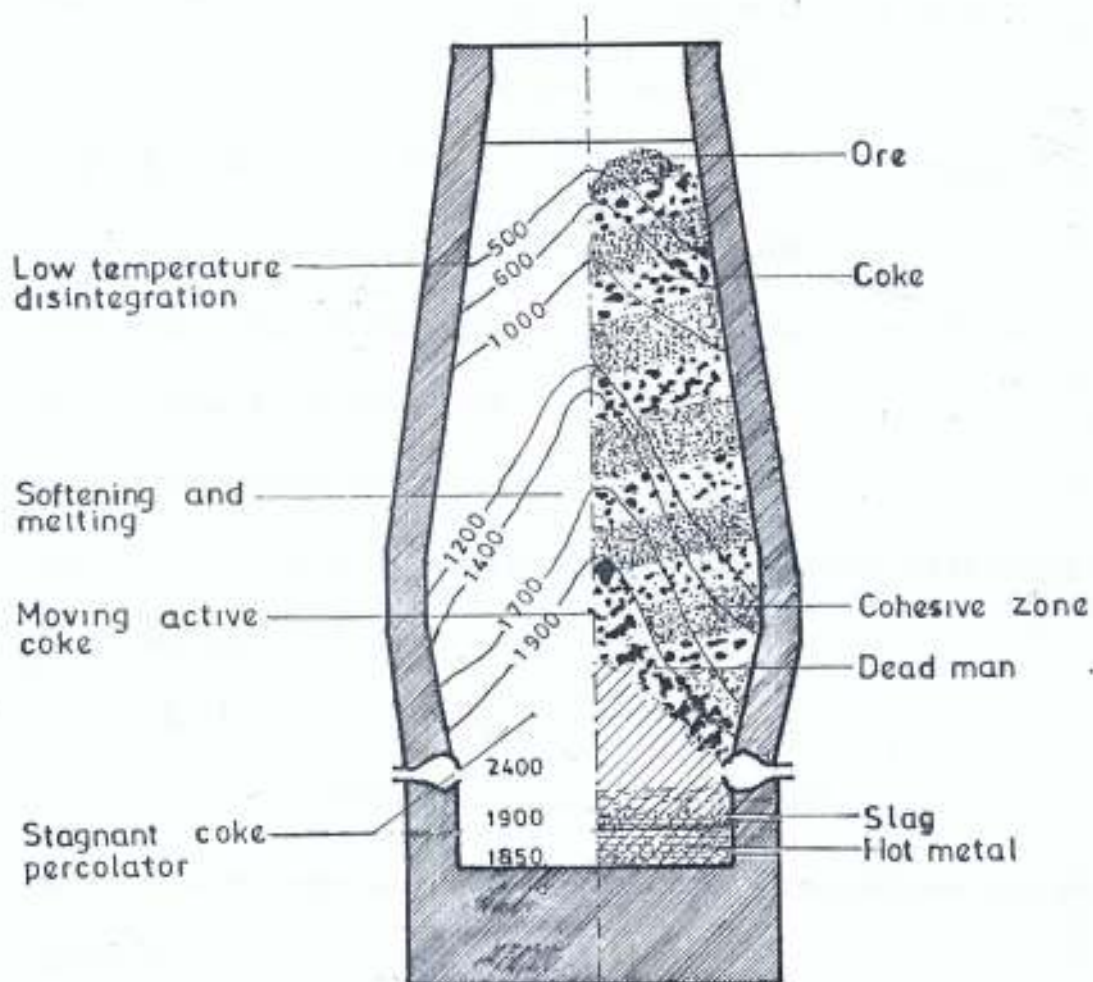
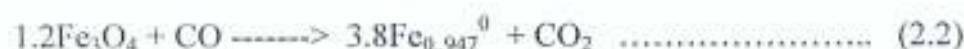


Fig.4: Schematic drawing of the inside of a blast furnace.

further down in the furnace. Here the indirect reduction of iron oxides take place, some of which are;



$$\Delta H_{298} = -4800\text{kJ}(\text{kg mole CO})^{-1}$$



$$\Delta H_{298}^0 = + 50,000\text{kJ}(\text{kg mole CO})^{-1}$$

Temperature of the gas falls rapidly as it passes through this zone due to

- (i) Cooling by incoming solids
- (ii) Evaporation of moisture and
- (iii) Net endothermic nature of reducing higher oxides to FeO according to the reaction.



$$\Delta H_{298}^0 = + 13,000\text{kJ}(\text{kg mole CO})^{-1}$$

It is also in this zone that reduction accompanied by degradation takes place as shown in.

## 2.3.2 SOFTENING - MELTING ZONE

This zone consists of solids, gases and small amount of liquids. The boundaries of this zone are characterised by the beginning of softening of iron-bearing burden materials as defined by 10 percent contraction under load (Lu 1979) and the commencement of melting of sponge iron into liquid metal and slag. The location and shape of this zone

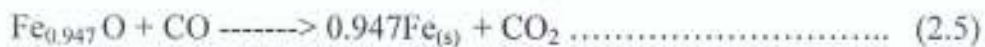
depends on relative total heat capacity of gaseous and solid streams. Factors such as higher fuel rates, less limestone addition or lower melting temperature for sponge iron will cause the melting front to move further up or further away from the tuyere level.

In this zone, both direct and indirect reduction reactions take place as well as coke gasification (solution loss). Not all the FeO produced can be completely reduced because of the reversing action of CO present (Nat 1992), thus the carbon accomplishes the reduction.

#### *Direction reduction*



#### *Indirect reduction*



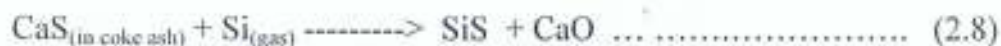
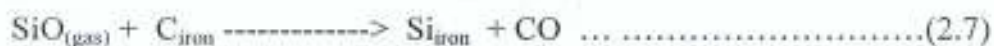
$$\Delta H_{298}^0 = -1700 \text{ kJ}(\text{kg mole CO})^{-1}$$

#### *Coke gasification*



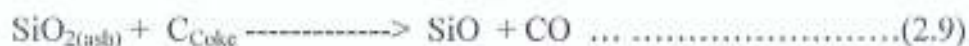
$$\Delta H_{298}^0 = 172000 \text{ KJ}(\text{kg mole CO})^{-1}$$

Other events in this zone are the absorption of silicon and sulphur by liquid metal and slag via the following reactions.



### 2.3.3 DRIPPING ZONE

The only solid material left here is coke, and the rest are gases and liquids. Here direct reduction and solution loss reactions start. Generation of silicon monoxide from coke ash takes place according to the reaction.



When droplets of liquid metal and slag tuckle down through the coke bed, silicon, sulphur, and heat are being transferred from gas to liquids. The large gas/liquid contact area and high temperature makes the dripping zone a very important region for reactions. The longer the dripping distance or time (i.e. the higher the location of the melting front). The more the silicon and sulphur, the more heat will be transferred within the coke bed.

### 2.3.4 RACEWAY ZONE

This zone consists of coke and gas. The raceway extends 1-2 meters into the furnace and are bound in front at the sides and below by rather firm regions of lump coke which have bypassed oxidation during its descent through the furnace. The raceways are also bounded above by lump coke but loosely packed due to the rapid ascent of raceway gas between the pieces.

The main activity in this zone is CO generation. This is a two step reaction; oxygine first reacts with coke to form CO<sub>2</sub>.



$$\Delta H_{298}^0 = - 394,000\text{kJ}(\text{kg mole CO}_2)^{-1}$$

The net result of these two reactions is generation of heat, which is carried upwards into the furnace by the ascending gases, which also contains sulphur. Some SiO is generated in the peripheral region of the furnace.

In a furnace operation, where hydrocarbon is injected, the cracking of the hydrocarbon with the attendant loss of heat takes place in this zone and additional CO and H<sub>2</sub> generation

### 2.3.5 HEARTH ZONE

The hearth contains only coke and liquids (slag through the stagnant coke in bosh and hearth to be periodically or continuously (only in big furnaces) tapped from the furnace. The hearth region determines the quality of the hot metal (Williams 1983).

The high temperature reached in this zone lead to the reduction of the stable oxides MnO, SiO<sub>2</sub> and the phosphates. Silicon and manganese are dissolved in the iron and slag is formed from the ore gauge. As the hot metal iron passes through the slay layer, there is the oxidation of silicon by iron and maganese oxide in the slay, and also the desulphunisation of metal.

The reactions take place are; (Tukdogan 1978 and 1980)



The underscore indicates elements dissolved in iron.

**TABLE 1**

Summary of Reactions and Thermal Behaviour in Various Regions of the Iron Blast  
Furnace (steady-state conditions)

| Zone                              | Chemical Behaviour                                                                                                                                                           | Thermal Behaviour                                                                                                                                                                           |
|-----------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Hearth (below tuyeres)            | Saturation of iron with carbon and final reduction of (CaO), $P_2O_5$ , MnO and $SiO_2$ . Impurities reach their final concentrations.                                       | Falling drops of metal and slag bring heat down into the hearth.                                                                                                                            |
| Tuyere raceways                   | Coke and hydrocarbons are oxidized to $CO_2$ then CO                                                                                                                         | Large evolution of heat from combustion of incandescent coke with hot air                                                                                                                   |
| Active coke zone (bosh and belly) | Impurity oxides are reduced and iron absorbs carbon during percolation of metal and slag droplets. Coke bed acts as a reserve to guarantee complete reduction of iron oxides | Transfer of heat from ascending gas to descending coke and droplets of metal and slag. Gas supplies enthalpy for superheating of liquid metal and slag and for reduction of impurity metals |
| Fusion zone                       | Formation and melting of slag, final reduction of $Fe_{0.947}O$ , melting of Fe                                                                                              | Transfer of heat from ascending gas to melting solids                                                                                                                                       |
| Cyclic                            | Wustite reduction and coke                                                                                                                                                   | Temperature of ascending gas                                                                                                                                                                |

|                        |                                                                                                                                                                                                                                                       |                                                                                                                                                                |
|------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------|
| reduction zone         | gasification                                                                                                                                                                                                                                          | falls rapidly due to absorption of enthalpy.                                                                                                                   |
| Middle of Shaft        | Very little coke gasification occurs. Reduction of $\text{Fe}_{0.947}\text{O}$ by CO over much of the zone. Little or no reaction in higher portions due to depletion of CO (chemical reserve zone). Wustite is the iron oxide throughout this region | Steady temperature (1200K) throughout, (thermal reserve zone). Wustite reduction of Fe requires no enthalpy.                                                   |
| Upper quarter of Shaft | Reduction of $\text{Fe}_2\text{O}_3$ and $\text{Fe}_3\text{O}_4$ to wustite                                                                                                                                                                           | Temperature of gases decreases rapidly due to transfer of heat to cold incoming solids. Reduction reactions and evaporation of moisture also require enthalpy. |

## 2.4 IMPROVEMENTS IN BLAST FURNACE OPERATION.

The severe competition into which the blast furnace has entered with alternative processes during the past years has not modified its predominant position as a reducing unit, but on the contrary, it had quite a stimulative effect (Poos 1981). Several efforts have

been made towards improving the operations of the furnace to enhance high productivity, efficiency, and reliability. These are achieved by the following factors.

- (i) Burden type
- (ii) Gas permeability
- (iii) Blast enrichment
- (iv) Coke quality
- (v) Blast injectants
- (vi) Blast velocity
- (vii) Burden arrangement and uniformity
- (viii) Operating temperature
- (ix) Operating pressure
- (x) Furnace capacity
- (xi) Cooling system

### **2.4.1 BURDEN TYPE**

For the production of iron at minimum cost and efficient operation of the iron blast furnace, a burden of optimum properties is necessary (Egundebi 1986). Compare to a lump ore practice, pellets provided for increased permeability, more uniform reducing gas distribution, improved reducibility of the burden, and a smoother stock (Holditch and Eikidysz 1986). Lumps and pellets melt earlier than sinter. Sinter proves to be the more favourable on account of its higher temperature softening and melting point (Walter

1996). Burden that melts easily have a negative effect on the reducing action of the process. To reduce gas permeability (Panigrahy and Rigand 1986) concluded that Ca-ferrite provide good physical strength and reduction properties, and possess high softening and melt-down properties.

## **2.4.2 BURDEN ARRANGEMENT AND UNIFORMITY**

Up to the fusion zone, the burden is made up of alternate layers of ore and flux usually 0.5 - 1m thick. Burden distribution at the stock-line is one of the most important factors governing furnace operation (Standish 1986). Uniform gas-flow especially in the stack is due to proper distribution of burden right from the receiving hopper. Uniform burden permits furnace gases to rise rapidly through the charge without channeling and allow the furnace to be operated at high blast rates.

Proper separation of coke and sinter from fines is usually maintained. Coke and sinter both tend to abrasion, which affects the blast furnace (Benhard 1992). Arrangement of the conveyor system, and the bell top charging system helps in proper layering of the charge inside the furnace, thereby improving the gas flow.

## **2.4.3 GAS PERMEABILITY**

The productivity of blast furnace is defined as the quotient between the possible gas throughput per unit of time and the specific gas generation for one tone of hot metal (Walter 1996). The gas throughput is a function of the furnace permeability (Beppler 2000), through high quality charge materials. The quality and behaviour of charge in the

blast furnace determines the permeability. Good permeability can be achieved by having the different components of the charge in their correct sizes range. Non-uniform sizing of materials results in non-uniform gas flow and thereby reduced furnace permeability. Fines results in coke penalty and reduction of productivity.

Flow equation for packed beds have been developed by many workers (Furnas 1929 and Ergun 1952), and the relationship between pressure and gas flow rate in a packed bed is given by the Ergun equation.

$$\frac{P}{L} = 1.75 \frac{1 - \Sigma}{\Sigma \phi D_e} \frac{G^2}{P_g}$$

P = Pressure drop

L = Length or height of packed column

$\Sigma$  = Void fraction

$\phi$  = Shape fraction

$P_g$  = Density of the gas

$D_e$  = Equivalent particle diameter

G = Mass flow rate (Gas velocity)

The equation shows that an increased top pressure increases gas density and decreases resistance to flow. The equation is rearranged to define the burden permeability 'K' as:

$$K = \frac{G^2/P_g}{P/L} = 0.57 \frac{\Sigma^3 \phi D_e}{1 - \Sigma}$$

Permeability 'k' is proportional to the equivalent particle diameter  $D_e$ , the shape factor i.e. approach to sphericity and the quantity

$$\frac{\Sigma^3}{1 - \Sigma} \cdot \frac{1-2}{\Sigma^3} = \text{Resistance to flow.}$$

The permeability increased as particle diameter and void fraction increases.

#### 2.4.4 COKE QUALITY

Coke does not change in state of aggregation down to the tap hole level. Therefore, the properties of coke in the cohesive zone are of special importance. Coke functions as;

- (1) The supplier of the reducing gas and heat.
- (2) Supporting structure for the burden.
- (3) Gas distributor
- (4) The direct reduction of iron oxides.

Since efforts are being made to minimize coke consumption by using alternative fuel injectants, the quality of coke charged and the charging techniques is paramount importance. The quality of coke influences the blast furnace performance especially if high rates of additional reducing agents are injected (Beppler 1999). To achieve a uniform furnace working, and good operating results, the process must take place evenly around the furnace centre line (Peter and Poth, 1986). Tuyere flame temperature and blast velocity have a great influence on the degradation of coke (Iwanaga, Takatani, and

Aminaga 1986), leading of the system. For this reason, a greater quantity of coke must be charged into the furnace centre as the injection rate increases (Beppler 1999).

The quality of coke needed for a good operation of the blast furnace are based on:

- (1) High hot coke strength (CSR), and lower coke reactivity (CRI) (Beppler 1996).
- (2) Coarse coke to ensure high voidage gas permeability (Beppler 2000)
- (3) Low ash to increase the rate of burden yield and to reduce coke disintegration (Beppler 1994). Low sulphur content so as to get an acid slag. Low phosphorus and volatile matters.

Hearth disturbances in the blast furnace can be avoided by maintaining a suitably high CSR (Kerkkonen 1997). As the CSR value increases, alternative fuel injection can be move, thereby lowers the level of coke consumption, and increasing gas permeability.

## 2.4.5 BLAST INJECTANTS

The goal of alternative fuels injection through the tuyere is to demonstrate the economic, environmental, and energy savings benefits by minimising the amount of coke consumption and the reduction of the harmful emissions from the coke oven plants.

The choice of these fuels depends on many factors of which relative abundance and cost are paramount. For example, Canada, India, and UK use pulverized coal, Nigeria and part of USA use natural gas, and according to Tsukasa (1998), presently researches in Japan are being carried out on the use of plastic. The success of these injectants is

dependent on their combustion rate as well as the control of the gas distribution. Their choice is dependent on the following.

- (i) Their effect on bosh slag basicity.
- (ii) Flame temperature
- (iii) Utilization of hydrogen in indirect reduction of iron oxide.
- (iv) Productivity
- (v) Fuel requirement
- (vi) Coke replacement ratio

Alternative fuel injection requires additional blast heat, thus a combined blast i.e. simultaneous injection of atmospheric blast, process oxygen and injectants is adopted (Ulianor 1986). Thus a working relationship is established to maintain a thermal balance, since injectants reduced the flame temperature. In iron making process in the blast furnace, the injectants' carbon combines with the ore's Oxygen to form Carbon monoxide and Hydrogen gas leading high quality molten iron with a lower Oxygen contents (Tsukasa 1998).

Various work have been carried out on different injectants and results have shown that they have different effects (Guili 1986, Tavorovskii 1980, Gudenau 1986, Ulianor 1986, Watanable 1986, and Athapan 1996). High slag basicity has an adverse effect on the permeability of the furnace, thus reducing productivity. Low ash basicity leads to better liquidus temperature, fluidity, and permeability (Athapan 1996).

High injection rate increases the residence time (Antonic 1994 and Gudenan 1986). High residence time increase combustion degree, and affects coke degradation.

Tovarovskii (1980) gives the coke Replacement Ratio (RR) for various injectants.

For Natural gas

$$RR = (3.2T/2000 + 2.3) \Delta r$$

$$\Delta r = 0.2 - 2.5 \times 10^{-4} V_{ng}$$

Coke oven gas

$$RR = (2.3T/2000 + 2.3) \Delta r$$

$$\Delta r = 0.10 - 10^{-4} V_{cg}$$

Fuel oil

$$RR = 1 + 0.4T/2000$$

$$\Delta r = \text{Constant}$$

$\Delta r$  = increase in the degree of indirect reduction per unit blast addition.

T = Flame temperature

$V_{ng}$  = Consumption of natural gas NG, m<sup>3</sup>/t pig iron

$V_{cg}$  = Consumption of coke oven gas CG, m<sup>3</sup>/t pig iron

## 2.4.6 BLAST TEMPERATURE AND VELOCITY

The overall heat required for the blast furnace is obtained from the heat of coke gasification, which is dependent on the temperature of the blast. The introduction of injectant lowers the operating temperature of the furnace. Oxygen enrichment, and increasing the blast temperature compensate for such. The blast temperature is usually 1200°C or up to 1400°C, but the flame temperature must be within the range of 2200K and 2600K (Peacey 1978, Tovarovskii 1980).

To obtain sufficient kinetic energy of the blast, the velocity must be high enough, even up to 250m/s (Jose 1998). When there is fuel injection, the velocity of the blast must be increased, because some gases like  $N_2$ ,  $H_2$ , and  $O_2$  are gasified before the tuyere tip. The velocity therefore needs to be increase by 15m/s in view of the composition of the injectant (Beppler 1994).

## 2.5 OPTIMIZATION CONCEPTS AND ITS APPLICATION IN STEEL INDUSTRY

### 2.5.1 CONCEPT OF OPTIMIZATION

Optimization means to select the best course of action from the available alternatives (Ray W.H. and Szekely Y. 1973). It involves finding the best solution to a problem. Mathematically, this means finding the minimum or maximum of a function of  $n$  variables,  $f(x_1, \dots, x_n)$ , say, where  $n$  may be any integer greater than zero (Beale 1988). The function may be unconstrained or it may be, subject to certain constraints on the variables of the function.

The Linear Programming (LP) is one of the most widely used optimization techniques, and one of the most effective (Edgar and Himmelblan 1989). The term linear Programming was coined by George Dantzing in 1947 to refer to the procedure of optimization in problems in which objective function and the constraints are linear (Dantzig 1963). Once the mathematical programming model has been formulated, we communicated it to the computer programme. The LP has a wide range of application especially in Engineering, Agriculture and Manufacturing.

## 2.5.2 APPLICATION OF OPTIMIZATION IN THE STEEL INDUSTRY

Mathematical programming techniques were used in the steel industry as early as 1958, and many application of optimization in steel production have been reported since then. Duttal and Fourer (2001). A survey of published applications of optimization are summarised below.

### 2.5.2.1 PRODUCTION PLANNING

Tsao and Day (1971) developed a process analysis model of production in the United States on a national level. A technology matrix is estimated using engineering and metallurgical information. This matrix together with the detailed cost, sales and revenue figures is then used in LP model of short run allocations of the steel industry as a reliable. The study of Mexican steel modeled, by Kendrick, Meeraus, and Alatoire (1984) developed two static models for production planning and one dynamic model for investment analysis. The two static models, formulated as linear programming models, are mixed production and transportation problems. The dynamic model, formulated as a mixed integer programme. Their inputs were similar, and the outputs were, optimal product distribution, and investment decisions.

In the production planning in Zambia, sashidhar and Achray (1991a) deal with the problem of planning in a steel mill with the objective of maximizing capacity utilization. The model is formulated as a maximum flow problem in a multiple activity network formulation for production planning with the priorities in

a steel mill. In another paper, Sashidhar and Achray (1991b) discussed the problem of allocating the major components of process costs to various quantities of products produced in a smelting shop of an alloy and special steel manufacturing unit. Quadratic programming techniques was used to estimate the consumption pattern of important operational materials.

Also, in the production planning in Algeria, Sarma (1995) describe an application of lexicographical goal programming at the only steel manufacturing plant; Societe Nationale de Siderurgie. The lexicographical approach has helped the management to spell out aspiration level of several principal objectives such as profitability, capacity utilization of some key plants, and production quantity of some key products.

Bielefeld et al (1986) describe an L-P based supply chain planning model which plans purchasing, production, and distribution for many products in many plants on an annual basis for Hoesch, a German Steel-maker.

#### **2.5.2.2 PRODUCT - MIX OPTIMIZATION**

Fourer (1997) presents a model which grew out of a project to design an optimization package for steel mill planning for American iron and steel institute. This was based on generic model, which could be customized by any steel plant to its own operation, simply by supplying its own data, which has been proved successful. In United Kingdom, Lawrence and Flowerdew (1963) develop an economic model for steel production that focussed on the application to the individual process. Bandyopadhy (1969) also proposed a linear programming

model that allocates different capacities between two processes for production planning, namely basic oxygen furnace and the open hearth furnace. The model is a cost minimization model with all technological and financial constraints. The model can also predict the required operation level of blast furnace and lime burning plant at different level of total steel production.

In the Indian steel plant, Dutta, Sinha, and Roy (1990), Dutta et al (1994), and Sinha et al (1995) deal with the development and implementation of a mathematical model for optimal allocation of electrical energy of Tata steel. The guiding principle of the model is that in the case of a power shortage, power is allocated to those non-essential loads which have a higher profitability (based on a mixed integer linear programming model). Hunneault and Galiana (1991) McCutcheon (1988), later reported the use of power plants, such studies have addressed the issue with a cost minimization modeling approach for power generating and distributing plants. Fabian (1958), Biellfield, Walter and Wartman (1986), Baker et al (1987) studied the most profitable use of an integrated steel plant, where the problem has been addressed as a cost minimization or profit maximization linear programming model. In the steel authority of India limited, Shama and Sinha (1991), describe an optimization model for determining the optimal product mix in which various issues relevant to the choice of an optimum product mix in a steel making operation.

### 2.5.2.3 BLENDING MODELS

Generally, the problems are formulated as cost minimization linear programming models.

In the United State blast furnace/cupola blending, the results obtained from Fabian (1967) enable producers to determine among others, the least cost raw material, blending, optimal furnace scheduling and optimal raw material inventory level. Metzger and Schwarxreck (1961), describe an application of linear programming for the determination of least cost cupola charging in an iron foundry. Actual data, evolution of the solution, and cost saving were obtained from the work.

In United Kingdom, Beale, Coen, and Flowerdew (1965), proposed a model in which the variables are usages, in a given time period of ore and other materials, outputs of gi iron, and levels of certain factors that depend on the mix of materials.

In Belgium, Hernandez and Proth (1982) approached the problem of selecting the charge materials from available stock in order to produce alloy as cheaply as possible which extremely important to foundaries producing micro components alloys, such as bronze and special steels, through the use of a new algorithm. The system has been implemented to give an improvement in profit.

In Sweden, Westerberg, Bjorkland and Hultan (1977) carried out work on Fagersta AB, and the contact Research Group Applied Mathematics, Royal Institue of Technology in stock-holum. The problem was modeled as a traditional blending model with the additional constraint that some of the variables should be

integer valued. The company produce stainless steels in high frequency furnaces, and used up to fifteen different types of scrap and alloys which are melted together. The linear programming model is a cost minimization model with constraints given by weight restrictions and metallurgical composition restriction. The implementation of the model has decreased the cost raw material by 5%.

In East European countries, Muteana and Rado (1960) solved a blending problem in a Rumanian Steel Plant that deal with the raw material loading of an iron-smelting furnace in such a way as to obtain an optimal production at minimum cost of pig iron, taking into account definite prescribed production. Tarabar (1963) developed a model in Yugoslavia, which has a objective of profit maximization. It provides an elementay example of the use of the linear programming and in deciding the composition of furnace charge for blast furnace.

#### 2.5.2.4 BLAST FURNACE OPERATION



Many researchers have carried out work, and the development of models for the operation of blast furnace. Peacey and Davenport (1979) development models for the blast furnace operation, focussing on the use of alternative fuel injectants. The modelts can be used to determine cost of materials, raw materials balances, and the thermal requirement and implication on the furnace.

Deitz (1997), describes a system developed by Voest Alpha Stahl, an Austrian firm, for controlling blast furnace performance. The system consist of a series of computer models for various phases of blast furnace operation. It includes a burden optimization model for determining the optimal mix of inputs,

while other models determine control settings and hot metal qualities. Zuo et al (1998) report on the design of three models base on neural network for recognition of top gas distribution, distribution of the heat fluxes through the furnace wall, and the prediction of slips in the blast furnace. Inkala et al (1995), describes the application of an expert system, at the finish firm Rautaruukki Oy, to blast furnace control. Iida et al (1995) describes several AI applications at Kawasaki steel including fuzzy inference applied to store heat control and a neural network application to blast furnace burden distribution control. Angstenberger (1996) describes the application of fuzzy clustering and neural network to blast furnace modeling and control at a German steel producer.

## 2.6 THE MATLAB

MATLAB is a mathematical programming language built for solving the tedious and the resulting interface slow problem, in interfacing in an environment where complex mathematical calculations are involved. MATLAB stands for Matrix Laboratory. It was originally written to provide easy access to matrix developed by LINPACK and ELSPACK projects, which together represent the state-of-the-art in software for matrix computation. In industry, MATLAB is the tool of choice for high productivity research, development, and analysis, in university environments, it is the standard instructional tool for introductory and advanced courses in mathematics, engineering, and science.

MATLAB is a high – performance language for technical computing. It integrates computation, visualisation, and programming in an easy-to-use environment where problems and solutions are expressed in familiar Mathematical notation. Typical uses include;

- (1) Math and Computation
- (2) Algorithm development
- (3) Modelling, simulation and prototyping
- (4) Data analysis, exploration, and visualisation
- (5) Scientific and engineering graphics
- (6) Application development including graphical user interface building

MATLAB is an interactive system whose basic data element is an array that does not require dimensioning.

This allows solving many technical – computing problems, especially those with matrix and vector formulations, in a fraction of the time it would take to write a program in a scalar non – interactive language such as C or Fortran.

MATLAB features a family of application – specific solutions called toolboxes. Very important to most users of MATLAB, toolboxes allow you to learn and apply specialised technology. Toolboxes are comprehensive collections of MATLAB functions (M-files) that extend the MATLAB environment to solve particular classes of problems. Areas in which tool boxes are available include signal processing, control systems, neural networks, fuzzy logic, wireless, simulation, and many others.

## **2.6.1 THE MATLAB SYSTEM**

The MATLAB system consists of five main parts:

1. The MATLAB language. This is a high-level matrix/array language with control flow statements, functions, data structures, input/output, and object-oriented programming features. It allows both “programming in the small” to rapidly create quick and dirty throwaway programs, and “programming in the large” to create complete large and complex application programs.
2. The MATLAB Working Environment. This is the set of tools and facilities that you work with as the MATLAB user or programmer. It includes facilities for managing the variables in your workspace and importing and exporting data. It also includes tools for developing, managing, debugging, and profiling M-files, MATLAB’s applications.

3. **Handle Graphics ®.** This is the MATLAB graphics system. It includes high-level commands for two-dimensional and three-dimensional data visualisation, image processing, animation, and presentation graphics. It also includes low-level commands that allow you to fully customise the appearance of graphics as well as to build complete graphical user interfaces (GUIs) for your ops Operators and special characters.
4. **The MATLAB Mathematical Function Library.** This is a vast collection of computational algorithms ranging form elementary functions like sum, sine, cosine, and complex arithmetic, to more sophisticated functions like matrix inverse, matrix eigenvalues, Bessel functions and fast Fourier transforms.
5. **The MATLAB Application Program Interface (API).** This is a library that allows you to write C and Fortran programs that interact with MATLAB. It includes facilities for calling routines form MATLAB (dynamic linking), calling MATLAB as a computational engine and for reading and writing MAT-files.

### **2.6.1.1 PORTABILITY**

It's sometimes necessary to work with MATLAB implementations on different computer systems, or to transmit MATLAB applications to users on other systems. MATLAB applications consist of M-files, containing functions and scripts, and MAT-files, containing binary data. Both types of files can be transported directly between different computers:

1. M-files consist of ordinary text. They are machine independent. While different platforms terminate lines with various combinations of CR (carriage return) and LF (line feed) characters, the MATLAB interpreter tolerates all possible combinations. (However, text editors and other tools may not work correctly with M-files from other platforms.)
2. MAT-files are binary and machine dependent, but they can be transported between machines because they contain a machine signature in the file header. MATLAB checks the signature when it loads a file and, if a signature indicates that a file is foreign, performs the necessary conversion.

To use MATLAB across different platforms, you need a program for exchanging both binary and text data between the machines. When using these programs, be sure to transmit MAT-files in binary file mode and M-files in ASCII file mode. Failure to set these modes correctly usually corrupts the data.

### **2.6.1.2 M-FILES**

Files that contain MATLAB language code are called M-files. M-files can be functions that accept arguments and produce output, or they can be scripts that execute a series of MATLAB statements. For MATLAB to recognize a file as an M-file, its name must end in .m. You create M-files using a text editor, then use them as you would any other MATLAB function or command.

### **2.6.1.3     SCRIPTS**

Scripts are the simplest kind of M-file – they have no input arguments. They're useful for automating series of MATLAB commands, such as computations that you have to perform repeatedly from the command line.

Scripts operate on existing data in the workspace, or they can create new data on which to operate. Any variables that scripts create remain in the workspace after the script finishes so you can use them for further computations.

### **2.6.1.4     FUNCTIONS**

Functions are M-files that accept input arguments and return output arguments. They operate on variables within their own workspace. This is separate from the workspace you access at the MATLAB command prompt.

#### **2.6.1.4.1   BASIC PARTS OF A FUNCTION M-FILE**

A function M-file consists of:

1.    A function definition line
2.    A H1 line
3.    Help text
4.    The function body
5.    Comment

#### 2.6.1.4.2 FUNCTION DEFINITION LINE

The function definition line informs MATLAB that the M-file contains a function, and specifies the argument calling sequence of the function.

ALL MATLAB functions have a function definition line that follows this pattern. If the function has multiple output values, enclose the output argument list in square brackets. Input arguments, if present, are enclosed in parentheses. Use commas to separate multiple input or output arguments.

#### 2.6.1.4.3 H1 LINE

The H1 line, so named because it is the first help text line, is a comment line immediately following the function definition line. Because it consists of comment text, the H1 line begins with a percent sign “%”.

This is the first line of text that appears when a user types help function name at the MATLAB prompt. Further, the **lookfor** command searches on and displays only the H1 line. Because this line provides important summary information about the M-file, it is important to make it as descriptive as possible.

#### 2.6.1.4.4 HELP TEXT

You can create online help for your M-files by entering text on one or more comment lines, beginning with the line immediately following the H1 line. When you type help function name, MATLAB displays the comment lines that appear between the function definition line and the first non-comment (executable or

blank) line. The help system ignores any comment lines that appear after this help block.

#### **2.6.1.4.5 FUNCTION BODY**

The function body contains all the MATLAB code that performs computations and assigns values to output arguments. The statements in the function body can consist of function calls, programming constructs like flow control and interactive input/output, calculations, assignments, comments, and blank lines.

#### **2.6.1.4.6 COMMENTS**

As mentioned earlier, comment lines begin with a percent sign (%). Comment lines can appear anywhere in an M-file, and you can append comments to the end of a line of code. The first comment line immediately following the function definition line is considered the H1 line for the function. The H1 line and any comment lines immediately following it constitute the online help entry for the file. In addition to comment lines, you can insert blank lines anywhere in an M-file.

Blank lines are ignored. However, a blank line can indicate the end of the help text entry for an M-file.

#### **2.6.1.4.7 FUNCTION NAMES**

MATLAB function names have the same constraints as variable names. MATLAB uses the first 31 characters of names. Function names must begin with a letter; the remaining characters can be any combination of letters, numbers, and underscores. Some operating systems may restrict function names to shorter lengths. The name of the text file that contains a MATLAB function consists of the function name with the extension `.m` appended.

If the filename and the function definition line name are different, the internal name is ignored. Thus, while the function name specified on the function definition line does not have to be the same as the filename.

#### **2.6.1.4.8 SUBFUNCTIONS**

Function M-files can contain code for more than one function. The first function in the file is the primary function, the function invoked with the M-file name. Additional functions within the file are Subfunctions that are only visible to the primary function or other Subfunctions in the same file.

Each subfunction begins with its own function definition line. The functions, immediately follow each other. The various Subfunctions can occur in any order, as long as the primary function appears first.

## CHAPTER THREE

### 3.0 MATERIALS AND METHODS

#### 3.1 MATERIALS

For the purpose of this project work the data collected for the programming are obtained from the Nigerian blast furnace at Ajaokuta Steel Complex. The auxiliary fuels used are:

|    |              |              |               |
|----|--------------|--------------|---------------|
| 1. | Natural gas  | 75% Carbon   | 25% Hydrogen  |
| 2. | Bunker C Oil | 86% Hydrogen | 14% Hydrogen  |
| 3. | Coal dust    | 79.2% Carbon | 5.4% Hydrogen |
|    |              | 12.4% Oxygen |               |

#### 3.2 MODEL FORMULATION

Model can be described to be a simplified representation of a certain aspect of a real system. Mathematical model is a representation of the essential part of an existing system (or a system to be constructed), which presents knowledge of that in a usable form and is created using mathematical concepts such as functions and equations.

The main aim of formulating models in this work is to provide a basis to; calculate the quantities of coke, injectants, and blast air require for the production of a given quantity of hot metal, and to predict their effects on the thermodynamics and kinetics of the system.

### 3.2.1 STOICHIOMETRIC DEVELOPMENT

The three basic elemental balance equations which the blast furnace must obey under a steady state conditions are;

$$n^1 \text{Fe} = n^0 \text{Fe} \dots\dots\dots (3.1)$$

$$n^1 \text{C} = n^0 \text{C} \dots\dots\dots (3.2)$$

$$n^1 \text{O} = n^0 \text{O} \dots\dots\dots (3.3)$$

$n^1$  and  $n^0$  are the number of moles of each component entering and leaving the furnace respectively.

$(\text{O/C})^{\#}$  = moles of  $\text{O}_2$  leaving the top gas per mole of carbon leaving the top gas.

$(\text{O/Fe})^x$  = moles of  $\text{O}_2$  entering in iron oxides per mole of Fe entering in iron oxide.

$(\text{C/Fe})^m$  = moles of C leaving in the molten metal per mole of product Fe.

$$X^{\#} \text{CO}_2 = (\text{O/C})^{\#} = -1 \dots\dots\dots (3.4)$$

$$X^{\#} \text{CO} = 2 - (\text{O/C})^{\#} \dots\dots\dots (3.5)$$

$X^{\#} \text{CO}_2$  and  $X^{\#} \text{CO}$  are the mole fractions of  $\text{CO}$  and  $\text{CO}_2$  in the top gas.

$(\text{O/Fe})^x$  - for hematite =  $\frac{3}{2}$

- for magnetite =  $\frac{3}{4}$

#### **Iron Balance;**

The only outlet for Fe is the molten metal, thus

$$n^1 \text{Fe} = n^0 \text{Fe} = 1 \dots\dots\dots (3.6)$$

### Carbon Balance;

Carbon leaves in the top gas and in the molten iron.

$$n^0C = n^eC + (O/Fe)^m \dots\dots\dots (3.7)$$

### Oxygen Balance;

Oxygen enters in the blast air and iron oxides, and leaves in the top gas.

$$n^1O = n^bO + (O/Fe)^x \dots\dots\dots (3.8)$$

$$n^0O = n^eO + (O/Fe)^y \dots\dots\dots (3.9)$$

Therefore,

$$n^bC + (O/Fe)^x = n^eC + (O/C)^y \dots\dots\dots (3.10)$$

$n^bO$  = moles of  $O_2$  through the blast air per kg mole product Fe.

$n^eC$  = moles of C leaving in the top gas as either  $CO_2$  or  $CO$ .

The actual carbon, which actually reacts in the reduction production is  $n^aC$ ; which ends up as either  $CO$  or  $CO_2$ .

Therefore,

$$n^aC = n^eC \dots\dots\dots (3.11)$$

Substitute eqn. (3.11) in eqn. (3.10)

$$n^bO + (O/Fe)^x = n^aC + (O/C)^y \dots\dots\dots (3.12)$$

If coke is the only source of carbon;  $n^iC = n^{coke}C$  and  $n^iC = n^0C$ .

From eqn. 3. 7 & 3.11,

$$n^{coke}C = n^eC + (O/Fe)^x \dots\dots\dots (3.13)$$

### 3.2.2 ENTHALPY BALANCE

Under steady state condition,

Enthalpy into the furnace = Enthalpy out of the furnace.

Thus,

$$n_{\text{Fe}_2\text{O}_3} \cdot H_{\text{Fe}_2\text{O}_3}^0 = H_{\text{Fe}_l}^0 + n_{\text{CO}}^{\text{E}} \cdot H_{\text{CO}}^0 + n_{\text{CO}_2}^{\text{E}} \cdot H_{\text{CO}_2}^0 \dots\dots\dots (3.14)$$

Rearranging to give a positive value,

$$n_{\text{Fe}_2\text{O}_3} (-H_{\text{Fe}_2\text{O}_3}^0) + H_{\text{Fe}_l}^0 = n_{\text{CO}}^{\text{E}} (-H_{\text{CO}}^0) + n_{\text{CO}_2}^{\text{E}} (H_{\text{CO}_2}^0) \dots\dots\dots (3.15)$$

Heat Supplied = Heat Demand

$$S = D$$

$$D = n_{\text{Fe}_2\text{O}_3} (-H_{\text{Fe}_2\text{O}_3}^0) + H_{\text{Fe}_l}^0$$

$$S = n_{\text{CO}}^{\text{E}} (-H_{\text{CO}}^0) + n_{\text{CO}_2}^{\text{E}} (H_{\text{CO}_2}^0)$$

Numerically, (from appendices IV & V)

$$H_{\text{Fe}_2\text{O}_3}^0 = H_{\text{Fe}_2\text{O}_3}^{\text{f}} = -826000 \text{ KJ}(\text{kg mole of Fe}_2\text{O}_3)^{-1}$$

$$H_{\text{CO}}^0 = H_{\text{CO}}^{\text{f}} = -111000 \text{ KJ}(\text{kg mole of CO})^{-1}$$

$$H_{\text{CO}_2}^0 = H_{\text{CO}_2}^{\text{f}} = -394000 \text{ KJ}(\text{kg mole of CO}_2)^{-1}$$

$$H_{\text{Fe}_l}^0 = (H_{\text{Fe}_l}^0 - H_{\text{Fe}_2\text{O}_3}^0) = -73000 \text{ KJ}(\text{kg mole of Fe})^{-1}$$



Eqn. 3.14 becomes

$$n\text{Fe}_2\text{O}_3 \cdot 826000 + 73000 = n^{\text{B}}\text{CO} \cdot 111000 + n^{\text{B}}\text{CO}_2 \cdot 394000 \dots\dots\dots (3.16)$$

One mole product Fe requires  $\frac{1}{2}$  mole input  $\text{Fe}_2\text{O}_3$ , thus,  $n\text{Fe}_2\text{O}_3 = \frac{1}{2}$

Substituting eqn.3. 4 &3.5 into eqn.3. 15

$$\frac{1}{2} 826000 + 73000 = n^{\text{A}}\text{C} \{ (2 - (\text{O/C})^{\text{B}} - 1) \cdot 394000 \} \dots\dots\dots (3.17)$$

$$\frac{1}{2} 826000 + 73000 = n^{\text{A}}\text{C} \{ 283000 \cdot (\text{O/C})^{\text{B}} - 172000 \} \dots\dots\dots (3.18)$$



Eqn. 18 can be rearranged to give

$$\frac{\text{D}}{283000} = n^{\text{A}}\text{C} (\text{O/C})^{\text{B}} - n^{\text{A}}\text{C} \cdot \frac{172000}{283000} \dots\dots\dots (3.19)$$

Subtract eqn. 3.19 from eqn. 3.12

$$n^{\text{B}}\text{O} + (\text{O/Fe})^{\text{x}} - \frac{\text{D}}{283000} = n^{\text{A}}\text{C} \frac{172000}{283000} \dots\dots\dots (3.20)$$

Eqn. 3.12 and 3.20 are the basis for the "Rist Diagram" (Rist 1977). The diagram can be used to obtain a graphical view of the efficiency of the furnace, and the effects of changes in operating parameters.

### 3.2.3 THE WUSTITE REDUCTION ZONE.

Eqn. 12 can be rewritten as

$$n^{\text{B}}\text{O} + (\text{O/Fe})^{\text{x Wtz}} = n^{\text{A}}\text{C} (\text{O/C})^{\text{B Wtz}} \dots\dots\dots (3.21)$$

wrz = wustite reduction zone.

The only iron-bearing material in this zone is  $\text{Fe}_{0.947}\text{O}$ .

$$(\text{O}/\text{Fe})^{\text{wrtz}} = 1.056$$



According to Stull (1970), at 1200K, the equilibrium composition is

$$X_{\text{CO}} = 0.694 \approx 0.7$$

$$X_{\text{CO}_2} = 0.306 \approx 0.3$$

Therefore,

$$(\text{O}/\text{Fe})^{\text{wrtz}} = 1.3$$

Substitution these numerical values into eqn. 3.20,

$$N^{\text{B}}\text{O} + 1.06 = 1.3 \cdot N^{\text{A}}\text{C} \dots\dots\dots (3.22)$$

The enthalpy eqn. for the Wustite reduction zone can be summarises as,

$$\begin{aligned} 1.06 \cdot H_{\text{Fe}_{0.947}\text{O}}^0 + \{n^{\text{A}}\text{C} + (\text{O}/\text{Fe})^{\text{m}}\} \cdot H_{\text{C}}^0 + n^{\text{B}}\text{O} \cdot \left( \frac{1}{2} H_{\text{O}_2}^0 \text{TB} + \frac{0.79}{0.21} + \frac{1}{2} H_{\text{N}_2}^0 \text{TB} \right) = \\ H_{\text{Fe}_1}^0 + (\text{C}/\text{Fe})^{\text{m}} \cdot H_{(\text{C})}^0 + n^{\text{A}}\text{C} \{ (2 - (\text{O}/\text{C})^{\text{wrtz}}) \cdot H_{\text{CO}}^0 + \{ (\text{O}/\text{Fe})^{\text{wrtz}} - 1 \} \cdot H_{\text{CO}_2}^0 \} \\ + n^{\text{B}}\text{O} \cdot \frac{0.79}{0.21} \cdot \frac{1}{2} \cdot H_{\text{N}_2}^0 \dots\dots\dots (3.23) \end{aligned}$$

upon simplification, eqn 3. 23 becomes

$$\begin{aligned} D^{\text{wrtz}} = S^{\text{wrtz}} \\ = n^{\text{A}}\text{C} \{ (2 - (\text{O}/\text{C})^{\text{wrtz}}) \cdot H_{\text{CO}}^f + \{ (\text{O}/\text{Fe})^{\text{wrtz}} - 1 \} \cdot H_{\text{CO}_2}^f \} \\ + E^{\text{B}} \cdot E_{\text{O}_2}^{\text{B}} \cdot \frac{1}{2} \cdot H_{\text{O}_2}^0 \{ n^{\text{A}}\text{C} \cdot (\text{O}/\text{C})^{\text{wrtz}} - n^{\text{B}}\text{O} - 1.06 \} \dots\dots\dots (3.24) \end{aligned}$$

$$E^B = \left( \frac{1}{2} H_{O_2}^0 T_B - \frac{1}{2} H_{O_2}^0 \right) + \frac{0.79}{0.21} \cdot \left( \frac{1}{2} H_{N_2}^0 T_B - H_{N_2}^0 \right) \dots \dots \dots (3.25)$$

$T_B$  = blast temperature

$E^B$  = blast Enthalpy

Numerically

$$H_{CO}^f = -113000 \text{ KJ(kg mole of CO)}^{-1}$$

$$H_{CO_2}^f = -395000 \text{ KJ(kg mole of CO}_2\text{)}^{-1}$$

$$(O/C)^{gwtz} = 1.3$$

eqn. 3.24 becomes

$$\begin{aligned} D^{wtz} &= S^{wtz} \\ &= n^A C (198000) + E^B \cdot n^B O - \frac{1}{2} H_{O_2}^0 (1.3 n^A C - n^B O - 1.06) \dots \dots \dots (3.26) \end{aligned}$$

The last term of eqn.3. 26 is always zero, therefore eqn. 26 becomes.

$$\begin{aligned} D^{wtz} &= S^{wtz} \\ &= n^A C \cdot 198000 + E^B \cdot n^B O \dots \dots \dots (3.27) \end{aligned}$$

Recall eqn. 3.22,

$$n^B O + 1.06 = 1.3 n^A C$$

$$n^B O = 1.3 n^A C - 1.06$$

Substituting into eqn. 3.27

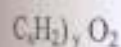
$$D^{WTZ} = S^{WTZ}$$

$$= n^A C (198000) + E^B (1.3 n^A C - 1.06)$$

$$= n^A C (198000 + 1.3 E^B) - 1.06 \dots\dots\dots (3.28)$$

### 3.2.4 TUYERE INJECTION EFFECT

Injectant is generally represented as



$N^I$  is termed the mole of injectant per mole of product Fe.

Stoichiometrically, the elements present in injectants are;

Carbon:  $xN^I$  (mole of C per mole of product Fe)

Hydrogen:  $yN^I$  (mole of  $H_2$  per mole of product Fe)

Oxygen:  $zN^I$  (mole of O per mole of product Fe)

*Carbon balance;*

This is altered as

$$n^I C = n^{coke} C + N^I$$

$$n^I C = n^A C + (C/Fe)^m$$

Therefore

$$n^I C + n^{coke} C + xN^I - (C/Fe)^m \dots\dots\dots (3.29)$$

*Oxygen Balance;*

$$n^I O = n^B O + (O/Fe)^x + zN^I \dots\dots\dots (3.30)$$

$$n^I O = u^B CO + 2u^E CO_2 + w^B H_2O \dots\dots\dots (3.31)$$

The Stoichiometric equation is given as

$$n^B C + (O/Fe)^{w_{wz}} + z N^I = n^A C (X^{g_{wz}} CO + 2X^{g_{wz}} CO_2) + y.N^I X^{g_{wz}} H_2O \dots\dots\dots(3.32)$$

where  $(O/Fe)^{w_{wz}} = 1.06$

$$X^{g_{wz}} CO = 0.7$$

$$X^{g_{wz}} CO_2 = 0.3$$

The value of  $XH_2^{g_{wz}}$  and  $XH_2O^{g_{wz}}$  are;

$$XH_2^{g_{wz}} = 0.62$$

$$XH_2O^{g_{wz}} = 0.38$$

Inserting these values into eqn 3.32.

$$n^B O + z N^I + 1.06 = n^A C (1.3) + y.N^I (0.38) \dots\dots\dots(3.33)$$

In the Enthalpy form,

$$D^{wz} = S^{wz}$$

Recall eqn 3.27

$$= n^A C (198000) + E^B n^B O$$

The total heat demand is altered as

$$\text{heat demand} = D^{wz} + N^I D^I$$

$D^I$  = injectant heat demand, KJ (kg mole of injectant)<sup>-1</sup> from eqn. 3.33 the heat demand can be simplified as

$$D^{wrx} + N^I D^I = S^{wrx}$$

$$= n^A C (0.7 H_{1200}^{f_{CO}} + 0.3 H_{1200}^{f_{CO_2}}) - 0.38 \cdot y \cdot N^I H_{1200}^{f_{H_2O}} + E^B \cdot n^B O \dots\dots\dots (3.34)$$

$$H_{1200}^{f_{CO}} = -113000 \text{ KJ(kg mole of gas)}^{-1}$$

$$H_{1200}^{f_{CO_2}} = -395000 \text{ KJ(kg mole of gas)}^{-1}$$

$$H_{1200}^{f_{H_2O}} = -249000 \text{ KJ(kg mole of gas)}^{-1}$$

Substitute into eqn. (3.34)

$$D^{wrx} + N^I D^I = S^{wrx}$$

$$= n^A C (0.7(-113000) + 0.3(-395000)) - 0.38(-249000 + y \cdot N^I + E^B \cdot n^B O$$

$$D^{wrx} + N^I D^I = n^A C (198000) + y \cdot N^I (95000) + E^B \cdot n^B O \dots\dots\dots (3.35)$$

$D^I$  is given as

$$D_T^I = -H_T^f + x (H_{1200}^0 - H_T^0)_C + y (H_{1200}^0 - H_T^0)_{H_2} + Z$$

$$+ \frac{1}{2} (H_{1200}^0 - H_T^0)_{O_2} \dots\dots\dots (3.36)$$



$T$  = injection temperature.

$D^{wrx}$  is the sum of the heat demand of the elements in the furnace. Therefore;

$$D^{wrx} = D^{fc} + (C/Fe)^m \cdot D^c + D^{loss} + (Si/Fe)^m \cdot D^{si} + (Mn/Fe)^m \cdot D^{mn} + (P/Fe)^m \cdot D^p + Wt_{slag} \cdot D^{slag} + nCaCO_3 \cdot D^{caco3} \dots\dots\dots (3.37)$$

$D^{si}$ ,  $D^{fc}$ ,  $D^c$ ,  $D^{mn}$ ,  $D^p$ ,  $D^{slag}$ ,  $D^{caco3}$  are the heat demand of such element and product.

The calculated values of the heat demands are given as (Peacey 1979).

$$D^{Si} = 873000 \text{ KJ}(\text{kg mole of dissolved Si})^{-1}$$

$$D^{Mn} = 435000 \text{ KJ}(\text{kg mole of dissolved Mn})^{-1}$$

$$D^C = 44000 \text{ KJ}(\text{kg mole of dissolved C})^{-1}$$

$$D^{Fe} = 319000 \text{ KJ}(\text{kg mole of dissolved Fe})^{-1}$$

$$D^{CaCO_3} = 561000 \text{ KJ}(\text{kg mole of dissolved CaCO}_3)^{-1}$$

$(C/Fe)^m$ ,  $(Si/Fe)^m$ ,  $(Mn/Fe)^m$ ,  $(P/Fe)^m$ , are the moles of such element per mole of product Fe. They are specified from data collected about a particular furnace.

The slag heat demand is calculated from the data given by (Foerster 1967) to be,

$$D^{slag} = 250 \text{ KJ}(\text{kg of Slag})^{-1}$$

According to Peacey 1979,  $D^{loss}$  is given to be,

$$D^{loss} = 6.4 \times 10^6 \text{ m}^{-1} \text{ hr}^{-1} \times \text{hearth diameter (m)}$$

$$\frac{\text{Pig iron Production rate (Kg hr}^{-1}\text{)}}{55.85} \times \frac{\%Fe \text{ in Pig Iron}}{100}$$

When using injectants with known weight percentages of its composition and known

Heat of combustion,

Equation 3.12 becomes,

$$n_O^B = n_C^{cokc} + 1 + \frac{0}{100} \cdot W^I - (C/Fe)m \dots \dots \dots 3.39$$

$$W^I = \text{injectant}$$

Equation 3.22 also becomes,

$$n^B_O + 1 \cdot B \cdot W^I + 1.06 = 1.3 \cdot n^A_c + 0.38 \cdot \frac{1}{2} \cdot \frac{\lambda}{100} \cdot W^I \dots\dots\dots 3.40$$

likewise equation 3.35 becomes

$$D^{wtz} + W^I \cdot D^I W \cdot n^A_c \cdot (198000) + \frac{1}{2} \cdot \frac{\lambda}{100} \cdot W^I \cdot (95000) + E^B \cdot n^B_O \dots\dots\dots (3.41)$$

The injectant heat demand  $D^I w$  is given as;

$$\begin{aligned} D^I w = & \left[ H^c_w - \frac{1}{12} \cdot \frac{0}{100} \cdot H^f_{298} - \frac{1}{2} \cdot \frac{\lambda}{100} \cdot H^f_{298} \right]_{CO_2} \\ & + \frac{1}{12} \cdot \frac{0}{100} \cdot [H^0_{1200} - H^0_{298}]_c + \frac{1}{12} \cdot \frac{\lambda}{100} \cdot [H^0_{1200} - H^0_{298}]_{H_2} \\ & + \left[ \frac{1}{28} \cdot \frac{0}{100} \right] \cdot \frac{1}{2} [H^0_{1200} - H^0_{298}]_{N_2} \dots\dots\dots (3.42) \end{aligned}$$

$H^c_w$  is the heat of combustion of the injectant, given as;

$$H^c_w - \frac{1}{2} \cdot \frac{0}{100} \cdot H^f_{298} - \frac{1}{2} \cdot \frac{\lambda}{100} \cdot H^f_{298} - H^f_w \dots\dots\dots (3.43)$$

–  $H^f_w$  is the of dissociation of the injectant

$\Theta$  = wt % C                       $\varphi$  = wt % N

$\lambda$  = wt % H                       $\beta$  = wt % O

### 3.3 THE DATA PROPOSED FOR THE FURNACE ;

#### TABLE 2.1 CHARGE MATERIAL

| DESCRIPTION                    | UNIT | VALUE |
|--------------------------------|------|-------|
| <u>Sinter Analysis</u>         |      |       |
| Fe (Total)S                    | %    | 52.70 |
| Fe <sub>2</sub> O <sub>3</sub> | %    | 60.29 |
| Fe <sub>2</sub>                | %    | 13.55 |
| Mn                             | %    | 1.03  |
| P                              | %    | 0.036 |
| S                              | %    | 0.011 |
| MnO                            | %    | 1.33  |
| SiO <sub>2</sub>               | %    | 9.03  |
| Al <sub>2</sub> O <sub>3</sub> | %    | 1.00  |
| CaO                            | %    | 12.09 |
| MgO                            | %    | 2.12  |
| TiO <sub>2</sub>               | %    | 0.05  |
| P <sub>2</sub> O <sub>5</sub>  | %    | 0.026 |
| <u>Coke Analysis</u>           |      |       |
| Ash                            | %    | 13.0  |
| Sulphur                        | %    | 1.2   |
| Volatiles                      | %    | 2.0   |
| Humidity                       | %    | 1.0   |
| Carbon                         | %    | 83.8  |
| <u>Organic Mass of Coke</u>    |      |       |
| N <sub>2</sub>                 | %    | 0.33  |
| H <sub>2</sub>                 | %    | 0.25  |
| O <sub>2</sub>                 | %    | 0.25  |
| C                              | %    | 86.21 |
| H <sub>2</sub> O               | %    | 2.7   |

**TABLE 2.2 FURNACE PRODUCT**

| DESCRIPTION                    | UNIT | VALUE |
|--------------------------------|------|-------|
| <u>Hot Metal Analysis</u>      |      |       |
| Si                             | %    | 0.8   |
| Mn                             | %    | 1.1   |
| S                              | %    | 0.025 |
| P                              | %    | 0.067 |
| C                              | %    | 4.4   |
| <u>Slag Analysis</u>           |      |       |
| SiO <sub>2</sub>               | %    | 28.59 |
| Al <sub>2</sub> O <sub>3</sub> | %    | 6.07  |
| TiO <sub>2</sub>               | %    | 0.19  |
| CaO                            | %    | 44.10 |
| MgO                            | %    | 8.0   |
| MnO                            | %    | 1.94  |
| FeO                            | %    | 0.25  |
| Alkalies                       | %    | 0.25  |
| S                              | %    | 0.50  |
| <u>B/f Gas Analysis</u>        |      |       |
| CO                             | %    | 29.08 |
| CO <sub>2</sub>                | %    | 17.68 |
| H <sub>2</sub>                 | %    | 11.26 |
| N <sub>2</sub>                 | %    | 41.98 |

**TABLE 2.3 DIMENSION OF THE FURNACE**

| PARAMETER                            |              | UNIT           | VALUE |
|--------------------------------------|--------------|----------------|-------|
| Diameter                             | Hearth       | Mm             | 9750  |
|                                      | Belly        | Mm             | 10900 |
|                                      | Top          | Mm             | 7300  |
|                                      | Large bell   | Mm             | 5400  |
| Height                               | Hearth       | Mm             | 4300  |
|                                      | Bosh         | Mm             | 3000  |
|                                      | Belly        | Mm             | 1700  |
|                                      | Stack        | Mm             | 18200 |
|                                      | Top          | Mm             | 2900  |
|                                      | "Dead Space" | Mm             | 1103  |
| Distance from slag notch centre-line |              | Mm             | 1800  |
| Effective height of furnace          |              | Mm             | 30100 |
| Hearth Area                          |              | m <sup>2</sup> | 74.67 |

**TABLE 2.4 CONSUMPTION AND OUTPUT**

| DESCRIPTION                                      | UNIT            | VALUE |
|--------------------------------------------------|-----------------|-------|
| Natural gas consumption                          | N.m/ton of Fe   | 115   |
| Skip coke consumption                            | Kg/ton of Fe    | 475   |
| Consumption of gas for blast heating:            |                 |       |
| Blast furnace gas                                | N.m/ton of Fe   | 400   |
| Natural gas                                      | N.m/ton of Fe   | 10    |
| Dry top gas recovery                             | N.m/ton of Fe   | 1660  |
| Oxygen enrichment                                | %               | 30    |
| Flue dust yield                                  | Kg/ton of Fe    | 15    |
| Output of furnace:                               |                 |       |
| Daily output                                     | Tons/day        | 3860  |
| Annual output                                    | Thou. Tons/year | 1350  |
| Slag basicity:                                   |                 |       |
| In term of $\text{CaO}/\text{SiO}_2$ ratio       | Unit            | 1.14  |
| In term of $\frac{\text{CaO}}{\text{MgO}}$ ratio | Unit            | 1.17  |
| $\text{Al}_2\text{O}_3 + \text{SiO}_2$           |                 |       |
| Relative weight of slag                          | Kg/ton of fe    | 500   |

### 3.4 OPTIMIZATION METHOD

The objective of the optimization is to minimize the total cost of fuel required for producing a given quantity of liquid iron.

This objective function i.e. the cost equation is given as;

$$\text{Total fuel cost (₦)} = \frac{\text{Cost (₦) of coke}}{\text{Per kg of product Fe}} + \frac{\text{Cost (₦) of injectant}}{\text{per kg of product Fe}}$$

This can also be written as:

$$\text{Total Cost (₦)} = n^{\text{coke}} C (\text{₦}) + N^I (\text{₦})$$

This objective function is evaluated by the linearly related operating equations (eqn. 3.29, 3.33, 3.35, 3.39, 3.40, 3.41), which describe the process.

### 3.5 CONSTRAINTS

The constraints entered into the program are:

1. Those provided by the physical requirement of the furnace. According to Peacey and Davenport (1978), the amount of coke that must be left inside the furnace for proper burden support must not be less than 320kg (100%C). In the model form,

$$n_c \geq 1.5$$

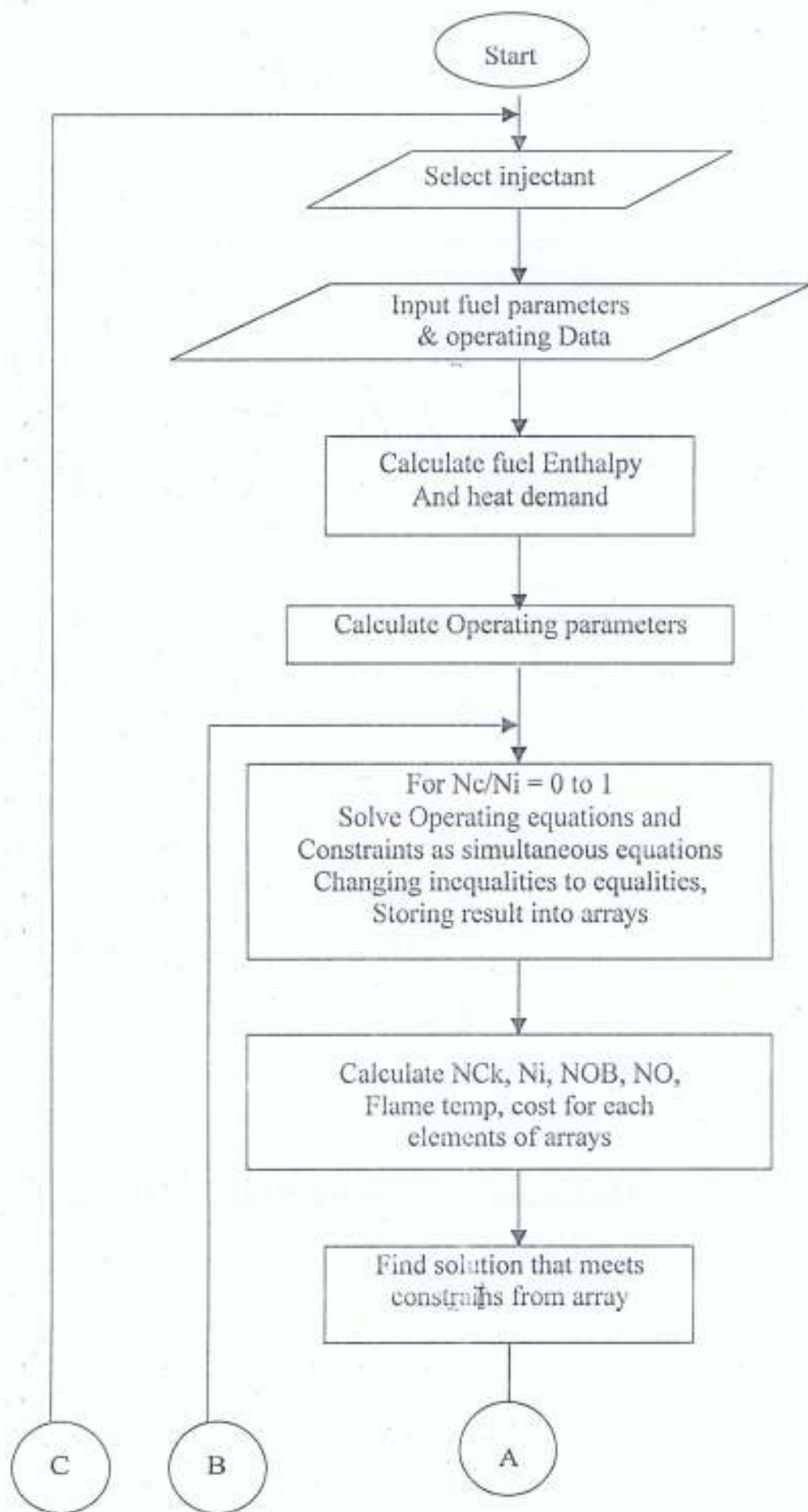
2. The thermal requirements of the process. According to Tovarovskii et al (1980) the flame temperature must be between 2200k and 2600k.

$$2200\text{k} \leq T_f \leq 2600\text{k}.$$

### 3.6 THE PROGRAM

The operating equation, constrains, fuel parameters, and the furnace operating data are input into the linear optimization computer program

The coke/injectant ratio is varied. The operating equations and constrains were solved as simultaneous equations changing inequalities to equalities. The results were stored into arrays. The algorithm is as shown.



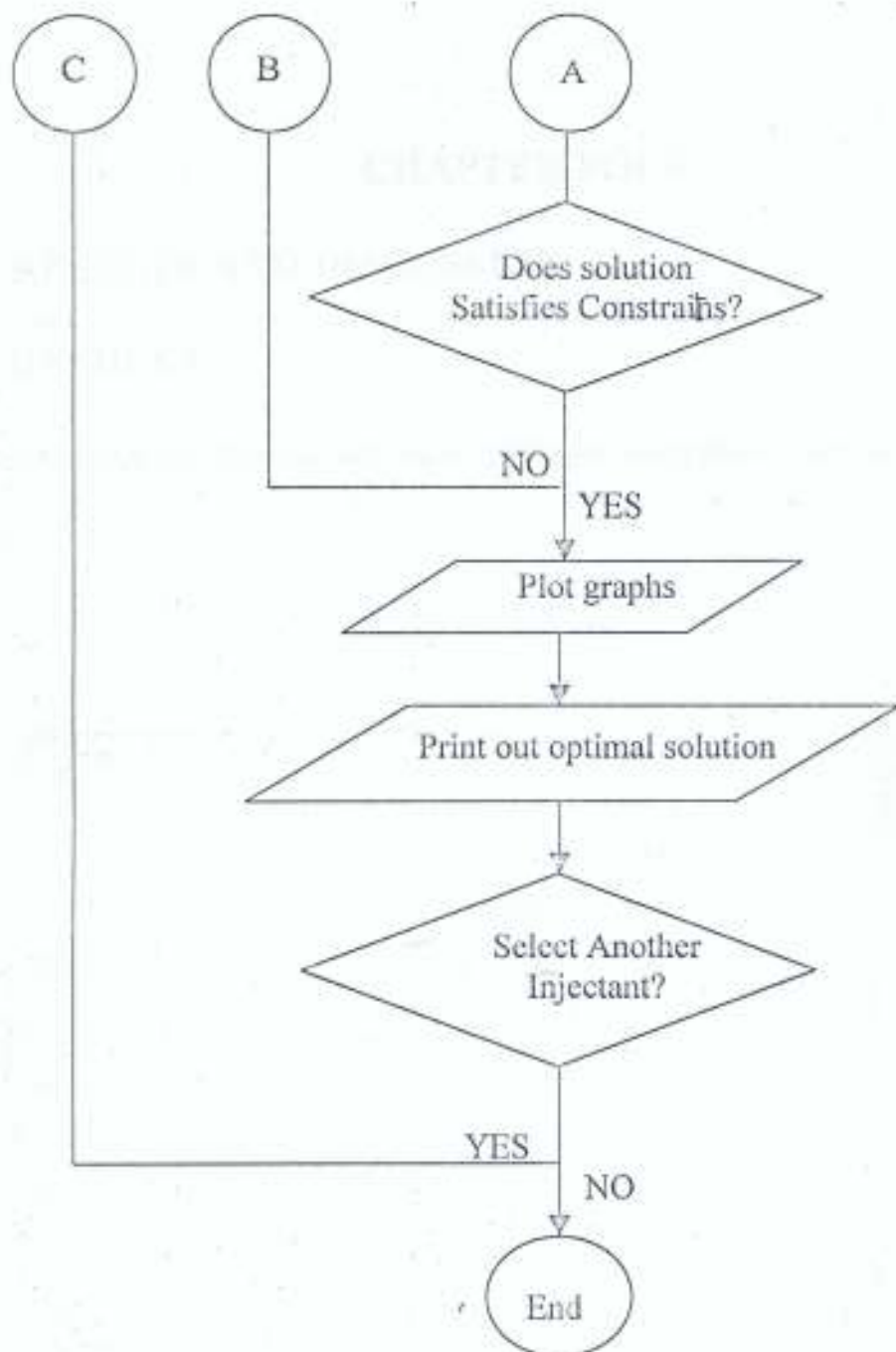


FIG.3: THE ALGORITHM FOR THE PROGRAM

## CHAPTER FOUR

### 4.0 RESULTS AND DISCUSSION

#### 4.1 RESULTS

The results obtained after running the program are in appendix 2, and as shown in Figures 6 to 16.

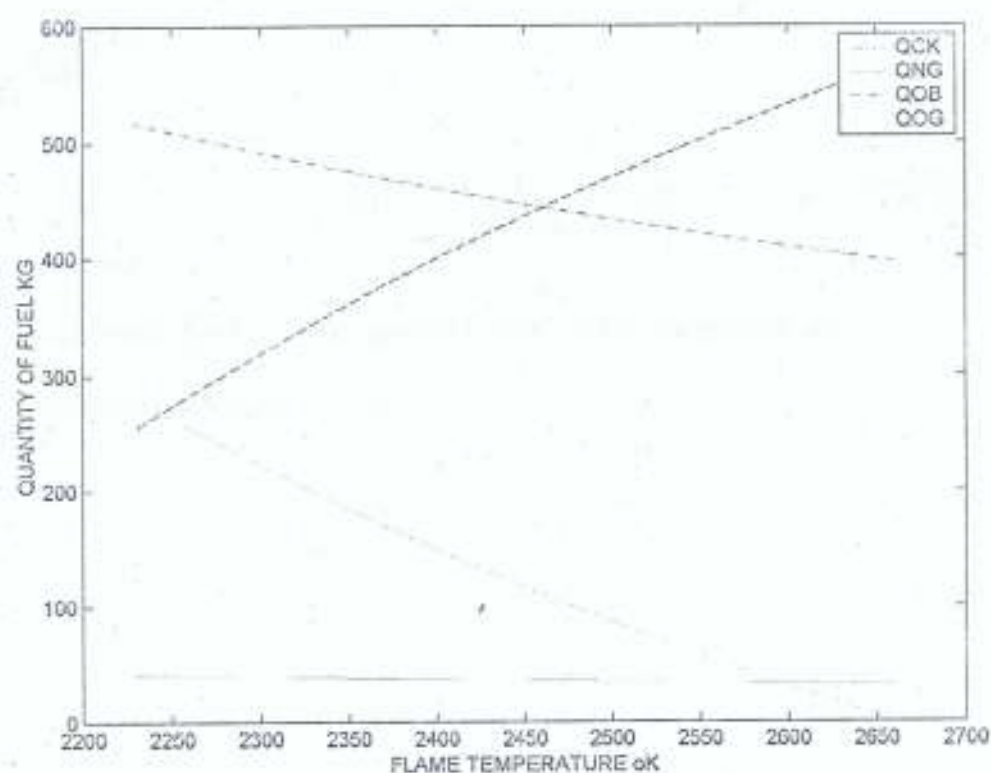


Fig 6: Plot of total Quantity of fuel against flame temperature at blast temperature of 1200k for natural gas injection.

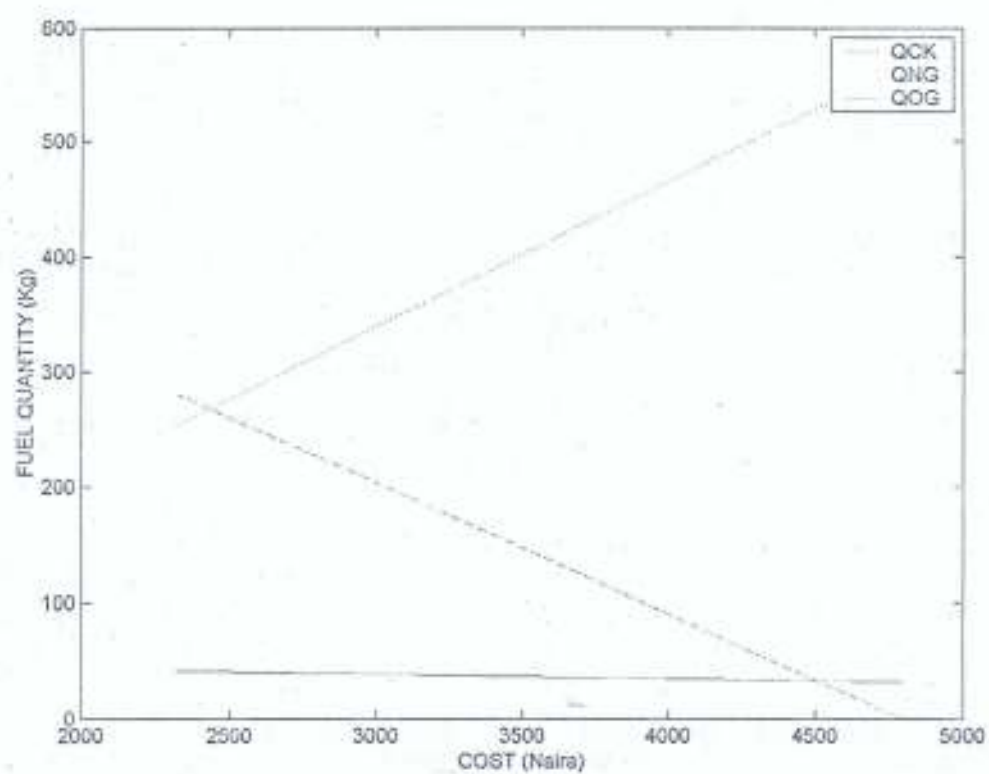


Fig 7: Plot of total Quantity of fuel against cost at a Blast temperature of 1200k for natural gas injection.

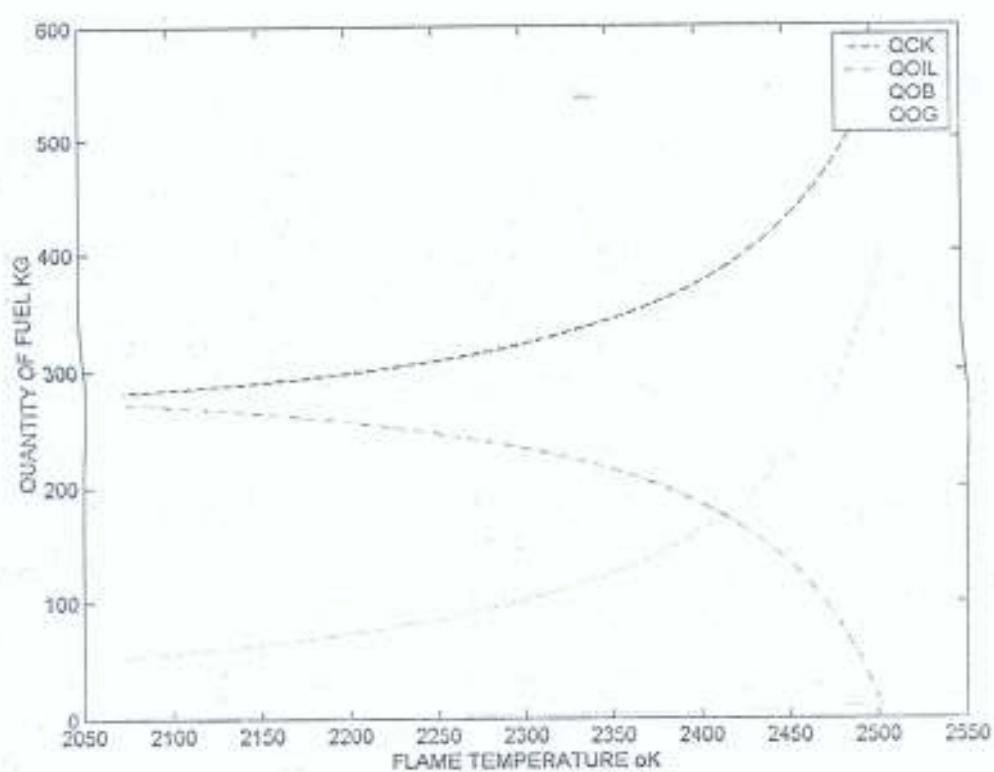


Fig 8: Plot of total Quantity of fuel against flame temperature at blast temperature of 1200k for oil injection.

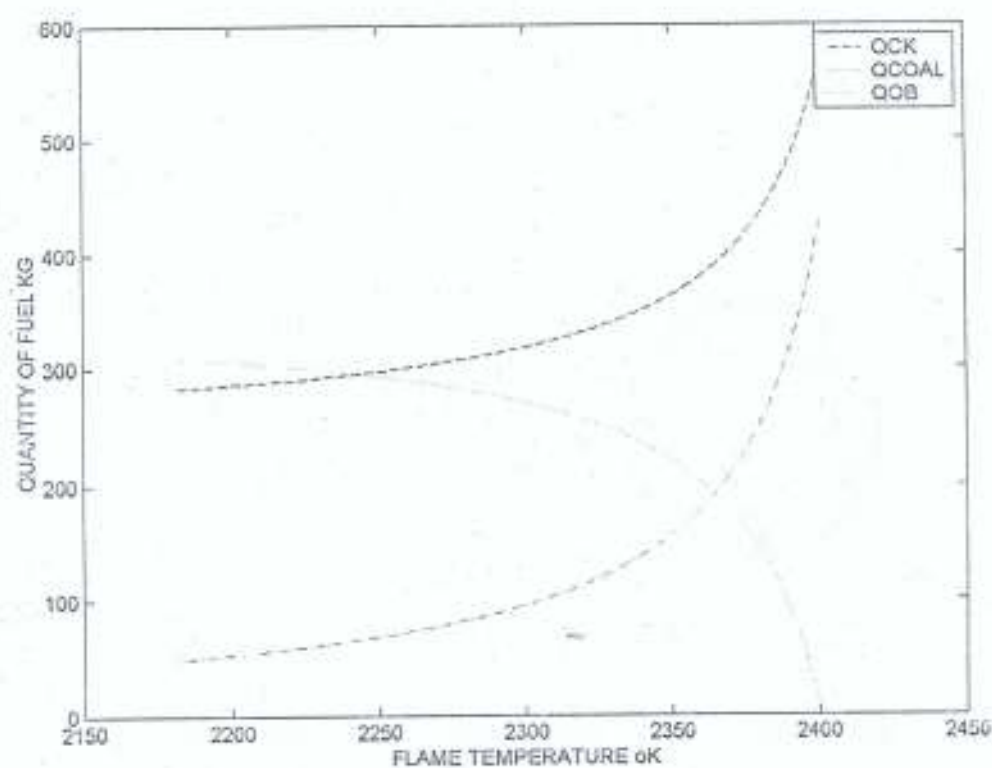


Fig 9: Plot of total Quantity of fuel against flame temperature at blast temperature of 1200k coal injection.

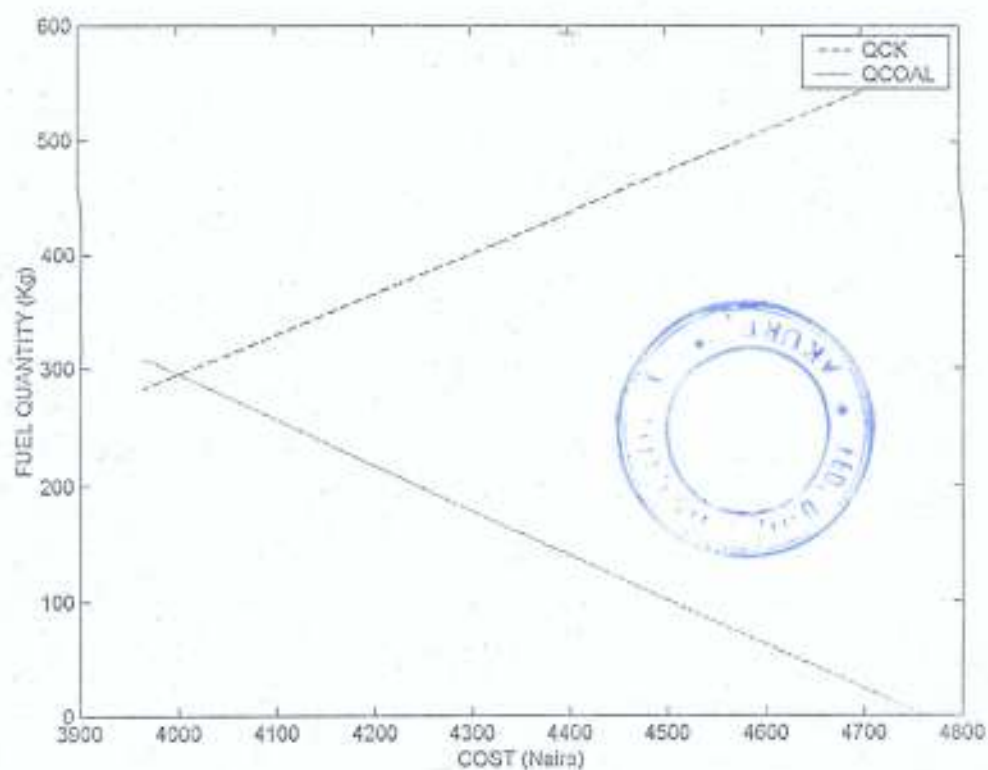


Fig 10: Plot of total Quantity of fuel against cost temperature at blast temperature of 1200k coal injection.

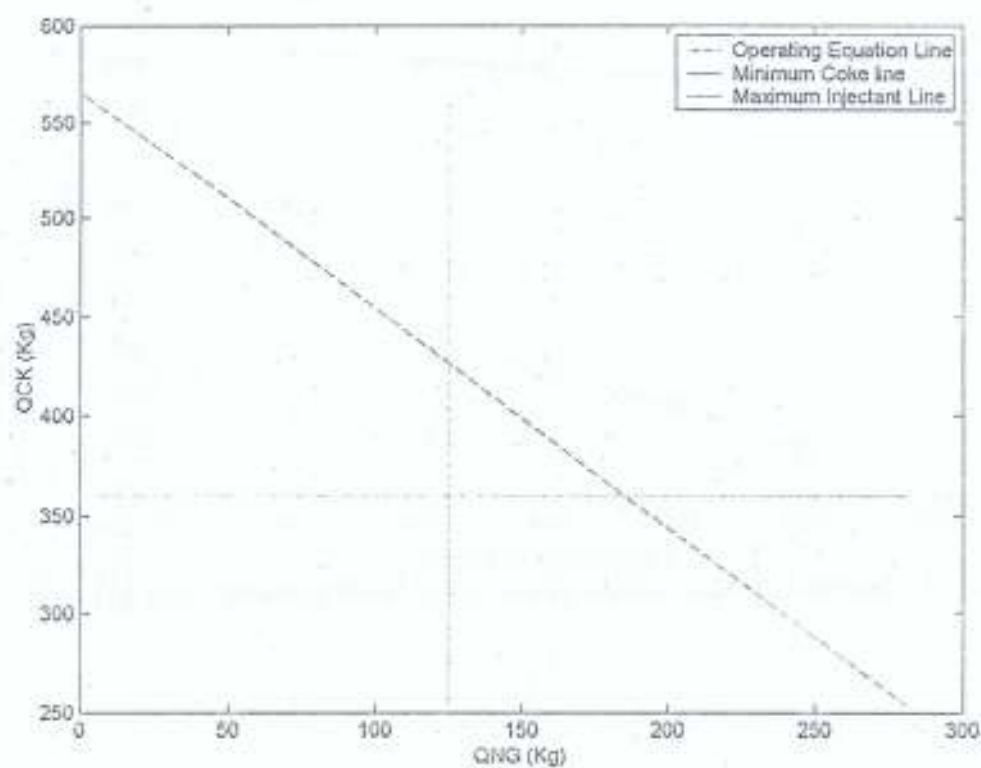


Fig 11: Optimisation graph for natural gas injection at blast temperature of 1200k

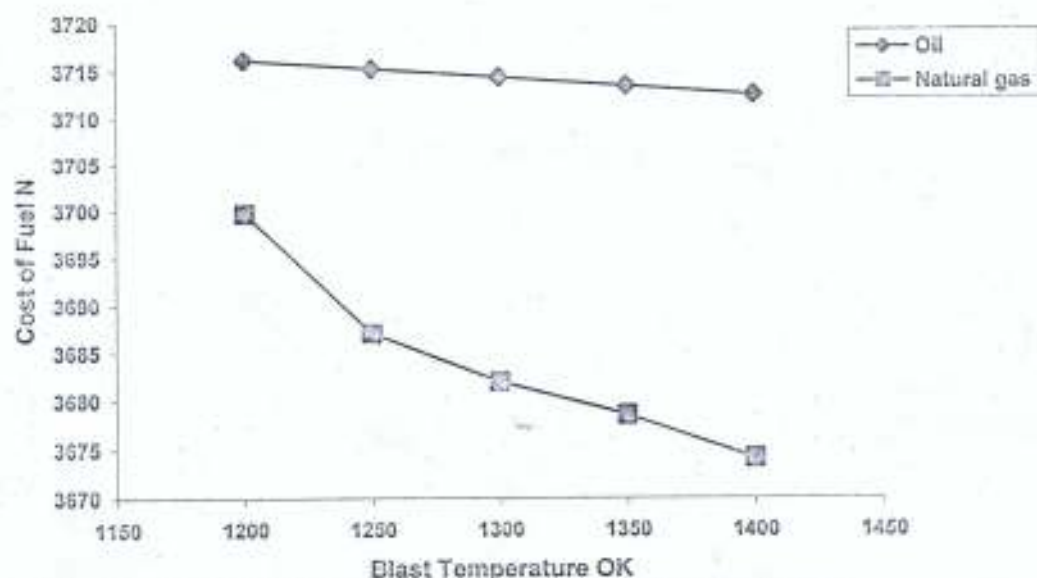


Fig 12: Effect of Blast temperature on the total cost of fuel

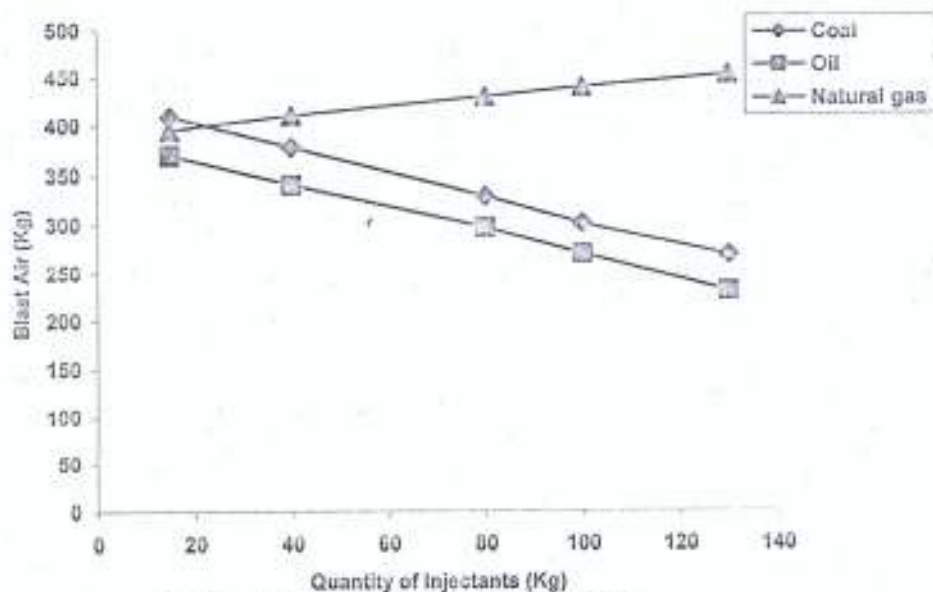


Fig 13: Effect of injectant on Blast air

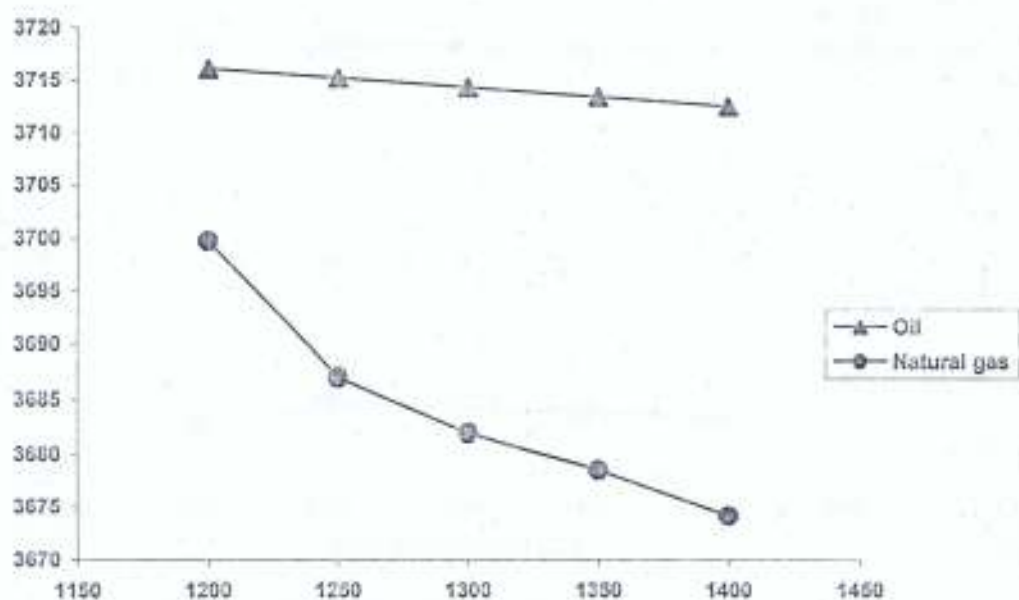


Fig 14: Effect of Blast temperature on the total cost of fuel

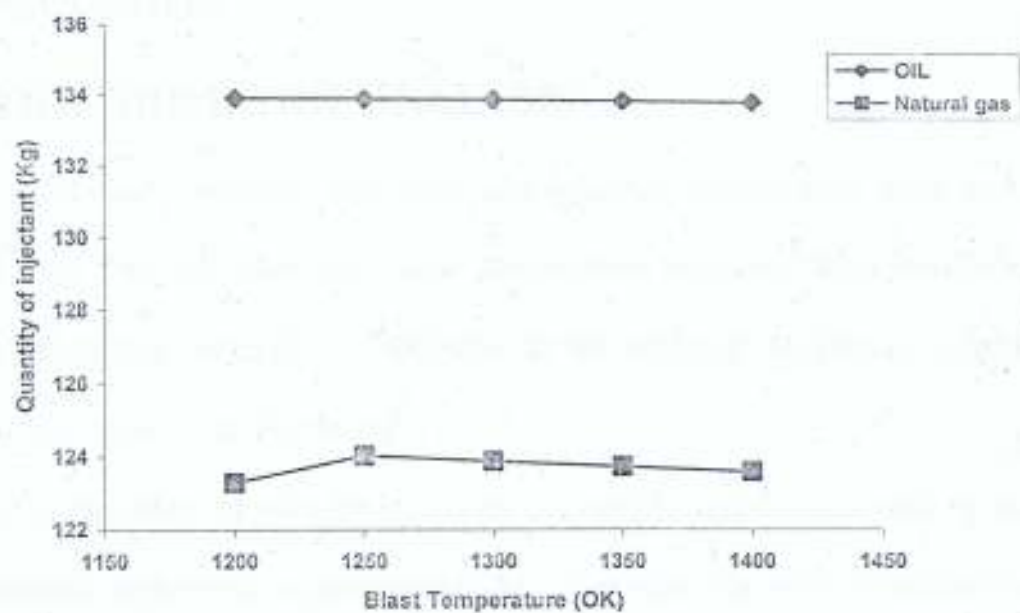


Fig 15: Effect of Blast temperature on injectant

## 4.2 DISCUSSION

### 4.2.1 STOICHIOMETRIC ANALYSIS

It is generally observed that coke and injectant consumption have an inverse relationship as both the blast and flame temperature increases; thus confirming that injectants substitutes coke. This is attributed to the reducing components (carbon and hydrogen) contained in the injectants.

The replacement of coke by injectants (the weight replacement ratio of coke per kg of injectants) varies with temperature and injectant type. The coke replacement ratio is made up of two components; coke saving from the decrease in the degree of direct reduction, and lowering (rise) of coke consumption because of the change in the amount of heat introduced into the furnace and carried out. Hence replacement ratio increases with rise in blast temperature. The replacement ratio of coke by heavy oil with increasing heaving oil consumption falls less significantly than with increasing natural gas consumption.

The blast air required for the various injectants varies. Table 6, Fig 6, 8, 9, 13 and Appendix II. It is observed that Natural gas injection has the highest requirement. This higher blast requirements and Oxygen enrichment of natural gas injection compared with Coal and Oil can be attributed to lack of Oxygen content as in Coal and Oil. As a result, blast requirement to burn unit quantity of natural gas and subsequently the yield of tuyere gas is higher for Natural gas.

#### 4.2.2 THERMAL ANALYSIS

Changing blast temperature affects the flame temperature and heat loss in production zone. Flame temperature increases with increase in blast temperature and so also is heat loss in production zone. The flame temperature is also observed to fall as the amount of injectant increases and rises as the quantity of coke consumed increase. Table 3, 5, Fig 6, 8, 9, and Appendix II.

As fuel is injected, in effect hydrogen replaces Nitrogen in the tuyere gas. As hydrogen reduction replaces the solution loss reaction, the thermal requirements to make a tonne of iron decrease markedly. The endothermic reaction of injectant combustion maintains a thermal balance unaltered, the blast temperature is either increased, or oxygen enrichment increased.

The oxygen enrichment reduces the heat loss in production zone and reduces the nitrogen contents of top gas. The reduction in heat loss in production zone with increase in flame temperature is connected with decreases in  $N_2$  content of the gas leaving production zone.  $N_2$  has been decreased due to increase in  $O_2$ . This establishes  $N_2$  as the main heat transporters in the furnace. Top gas temperature also goes down reduction in  $N_2$

The enrichment of the blast with oxygen raises the flame temperature in the tuyere zone thus permit some injectants to be added while still maintaining an acceptable hearth

temperature. This enriched oxygen combust the incandescent coke and injectant to CO, producing heat for melting and CO for reduction.

Reducing the coke rate leads to reduction in flame temperature, blast consumption and slag volume and therefore increase in production rate but also a situation of thermal imbalance may arise.

### 4.2.3 COST ANALYSIS

In trying to assess the technological aspect of the use of fuel addition and Oxygen enrichment of the blast, the main criterion in assessing the promise of any auxiliary fuel injection in the final reckoning is the overall economic effectiveness.

The maximum economic effectiveness is therefore achieved at the optimum ratio of consumptions of fuel additions and Oxygen.

The results clearly show that at higher alternative fuel injection rate, the cost reduces. Table 3, 4, 5, Fig 7, 10, 14 and Appendix II. This confirms the main basis for which cheaper fuel is injected. There is just a little reduction in cost as the blast temperature increases at constant coke/injectant consumption rate. On the other hand, the cost reduction is obvious at constant blast temperature varying the coke/injectant consumption rate.

The furnace was designed to be operated at a coke rate of 475kg/Thm and natural gas rate of 81kg (115m<sup>3</sup>)/Thm, amounting to ₦4,099.87 for the production of a tonne of

hot pig iron which cost ₦11,135.00. Operating the furnace according to the programme, as much as ₦399.9 can be saved in every tonne of Fe produced.

**Table 3: Effect of injectant on Blast Furnace Performance**

| Parameters                       | Unit   | BLAST TEMPERATURE |         |         |         |         |
|----------------------------------|--------|-------------------|---------|---------|---------|---------|
|                                  |        | 1200k             | 1250k   | 1300k   | 1350k   | 1400k   |
| Coke rate                        | Kg/Thm | 428.46            | 426.96  | 426.45  | 425.94  | 425.43  |
| Natural gas rate                 | Kg/Thm | 124.28            | 124.03  | 123.88  | 123.73  | 123.58  |
| Oxygen rate                      | Kg/Thm | 35.93             | 35.87   | 35.79   | 35.71   | 35.64   |
| Total fuel rate                  | Kg/Thm | 368.67            | 366.86  | 366.12  | 365.38  | 364.65  |
| Blast air                        | Kg/Thm | 448.97            | 448.39  | 447.43  | 446.47  | 445.52  |
| Cost of coke                     | ₦/Thm  | 3607.70           | 3595.02 | 3590.72 | 3586.43 | 3582.19 |
| Cost of natural gas              | ₦/Thm  | 44.73             | 44.63   | 44.59   | 44.54   | 44.49   |
| Cost of oxygen                   | ₦/Thm  | 28.73             | 28.69   | 28.63   | 28.57   | 28.51   |
| Total fuel cost                  | ₦/Thm  | 3672.79           | 3660.38 | 3655.98 | 3651.00 | 3647.23 |
| Flame temp.                      | °K     | 2439              | 2478    | 2518    | 2558    | 2588    |
| Carbon from coke consumed        | Kg/Tfe | 355.62            | 354.37  | 353.95  | 353.53  | 353.1   |
| Carbon from natural gas consumed | Kg/Tfe | 93.21             | 93.02   | 92.91   | 92.79   | 92.68   |
| Total carbon consumed            | Kg/Tfe | 448.83            | 447.39  | 446.86  | 446.32  | 445.78  |

**Table 4: Optimum Cost Analysis And Comparism of Natural Gas Injection**

| Variant                                    | Quantity of coke consumed Kg/Thm | Quantity of natural gas consumed Kg/Thm | Quantity of oxygen consumed Kg/Thm | Cost (₦) | Cost difference compared to the Optimum Value |             |               |
|--------------------------------------------|----------------------------------|-----------------------------------------|------------------------------------|----------|-----------------------------------------------|-------------|---------------|
|                                            |                                  |                                         |                                    |          | Per tonne (₦)                                 | Per day (₦) | Per year (₦)  |
| High blast Temp.                           | 565.15                           | -                                       | -                                  | 4758.89  | 1086.09                                       | 4,192,307.4 | 1,530,192.201 |
| High blast Temp + O <sub>2</sub> injection | 560.08                           | -                                       | 31.08                              | 4740.23  | 1067.43                                       | 4,120,279.3 | 1,503,902,127 |
| Designed rate                              | 475.50                           | 81                                      | 30                                 | 4055.87  | 384.01                                        | 1,482,501.2 | 541,116,223   |
| Optimum 1200° K                            | 428.46                           | 123.3                                   | 35.92                              | 367.280  | -                                             | -           | -             |

Table 5: Effect of Oil injection on blast furnace performance and cost

| Parameters                | Unit    | Blast Temp.<br>°C | Blast Temperature<br>°C | Blast Temperature<br>°C | Blast Temperature<br>°C | Blast Temperature<br>°C |
|---------------------------|---------|-------------------|-------------------------|-------------------------|-------------------------|-------------------------|
|                           |         | 1200              | 1250                    | 1300                    | 1350                    | 1400                    |
| Coke rate                 | Kg/Thm  | 425.52            | 425.42                  | 425.32                  | 425.21                  | 425.11                  |
| Oil rate                  | Kg/Thm  | 133.91            | 133.88                  | 133.85                  | 133.82                  | 133.78                  |
| Oxygen rate               | Kg/Thm  | 7.26              | 7.251                   | 7.242                   | 7.237                   | 7.23                    |
| Total fuel rate           | Kg/Thm  | 566.69            | 566.55                  | 566.412                 | 566.267                 | 566.12                  |
| Blast air                 | Kg/Thm  | 226.88            | 226.73                  | 226.59                  | 226.45                  | 226.31                  |
| Cost of coke              | \$/Thm  | 3582.96           | 3582.08                 | 3581.21                 | 3580.34                 | 3579.47                 |
| Cost of oil               | \$/Thm  | 131.239           | 131.2075                | 131.1755                | 131.14                  | 131.11                  |
| Cost of oxygen            | \$/Thm  | 5.8082            | 5.804                   | 5.8                     | 5.797                   | 5.793                   |
| Total cost                | \$/Thm  | 3716.11           | 3715.21                 | 3714.30                 | 3713.40                 | 3712.5                  |
| Flame temperature         | Ok      | 2449.46           | 2488.67                 | 2527.88                 | 2567                    | 2606                    |
| Carbon from coke consumed | Kg/kgFe | 353.18            | 353.09                  | 353.21                  | 352.91                  | 353.84                  |
| Carbon from oil consumed  | Kg/kgFe | 115.16            | 115.13                  | 115.11                  | 115.08                  | 115.05                  |
| Total carbon consumed     | Kg/kgFe | 468.34            | 468.22                  | 468.12                  | 467.99                  | 467.89                  |

**Table 6: Cooling & coke replacement characteristics and the effect on coke rate for Typical injectants**

| Variant          | Blast temp. ok | Optimum cost Rate Kg/Thm | Optimum Injectant Rate Kg/Thm | Optimum oxygen Injection rate Kg/Thm | Optimum Blast air rate Kg/Thm | Flame Temp. OK | Replacement Ratio |
|------------------|----------------|--------------------------|-------------------------------|--------------------------------------|-------------------------------|----------------|-------------------|
| High Blast Temp. | 1200           | 565.18                   | -                             | -                                    | 427.62                        | 2450           | -                 |
| Natural gas      | 1200           | 428.46                   | 123.28                        | 28.92                                | 448.94                        | 2439           | 1.10              |
| Oil              | 1200           | 425.52                   | 133.91                        | 7.26                                 | 226.88                        | 2449           | 1.48              |
| Coal             | 1200           | 428.99                   | 148.75                        | -                                    | 244.63                        | 2379           | 0.91              |

Optimum cost for coke only without injectant = N4758.89/Thm

Optimum cost for coal dust injection = N437348/Thm

Optimum cost for oil injection = N3716.11/Thm

Optimum cost for natural gas injection = N3699.72/Thm

#### 4.2.4 OPTIMUM SOLUTION ANALYSIS

In a bid to reduce the consumption of coke, at the least, cost, it is proposed that the Blast furnace should use natural gas as blast additive due to its high coke saving. This should be accompanied by oxygen enrichment of the blast, which compensate to a desirable level for the cooling effect of natural gas on the flame temperature.

From the experience of blast furnace operators, and this work, Oxygen enrichment permits the use of more tuyere injectant. This work has provided the operational choice with their corresponding cost and thermal implication. As revealed by the results, it is quite obvious that the furnace can be operated at a much minimised coke consumption rate, compared with the design. Based on the operational and physical restrictions, the best optimum solution is natural gas injection at 1200k (Table 4 and Figure 11). Higher blast temperature will attract higher cost for heating which are not included in the programme, and may require the use of expensive higher heat resistance equipment.

At the optimal solution, it can be seen that;

- (1) 123.2847kg of Natural gas per tonne of Fe lowers the coke requirement of the process by approximately 136.4kg i.e. the weight replacement ratio is of the order of 1.1kg of coke per kg of Natural gas. This lowered coke requirement produces the desired effect of providing more gaseous space at the shaft of the furnace for iron ore, thus permitting higher permeability.
- (2) ₦3,699.9 will be spent in producing a tonne of pig iron. If the furnace is to be operated at no injectant, ₦4,768.71 will be spent and if to be operated at the designed

fuel combination, ₦4,099.87 will be spent. A cost saving of ₦1,064.97 is obtained when compared with no injectant, and ₦399.97 when compared with the designed.

- (3) The total carbon requirement of the process is decreased by injecting natural gas i.e. from 565.1891kg of carbon (from coke only) to 520.6176 of carbon (from both coke and natural gas) per tonne of product Fe. This is due to the contribution made by hydrogen towards reducing wustite in the wustite reduction zone.
- (4) The blast oxygen requirement is slightly increased with natural gas injection. This extra oxygen is necessary to compensate (by combusting extra oxygen) for the heat demand of the injectant.
- (5) With oxygen enrichment of up to 30% the total gas volume is kept not too high, thereby decreasing the amount of Nitrogen entering the furnace per kg mole of product Fe. Thus, the enriched oxygen compensates for the cooling effect from the injectant, and the nitrogen.

## CHAPTER FIVE

### 5.0 CONCLUSION AND RECOMMENDATION

#### 5.1 CONCLUSION

When a blast furnace is being operated in the era of high cost of metallurgical coke, it is important to carefully analyse and evaluate the performances of other cheap alternative fuels available at such locality, which will meet both the Stoichiometric and thermal requirement of the process.

This work has clearly shown the flexibility of the blast furnace process, and how the input parameters can be optimized in order to minimize the consumption rate of Metallurgical coke, still maintaining a good process controllability. Alternative fuel injection with increased blast temperature enables optimum raceway flame temperature and burden support to achieved and controlled.

Reliance on cheap Natural gas saves diminishing supplies of expensive Metallurgical coking coal requiring high-cost coke ovens. By this prediction procedure, the total inputs can be evaluated in the absence of costly experiments. More so, the value of auxiliary fuel injection will increase as the availability of metallurgical grade coke decreases, as coke-oven production deteriorates, and as coke-oven environmental emission standards becomes more stringent.

This optimization work meets both the operating equation and the furnace physical restrictions. It has been found to be both technically acceptable and economically justified.

For optimum, from the techno-economic analysis of the optimization programme, using the data from the Nigerian blast furnace at Ajaokuta Steel Complex, the following conclusions can be drawn;

The coke consumption rate should be 428.4686kg/Thm. while the natural gas consumption be 123.2847kg/Thm. Since the coke charge are to function more as support, they should have a high hot coke strength (CSR), and lower coke reactivity (CRI).

The blast temperature should be maintained at 1200k, because higher blast temperature is always cost demanding.

In order to increase the flame temperature at such fuel combination, the blast air should be enriched with oxygen, up to 30%.

The coke, should be charged at the centre of the furnace for proper burden support, while the natural gas being blown through the tuyere at the wall produces much of the heat needed, and the reducing gas.

## **5.2 RECOMMENDATIONS**

In order to obtain a better furnace performance and operating the furnace at the optimum fuel combination, further research work should be centered on obtaining a coke with high hot coke strength (CSR), and lower coke reactivity (CRI). Also, effort should be made on improving the charge distribution system to ensure charging coke at the centre of the furnace to give enough burden support.

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## APPENDIX I

### THE PROGRAM

```
%program to optimise the fuel cost of blast furnance
% written by Aboginiye Peter Apata

injectant=input('Enter the injectant number, CH4=1,
Oil=2, Coaldust=3 ');
teta=input ('input the percentage composition of carbon
in injectant, teta ');
beta=input('input the percentage composition of
hydrogen in injectant, beta ');
phi=input('input the percentage composition of oxygen
in injectant, phi ');

switch injectant
    case 1
        x=1;
        y=2;
        z=0;
        HOTBNI=-75000;
        Di= 145000;
        material='Natural gas';
        inj=0.49;%cost
    case 2
        x=1/12*(teta/100);
        y=1/2*(beta/100);
        z=0;
        HOTBNI=-1660;
        Di=4700;
        material='Oil';
        inj=0.98;%cost
    case 3
        x=1/12*(teta/100);
        y=1/2*(beta/100);
        z=1/16*(phi/100);
        HOTBNI=0;
        Di=2400;
        material='Coal Dust';
        inj=5.4;%cost
end
temp=input ('input the operating temperature');
t=num2str(temp);
wtC=input('input weight percent of carbon in
injectant');
```

```

wtH=input('input weight percent of hydrogen in
injectant');

%CFe('carbon content of the molten iron')
CFe=0.22;
% Eb=input('blast enthalpy')
Dwrz=388857;
%operating parameters
HOTBO2=36.2*temp-13500;
HOTBH2O=47.4*temp-22200-242000;
H1800C=30500;
HOTBN2=34.4*temp-13000;
HTFCO=36.6*temp-16400;
HTFH2=35.2*temp-17200;
HTFN2=36.4*temp-16500;
HOTBC=15.3*temp-46000;
HOTBH2=32.5*temp-12200;
HO1200O2=36.2*1200-13500;
%print heading for result NI/NC=injectant/coke ratio
%initialise the output file for results of calculation
%if ran without change, it overwrites the named file
%to change output filename, change the filename below
or
%add another path
% calculate eb
Eb=1/2*((HOTBO2-29940)+3.762*(HOTBN2-28280));
filenam=num2str(temp);
filename=strcat('a:',filenam,'.txt');
% rest=fopen(filename,'w');
i=1;
No=0;
for c=0:.0025:1;
    a=198000+95000*y-Di;
    b=Dwrz+198000*CFe-No*Eb;
    %equation is entered as a matrix [m1][d]=[m2]
    %where [d] is [NI NC]
    m1=[a 198000;-1 c];
    m2=[b;0];
    %solve for d
    d=inv(m1)*m2;
    N(i)=d(1);
    NC(i)=d(2);
    NAC(i)=NC(i)+x*N(i)-CFe;
    NB(i)=NAC(i)*1.3+y*N(i)*0.38-z*N(i)-1.06;
switch injectant
case 1
    NOB(i)=NB(i)/1.08;

```

```

    NO(i) = NB(i) - NOB(i);
    QNG = 286.4 * N;
    INJ = QNG;
case 2
    NOB(i) = NB(i) / 1.08;
    NO(i) = .4 * (NB(i) - NOB(i));
    QOIL = 14 * 17.9 * N;
    INJ = QOIL;
case 3
    NOB(i) = NB(i);
    NO(i) = 0;
    QCOAL = N * 214.8 / 0.76;
    INJ = QCOAL;
otherwise
    NOB(i) = NB(i);
    NO(i) = 0;
end
NH2o(i) = 0.024 * NOB(i);

flame = NOB(i) * 1/2 * HOTBO2 + NH2o(i) * HOTBH2O + NO(i) * HOTBO2 + N(i) * HOTBNI + ...
        ((NOB(i) + NH2o(i) + 2 * NO(i)) -
wtC / 1200 * N(i)) * H1800C + ...

1.88 * NOB(i) * HOTBN2 + (NOB(i) + NH2o(i) + 2 * NO(i)) * 127400 + (NH2o(i) + wtH / 200 * N(i)) * 17200 + 1.88 * NOB(i) * 16500;

flame1 = (NOB(i) + NH2o(i)) * 36.6 + (NH2o(i) + wtH / 200 * N(i)) * 35.2 + 1.88 * NOB(i) * 36.4;
flamet(i) = flame / flame1;
No = NO(i);
i = i + 1;
end

QCK = (214.8 / 0.83) * NC;
QOG = 286.4 * NO;
QOB = 286.4 * NOB;
switch injectant;
case 1
    g = 1;
    while (QNG(g) <= 125)
        g = g + 1;
    end
    h = 1;
    while (QCK(h) >= 385)
        h = h + 1;
    end
    g = min([g-1 h-1]);

```

```

cost=8.42*QCK+0.49*QNG+1.1*QOG;
h1=figure;
plot(QNG,QCK,'--', QNG,360,'-',125,QCK,'-.');
legend('Operating Equation Line', 'Minimum Coke
line','Maximum Injectant Line')
xlabel('QNG (Kg)');
ylabel('QCK (Kg)');
tit=strcat('OPTIMISATION GRAPH FOR NATURAL GAS AT BLAST
TEMPERATURE',t);
title(tit);
h2=figure;
plot(flamet,QCK,'--',flamet,QNG',':',flamet,QOB,'-
.',flamet,QOG,'-');
xlabel('FLAME TEMPERATURE oK')
ylabel('QUANTITY OF FUEL KG')
legend('QCK', 'QNG', 'QOB','QOG');
tit=strcat('GRAPH OF QUANTITY OF FUEL VS FLAME
TEMPERATURE AT ',t,'oK');
title(tit);
h3=figure;
plot(cost,QCK,':',cost,QNG,'--',cost,QOG,'-');
xlabel('COST (Naira)');
ylabel('FUEL QUANTITY (Kg)');
legend('QCK','QNG','QOG');
tit=strcat('GRAPH OF QUANTITY OF FUEL VS COST
AT',t,'oK');
title(tit);
case 2
    h=1;
    while(QCK(h)>=385)
        h=h+1;
    end
    g=1;
    while(QOIL(g)<135)
        g=g+1;
    end
    g=min([g-1 h-1]);
    cost=8.42*QCK+0.98*QOIL+1.1*QOG;
    h1=figure;
    plot(QOIL,QCK,':', QOIL,360,'--',135,QCK,'-');
    legend('Operating Equation Line', 'Minimum Coke
line','Maximum Injectant Line')
    xlabel('QOIL (Kg)');
    ylabel('QCK (Kg)');
    tit=strcat('OPTIMISATION GRAPH FOR OIL AT BLAST
TEMPERATURE',t);
    title(tit);

```

```

h2=figure;
plot(flamet,QCK,'--',flamet,QOIL,'-
.',flamet,QOB,':',flamet,QOG,'-');
xlabel('FLAME TEMPERATURE oK');
ylabel('QUANTITY OF FUEL KG');
legend('QCK', 'QOIL', 'QOB','QOG');
tit=strcat('GRAPH OF QUANTITY OF FUEL VS FLAME
TEMPERATURE AT ',t,'oK');
title(tit);
h3=figure;
plot(cost,QCK,'-',cost,QOIL,'--',cost,QOG,':');
xlabel('COST (Naira)');
ylabel('FUEL QUANTITY (Kg)');
legend('QCK', 'QOIL', 'QOG');
tit=strcat('GRAPH OF QUANTITY OF FUEL VS COST
AT',t,'oK');
title(tit);
case 3
    h=1;
    while(QCK(h)>=385)
        h=h+1;
    end
    g=1;
    while(QCOAL(g)<=150)
        g=g+1;
    end
    g=min([g-1 h-1]);
    cost=8.42*QCK+5.14*QCOAL;
    h1=figure;
    plot(QCOAL,QCK,':', QCOAL,360,'-.',150,QCK);
    legend('Operating Equation Line', 'Minimum Coke
line','Maximum Injectant Line')
    xlabel('QCOAL (Kg)');
    ylabel('QCOAL (Kg)');
    tit=strcat('OPTIMISATION GRAPH FOR COAL DUST AT BLAST
TEMPERATURE',t);
    title(tit);
h2=figure;
plot(flamet,QCK,'--',flamet,QCOAL,':',flamet,QOB,'-');
xlabel('FLAME TEMPERATURE oK');
ylabel('QUANTITY OF FUEL KG');
legend('QCK', 'QCOAL', 'QOB');
tit=strcat('GRAPH OF QUANTITY OF FUEL VS FLAME
TEMPERATURE AT ',t,'oK');
title(tit);
h3=figure;
plot(cost,QCK,'--',cost,QCOAL,'-');

```

```

xlabel('COST (Naira)');
ylabel('FUEL QUANTITY (Kg)');
legend('QCK','QCOAL');
tit=strcat('GRAPH OF QUANTITY OF FUEL VS COST
AT',t,'oK');
title(tit);
end
format compact;
format long G;
material;
OperatingTemperature=temp;
f=min([g-1 h-1]);
    fname1= strcat(t,material,'optim.jpg');
    fname2= strcat(t,material,'QTY.jpg');
    saveas(h1,fname1);
    saveas(h1,fname2);
    fname=strcat(material,t,'.txt');
    fid= fopen(fname,'w');
    fprintf(fid,'result computed for %s at temperature
%4f \n',material, temp);
    fprintf(fid,' QCK          QINJECT   QOB          QOG
COST          FLAME TEMP \n');
    for j=1:10:length(QNG);

fprintf(fid,'%8.4f\t%8.4f\t%8.4f\t%8.4f\t%8.4f\t%8.4f\n
',...
        QCK(j),INJ(j),QOB(j),QOG(j),cost(j),flamet(j));
    end
    fprintf(fid,'OPTIMUM Coke= %8.4f Kg\n',QCK(f));
    fprintf(fid,'OPTIMUM injectant= %8.4f Kg\n',INJ(f));
    fprintf(fid,'OPTIMUN Blast Oxygen= %8.4f
Kg\n',QOB(f));
    fprintf(fid,'OPTIMUM Injected Oxygen= %8.4f
Kg\n',QOG(f));
    fprintf(fid,'OPTIMUM TEMP=%8.4f oK\n',flamet(f));
    fprintf(fid,'OPTIMALCOST= %8.4f Naira\n', cost(g));
    fprintf(fid,'OPTIMALCOST of coke= %8.4f Naira\n',
8.42*QCK(f));
    fprintf(fid,'OPTIMALCOST of injectant = %8.4f
Naira\n', inj*INJ(f));
    fprintf(fid,'OPTIMALCOST of oxygen = %8.4f Naira\n',
0.8*QOG(f));
    fclose(fid);
    close all;

```

# APPENDIX II

## RESULTS

Result computed for Natural gas at temperature 1200.000000

| QCK      | QINJECT  | QOB      | QOG     | COST      | FLAME TEMP |
|----------|----------|----------|---------|-----------|------------|
| 565.1891 | 0.0000   | 395.9484 | 31.6759 | 4793.7354 | 2659.7517  |
| 548.3643 | 15.1714  | 402.4742 | 32.1979 | 4660.0788 | 2629.2702  |
| 532.5122 | 29.4657  | 408.6226 | 32.6898 | 4534.1496 | 2601.5243  |
| 517.5509 | 42.9567  | 414.4256 | 33.1540 | 4415.2965 | 2576.1615  |
| 503.4073 | 55.7104  | 419.9114 | 33.5929 | 4302.9395 | 2552.8874  |
| 490.0161 | 67.7856  | 425.1053 | 34.0084 | 4196.5601 | 2531.4543  |
| 477.3190 | 79.2350  | 430.0301 | 34.4024 | 4095.6936 | 2511.6519  |
| 465.2632 | 90.1060  | 434.7061 | 34.7765 | 3999.9224 | 2493.3011  |
| 453.8014 | 100.4414 | 439.1517 | 35.1321 | 3908.8698 | 2476.2478  |
| 442.8908 | 110.2798 | 443.3836 | 35.4707 | 3822.1955 | 2460.3591  |
| 432.4925 | 119.6563 | 447.4167 | 35.7933 | 3739.5911 | 2445.5197  |
| 422.5713 | 128.6025 | 451.2648 | 36.1012 | 3660.7766 | 2431.6289  |
| 413.0950 | 137.1475 | 454.9403 | 36.3952 | 3585.4969 | 2418.5986  |
| 404.0344 | 145.3177 | 458.4546 | 36.6764 | 3513.5196 | 2406.3513  |
| 395.3628 | 153.1372 | 461.8180 | 36.9454 | 3444.6318 | 2394.8184  |
| 387.0555 | 160.6281 | 465.0401 | 37.2032 | 3378.6390 | 2383.9392  |
| 379.0902 | 167.8106 | 468.1296 | 37.4504 | 3315.3623 | 2373.6597  |
| 371.4461 | 174.7035 | 471.0944 | 37.6876 | 3254.6375 | 2363.9315  |
| 364.1042 | 181.3239 | 473.9421 | 37.9154 | 3196.3133 | 2354.7115  |
| 357.0469 | 187.6877 | 476.6794 | 38.1344 | 3140.2499 | 2345.9610  |
| 350.2580 | 193.8094 | 479.3126 | 38.3450 | 3086.3186 | 2337.6448  |
| 343.7224 | 199.7027 | 481.8475 | 38.5478 | 3034.3999 | 2329.7315  |
| 337.4263 | 205.3801 | 484.2895 | 38.7432 | 2984.3833 | 2322.1925  |
| 331.3567 | 210.8533 | 486.6437 | 38.9315 | 2936.1660 | 2315.0018  |
| 325.5016 | 216.1330 | 488.9147 | 39.1132 | 2889.6528 | 2308.1359  |
| 319.8498 | 221.2294 | 491.1068 | 39.2885 | 2844.7548 | 2301.5732  |
| 314.3909 | 226.1518 | 493.2242 | 39.4579 | 2801.3894 | 2295.2941  |
| 309.1152 | 230.9091 | 495.2704 | 39.6216 | 2759.4793 | 2289.2805  |
| 304.0137 | 235.5093 | 497.2491 | 39.7799 | 2718.9526 | 2283.5161  |
| 299.0778 | 239.9601 | 499.1636 | 39.9331 | 2679.7419 | 2277.9855  |
| 294.2996 | 244.2687 | 501.0168 | 40.0813 | 2641.7841 | 2272.6750  |
| 289.6717 | 248.4418 | 502.8118 | 40.2249 | 2605.0200 | 2267.5715  |
| 285.1871 | 252.4857 | 504.5513 | 40.3641 | 2569.3943 | 2262.6632  |
| 280.8393 | 256.4063 | 506.2376 | 40.4990 | 2534.8548 | 2257.9392  |
| 276.6220 | 260.2091 | 507.8734 | 40.6299 | 2501.3527 | 2253.3892  |
| 272.5295 | 263.8994 | 509.4607 | 40.7569 | 2468.8418 | 2249.0038  |
| 268.5564 | 267.4821 | 511.0017 | 40.8801 | 2437.2790 | 2244.7743  |
| 264.6974 | 270.9619 | 512.4985 | 40.9999 | 2406.6231 | 2240.6924  |
| 260.9477 | 274.3431 | 513.9529 | 41.1162 | 2376.8359 | 2236.7506  |
| 257.3028 | 277.6298 | 515.3666 | 41.2293 | 2347.8807 | 2232.9417  |
| 253.7584 | 280.8259 | 516.7414 | 41.3393 | 2319.7233 | 2229.2592  |

OPTIMUM Coke= 428.4686 Kg

OPTIMUM injectant= 123.2847 Kg

OPTIMUM Blast Oxygen= 448.9774 Kg

OPTIMUM Injected Oxygen= 35.9182 Kg

OPTIMUM TEMP=2439.8547 oK

OPTIMALCOST= 3699.7266 Naira

OPTIMALCOST of coke= 3607.7058 Naira

OPTIMALCOST of injectant = 60.4095 Naira

OPTIMALCOST of oxygen = 28.7346 Naira

Result computed for Natural gas at temperature 1250.000000

| QCK      | QINJECT  | QOB      | QOG     | COST      | FLAME TEMP |
|----------|----------|----------|---------|-----------|------------|
| 545.1891 | 0.0000   | 395.9484 | 31.6759 | 4793.7354 | 2700.4080  |
| 547.7761 | 15.1551  | 401.6596 | 32.1328 | 4655.0469 | 2669.8344  |
| 531.9323 | 29.4336  | 407.7889 | 32.6231 | 4529.1774 | 2642.0047  |
| 516.9792 | 42.9093  | 413.5735 | 33.0859 | 4410.3847 | 2616.5654  |
| 502.8438 | 55.6480  | 419.0418 | 33.5233 | 4298.0880 | 2593.2212  |
| 489.4608 | 67.7087  | 424.2191 | 33.9375 | 4191.7688 | 2571.7234  |
| 476.7718 | 79.1441  | 429.1279 | 34.3302 | 4090.9622 | 2551.8614  |
| 464.7240 | 90.0015  | 433.7886 | 34.7031 | 3995.4250 | 2533.4554  |
| 453.2701 | 100.3238 | 438.2196 | 35.0576 | 3904.2562 | 2516.3507  |
| 442.3672 | 110.1494 | 442.4374 | 35.3950 | 3817.6397 | 2500.4143  |
| 431.9765 | 119.5135 | 446.4571 | 35.7166 | 3735.0923 | 2485.5303  |
| 422.0628 | 128.4478 | 450.2923 | 36.0234 | 3656.3337 | 2471.5978  |
| 412.5939 | 136.9812 | 453.9554 | 36.3164 | 3581.1091 | 2458.5284  |
| 403.5405 | 145.1401 | 457.4577 | 36.5966 | 3509.1856 | 2446.2443  |
| 394.8759 | 152.9486 | 460.8097 | 36.8648 | 3440.3508 | 2434.6768  |
| 386.5755 | 160.4288 | 464.0207 | 37.1217 | 3374.4099 | 2423.7650  |
| 378.6169 | 167.6011 | 467.0995 | 37.3680 | 3311.1840 | 2413.4544  |
| 370.9795 | 174.4840 | 470.0541 | 37.6043 | 3250.5089 | 2403.6973  |
| 363.6440 | 181.0947 | 472.8919 | 37.8313 | 3192.2333 | 2394.4497  |
| 356.5930 | 187.4491 | 475.6196 | 38.0496 | 3136.2177 | 2385.6729  |
| 349.8102 | 193.5617 | 478.2435 | 38.2595 | 3082.3329 | 2377.3318  |
| 343.2807 | 199.4461 | 480.7695 | 38.4616 | 3030.4598 | 2369.3948  |
| 336.9905 | 205.1149 | 483.2029 | 38.6562 | 2980.4878 | 2361.8333  |
| 330.9266 | 210.5796 | 485.5487 | 38.8439 | 2932.3141 | 2354.6211  |
| 325.0771 | 215.8512 | 487.8117 | 39.0249 | 2885.8435 | 2347.7346  |
| 319.4308 | 220.9396 | 489.9960 | 39.1997 | 2840.9872 | 2341.1523  |
| 313.9773 | 225.8543 | 492.1057 | 39.3685 | 2797.6674 | 2334.8544  |
| 308.7069 | 230.6040 | 494.1446 | 39.5316 | 2755.7924 | 2328.8228  |
| 303.6104 | 235.1969 | 496.1161 | 39.6893 | 2715.3047 | 2323.0411  |
| 298.6796 | 239.6406 | 498.0237 | 39.8419 | 2676.1321 | 2317.4941  |
| 293.9063 | 243.9422 | 499.8702 | 39.9896 | 2638.2115 | 2312.1676  |
| 289.2832 | 248.1086 | 501.6587 | 40.1327 | 2601.4839 | 2307.0489  |
| 284.8033 | 252.1459 | 503.3918 | 40.2713 | 2565.8939 | 2302.1260  |
| 280.4600 | 256.0600 | 505.0720 | 40.4058 | 2531.3893 | 2297.3878  |
| 276.2473 | 259.8566 | 506.7017 | 40.5361 | 2497.9214 | 2292.8243  |
| 272.1592 | 263.5408 | 508.2833 | 40.6627 | 2465.4440 | 2289.4354  |
| 268.1903 | 267.1175 | 509.8186 | 40.7855 | 2433.9138 | 2284.1836  |
| 264.3355 | 270.5914 | 511.3099 | 40.9048 | 2403.2901 | 2280.0895  |
| 260.5900 | 273.9669 | 512.7589 | 41.0207 | 2373.5341 | 2276.1359  |
| 256.9491 | 277.2481 | 514.1674 | 41.1334 | 2344.6097 | 2272.3157  |
| 253.4086 | 280.4388 | 515.5370 | 41.2430 | 2316.4824 | 2268.6222  |

OPTIMUM Coke= 426.9621 Kg

OPTIMUM injectant= 124.0325 Kg

OPTIMUM Blast Oxygen= 448.3970 Kg

OPTIMUM Injected Oxygen= 35.8718 Kg

OPTIMUM TEMP= 2478.4509 ok

OPTIMALCOST= 3687.3993 Naira

OPTIMALCOST of coke= 3595.0210 Naira

OPTIMALCOST of injectant = 60.7759 Naira

OPTIMALCOST of oxygen = 28.6974 Naira



Result computed for Natural gas at temperature 1300.000000

| QCK      | QINJECT  | QOB      | QOG     | COST      | FLAME TEMP |
|----------|----------|----------|---------|-----------|------------|
| 565.1891 | 0.0000   | 395.9484 | 31.6759 | 4793.7354 | 2741.0644  |
| 547.1903 | 15.1389  | 400.8484 | 32.0679 | 4650.0353 | 2710.1986  |
| 531.3547 | 29.4016  | 406.9585 | 32.5567 | 4524.2250 | 2682.4810  |
| 516.4098 | 42.8620  | 412.7250 | 33.0180 | 4405.4929 | 2656.9690  |
| 502.2827 | 55.5859  | 418.1759 | 33.4541 | 4293.2565 | 2633.5545  |
| 488.9078 | 67.6323  | 423.3365 | 33.8669 | 4186.9974 | 2611.9921  |
| 476.2268 | 79.0537  | 428.2295 | 34.2584 | 4086.2505 | 2592.0704  |
| 464.1870 | 89.8976  | 432.8750 | 34.6300 | 3990.5977 | 2573.6090  |
| 452.7410 | 100.2067 | 437.2914 | 34.9833 | 3899.6622 | 2556.4530  |
| 441.8459 | 110.0196 | 441.4953 | 35.3196 | 3813.1033 | 2540.4687  |
| 431.4628 | 119.3714 | 445.5016 | 35.6401 | 3730.6127 | 2525.5401  |
| 421.5565 | 128.2937 | 449.3239 | 35.9459 | 3651.9100 | 2511.5658  |
| 412.0949 | 136.8155 | 452.9747 | 36.2380 | 3576.7401 | 2498.4572  |
| 403.0487 | 144.9632 | 456.4652 | 36.5172 | 3504.8705 | 2486.1363  |
| 394.3911 | 152.7608 | 459.8057 | 36.7845 | 3436.0885 | 2474.5342  |
| 386.0976 | 160.2305 | 463.0057 | 37.0405 | 3370.1992 | 2463.5897  |
| 378.1457 | 167.3925 | 466.0739 | 37.2859 | 3307.0240 | 2453.2484  |
| 370.5148 | 174.2655 | 469.0183 | 37.5215 | 3246.3985 | 2443.4619  |
| 363.1858 | 180.8665 | 471.8462 | 37.7477 | 3188.1715 | 2434.1866  |
| 356.1411 | 187.2115 | 474.5644 | 37.9652 | 3132.2033 | 2425.3836  |
| 349.3645 | 193.3150 | 477.1792 | 38.1743 | 3078.3650 | 2417.0176  |
| 342.8409 | 199.1906 | 479.6963 | 38.3757 | 3026.5373 | 2409.0569  |
| 336.5566 | 204.8508 | 482.1212 | 38.5697 | 2976.6097 | 2401.4727  |
| 330.4984 | 210.3072 | 484.4587 | 38.7567 | 2928.4795 | 2394.2390  |
| 324.6545 | 215.5706 | 486.7136 | 38.9371 | 2882.0514 | 2387.3319  |
| 319.0137 | 220.6511 | 488.8901 | 39.1112 | 2837.2366 | 2380.7299  |
| 313.5655 | 225.5581 | 490.9923 | 39.2794 | 2793.9526 | 2374.4132  |
| 308.3003 | 230.3004 | 493.0238 | 39.4419 | 2752.1221 | 2368.3637  |
| 303.2090 | 234.8859 | 494.9883 | 39.5991 | 2711.6733 | 2362.5647  |
| 298.2832 | 239.3225 | 496.8890 | 39.7511 | 2672.5387 | 2357.0011  |
| 293.5148 | 243.6173 | 498.7289 | 39.8983 | 2634.6553 | 2351.6588  |
| 288.8965 | 247.7769 | 500.5109 | 40.0409 | 2597.9640 | 2346.5248  |
| 284.4212 | 251.8076 | 502.2376 | 40.1790 | 2562.4096 | 2341.5872  |
| 280.0825 | 255.7154 | 503.9117 | 40.3129 | 2527.9398 | 2336.8349  |
| 275.8742 | 259.5057 | 505.5355 | 40.4428 | 2494.5059 | 2332.2577  |
| 271.7905 | 263.1838 | 507.1112 | 40.5689 | 2462.0610 | 2327.8461  |
| 267.8259 | 266.7546 | 508.6410 | 40.6913 | 2430.5643 | 2323.5913  |
| 263.9753 | 270.2227 | 510.1268 | 40.8101 | 2399.9724 | 2319.4850  |
| 260.2339 | 273.5925 | 511.5704 | 40.9256 | 2370.2477 | 2315.5196  |
| 256.5970 | 276.8682 | 512.9737 | 41.0379 | 2341.3539 | 2311.6880  |
| 253.0604 | 280.0535 | 514.3383 | 41.1471 | 2313.2565 | 2307.9558  |

OPTIMUM Coke= 426.4521 Kg

OPTIMUM injectant= 123.8843 Kg

OPTIMUM Blast Oxygen= 447.4350 Kg

OPTIMUM Injected Oxygen= 35.7948 Kg

OPTIMUM TEMP=2518.4394 oK

OPTIMALCOST= 3682.9533 Naira

OPTIMALCOST of coke= 3590.7267 Naira

OPTIMALCOST of injectant = 60.7033 Naira

OPTIMALCOST of oxygen = 28.6358 Naira

Result computed for Natural gas at temperature 1350.000000

| QCK      | QINJECT  | QOB      | QOG     | COST      | FLAME TEMP |
|----------|----------|----------|---------|-----------|------------|
| 565.1891 | 0.0000   | 395.9484 | 31.6759 | 4793.7354 | 2781.7208  |
| 546.6069 | 15.1228  | 400.0404 | 32.0032 | 4645.0439 | 2750.9626  |
| 530.7795 | 29.3698  | 406.1316 | 32.4905 | 4519.2938 | 2722.9650  |
| 515.8428 | 42.8150  | 411.8799 | 32.9504 | 4400.6212 | 2697.3723  |
| 501.7230 | 55.5241  | 417.3135 | 33.3851 | 4288.4450 | 2673.8874  |
| 488.3571 | 67.5561  | 422.4576 | 33.7966 | 4182.2458 | 2652.2602  |
| 475.6842 | 78.9636  | 427.3348 | 34.1868 | 4081.5585 | 2632.2787  |
| 463.6523 | 89.7940  | 431.9652 | 34.5572 | 3985.9647 | 2613.7619  |
| 452.2141 | 100.0901 | 436.3672 | 34.9094 | 3895.0875 | 2596.5545  |
| 441.3267 | 109.8904 | 440.5572 | 35.2446 | 3808.5862 | 2580.5224  |
| 430.9512 | 119.2298 | 444.5502 | 35.5640 | 3726.1522 | 2565.5490  |
| 421.0523 | 128.1403 | 448.3597 | 35.8688 | 3647.5052 | 2551.5329  |
| 411.5980 | 136.6505 | 451.9982 | 36.1599 | 3572.3900 | 2538.3851  |
| 402.5590 | 144.7870 | 455.4769 | 36.4382 | 3500.5741 | 2526.0273  |
| 393.9084 | 152.5738 | 458.8061 | 36.7045 | 3431.8447 | 2514.3905  |
| 385.6218 | 160.0330 | 461.9952 | 36.9596 | 3366.0070 | 2503.4133  |
| 377.6766 | 167.1848 | 465.0579 | 37.204  | 3303.3855 | 2493.0211  |
| 370.0522 | 174.0479 | 467.9871 | 37.4390 | 3242.3062 | 2483.2754  |
| 362.7296 | 180.6393 | 470.8052 | 37.6644 | 3184.1275 | 2473.9224  |
| 355.6912 | 186.9750 | 473.5140 | 37.8811 | 3128.2067 | 2465.0931  |
| 348.9207 | 193.0694 | 476.1196 | 38.0896 | 3074.4147 | 2456.7021  |
| 342.4031 | 198.9362 | 478.6279 | 38.2902 | 3022.6323 | 2448.7177  |
| 336.1246 | 204.5878 | 481.0442 | 38.4835 | 2972.7489 | 2441.1109  |
| 330.0722 | 210.0359 | 483.3735 | 38.6699 | 2924.6621 | 2433.8555  |
| 324.2338 | 215.2913 | 485.6204 | 38.8496 | 2878.2763 | 2426.9279  |
| 318.5985 | 220.3639 | 487.7892 | 39.0231 | 2833.5029 | 2420.3062  |
| 313.1557 | 225.2633 | 489.8839 | 39.1907 | 2790.2594 | 2413.9707  |
| 307.8957 | 229.9981 | 491.9082 | 39.3527 | 2748.4685 | 2407.9031  |
| 302.8095 | 234.5764 | 493.8656 | 39.5093 | 2708.0584 | 2402.0869  |
| 297.8886 | 239.0059 | 495.7595 | 39.6608 | 2668.9616 | 2396.5067  |
| 293.1251 | 243.2938 | 497.5927 | 39.8074 | 2631.1152 | 2391.1485  |
| 288.5115 | 247.4467 | 499.3682 | 39.9495 | 2594.4602 | 2385.9992  |
| 284.0409 | 251.4709 | 501.0888 | 40.0871 | 2558.9412 | 2381.0469  |
| 279.7068 | 255.3723 | 502.7568 | 40.2205 | 2524.5061 | 2376.2805  |
| 275.5029 | 259.1564 | 504.3747 | 40.3500 | 2491.1061 | 2371.6897  |
| 271.4235 | 262.8285 | 505.9446 | 40.4756 | 2458.6952 | 2367.2649  |
| 267.4632 | 266.3933 | 507.4688 | 40.5975 | 2427.2301 | 2362.9974  |
| 263.6168 | 269.8557 | 508.9491 | 40.7159 | 2396.6700 | 2358.8789  |
| 259.8794 | 273.2199 | 510.3874 | 40.8310 | 2366.9765 | 2354.9018  |
| 256.2465 | 276.4900 | 511.7856 | 40.9428 | 2338.1131 | 2351.0588  |
| 252.7138 | 279.6700 | 513.1451 | 41.0516 | 2310.0456 | 2347.3433  |

OPTIMUM Coke= 425.9443 Kg

OPTIMUM injectant= 123.7368 Kg

OPTIMUM Blast Oxygen= 446.4771 Kg

OPTIMUM Injected Oxygen= 35.7182 Kg

OPTIMUM TEMP=2558.4271 oK

OPTIMALCOST= 3678.5264 Naira

OPTIMALCOST of coke= 3586.4508 Naira

OPTIMALCOST of injectant = 60.6310 Naira

OPTIMALCOST of oxygen = 28.5745 Naira

Result computed for Natural gas at temperature 1400.000000

| QCK      | QINJECT  | QOB      | QOG     | COST      | FLAME TEMP |
|----------|----------|----------|---------|-----------|------------|
| 565.1891 | 0.0000   | 395.9484 | 31.6759 | 4793.7354 | 2822.3772  |
| 546.0258 | 15.1067  | 399.2357 | 31.9389 | 4640.0725 | 2791.5265  |
| 530.2066 | 29.3381  | 405.3079 | 32.4246 | 4514.3820 | 2763.4447  |
| 515.2781 | 42.7681  | 411.0382 | 32.8831 | 4395.7694 | 2737.7772  |
| 501.1671 | 55.4625  | 416.4547 | 33.3164 | 4283.6532 | 2714.2199  |
| 487.8087 | 67.4802  | 421.5824 | 33.7266 | 4177.5140 | 2692.5278  |
| 475.1438 | 78.8739  | 426.4438 | 34.1155 | 4076.8861 | 2672.4865  |
| 463.1199 | 89.6909  | 431.0592 | 34.4847 | 3981.3512 | 2653.9143  |
| 451.6895 | 99.9739  | 435.4468 | 34.8357 | 3890.5322 | 2636.6554  |
| 440.8098 | 109.7616 | 439.6230 | 35.1698 | 3804.0883 | 2620.5752  |
| 430.4418 | 119.0889 | 443.6028 | 35.4882 | 3721.7107 | 2605.5571  |
| 420.5504 | 127.9875 | 447.3997 | 35.7920 | 3643.1192 | 2591.4991  |
| 411.1033 | 136.4863 | 451.0260 | 36.0821 | 3568.0586 | 2578.3120  |
| 402.0714 | 144.6117 | 454.4929 | 36.3594 | 3496.2962 | 2565.9174  |
| 393.4278 | 152.3877 | 457.8108 | 36.6249 | 3427.6192 | 2554.2458  |
| 385.1480 | 159.8364 | 460.9891 | 36.8791 | 3361.8330 | 2543.2358  |
| 377.2095 | 166.9781 | 464.0363 | 37.1229 | 3298.7586 | 2532.8327  |
| 369.5917 | 173.8313 | 466.9604 | 37.3568 | 3238.2318 | 2522.9877  |
| 362.2754 | 180.4132 | 469.7688 | 37.5815 | 3180.1014 | 2513.6570  |
| 355.2432 | 186.7395 | 472.4682 | 37.7975 | 3124.2277 | 2504.8014  |
| 348.4789 | 192.8250 | 475.0648 | 38.0052 | 3070.4819 | 2496.3854  |
| 341.9673 | 198.6830 | 477.5643 | 38.2051 | 3018.7446 | 2488.4172  |
| 335.6945 | 204.3261 | 479.9721 | 38.3978 | 2968.9054 | 2480.7477  |
| 329.6478 | 209.7659 | 482.2932 | 38.5835 | 2920.8617 | 2473.4708  |
| 323.8151 | 215.0132 | 484.5321 | 38.7626 | 2874.5181 | 2466.5225  |
| 318.1851 | 220.0780 | 486.6932 | 38.9355 | 2829.7860 | 2459.8811  |
| 312.7476 | 224.9698 | 488.7805 | 39.1024 | 2786.5828 | 2453.5268  |
| 307.4928 | 229.6971 | 490.7976 | 39.2638 | 2744.8314 | 2447.4411  |
| 302.4117 | 234.2683 | 492.7480 | 39.4198 | 2704.4598 | 2441.6076  |
| 297.4958 | 238.6908 | 494.6350 | 39.5708 | 2665.4008 | 2436.0108  |
| 292.7371 | 242.9718 | 496.4617 | 39.7169 | 2627.5913 | 2430.6367  |
| 288.1283 | 247.1180 | 498.2308 | 39.8585 | 2590.9724 | 2425.4721  |
| 283.6623 | 251.1357 | 499.9451 | 39.9956 | 2555.4886 | 2420.5050  |
| 279.3327 | 255.0308 | 501.6071 | 40.1286 | 2521.0880 | 2415.7245  |
| 275.1333 | 258.8087 | 503.2191 | 40.2575 | 2487.7218 | 2411.1200  |
| 271.0582 | 262.4747 | 504.7834 | 40.3827 | 2455.3440 | 2406.6821  |
| 267.1022 | 266.0338 | 506.3019 | 40.5042 | 2423.9113 | 2402.4020  |
| 263.2599 | 269.4904 | 507.7768 | 40.6221 | 2393.3829 | 2398.2712  |
| 259.5266 | 272.8490 | 509.2099 | 40.7368 | 2363.7204 | 2394.2822  |
| 255.8977 | 276.1136 | 510.6029 | 40.8482 | 2334.8873 | 2390.4278  |
| 252.3689 | 279.2882 | 511.9575 | 40.9566 | 2306.8495 | 2386.7011  |

OPTIMUM Coke= 425.4386 Kg

OPTIMUM injectant= 123.5899 Kg

OPTIMUM Blast Oxygen= 445.5231 Kg

OPTIMUM Injected Oxygen= 35.6419 Kg

OPTIMUM TEMP=2598.4139 oK

OPTIMALCOST= 3674.1183 Naira

OPTIMALCOST of coke= 3582.1931 Naira

OPTIMALCOST of injectant = 60.5591 Naira

OPTIMALCOST of oxygen = 28.5135 Naira

Result computed for Oil at temperature 1200.000000

| QCK      | QINJECT  | QOB      | QOG     | COST      | FLAME TEMP |
|----------|----------|----------|---------|-----------|------------|
| 565.1891 | 0.0000   | 395.9484 | 12.6703 | 4772.8293 | 2504.2977  |
| 551.2716 | 13.3454  | 379.1002 | 12.1312 | 4668.1292 | 2500.9797  |
| 538.0230 | 26.0493  | 363.0619 | 11.6180 | 4568.4616 | 2497.5416  |
| 525.3963 | 38.1569  | 347.7764 | 11.1288 | 4473.4721 | 2493.9768  |
| 513.3486 | 49.7093  | 333.1918 | 10.6621 | 4382.8389 | 2490.2781  |
| 501.8411 | 60.7437  | 319.2612 | 10.2164 | 4296.2691 | 2486.4378  |
| 490.8382 | 71.2943  | 305.9414 | 9.7901  | 4213.4954 | 2482.4476  |
| 480.3075 | 81.3921  | 293.1931 | 9.3822  | 4134.2735 | 2478.2986  |
| 470.2191 | 91.0658  | 280.9804 | 8.9914  | 4058.3795 | 2473.9811  |
| 460.5457 | 100.3414 | 269.2702 | 8.6166  | 3985.6081 | 2469.4846  |
| 451.2624 | 109.2431 | 258.0320 | 8.2570  | 3915.7704 | 2464.7978  |
| 442.3459 | 117.7930 | 247.2380 | 7.9116  | 3848.6926 | 2459.9083  |
| 433.7750 | 126.0116 | 236.8622 | 7.5796  | 3784.2142 | 2454.8027  |
| 425.5298 | 133.9178 | 226.8809 | 7.2602  | 3722.1870 | 2449.4664  |
| 417.5923 | 141.5290 | 217.2720 | 6.9527  | 3662.4738 | 2443.8832  |
| 409.9455 | 148.8615 | 208.0149 | 6.6565  | 3604.9475 | 2438.0357  |
| 402.5737 | 155.9302 | 199.0908 | 6.3709  | 3549.4901 | 2431.9047  |
| 395.4623 | 162.7492 | 190.4820 | 6.0954  | 3495.9920 | 2425.4691  |
| 388.5978 | 169.3315 | 182.1721 | 5.8295  | 3444.3512 | 2418.7055  |
| 381.9676 | 175.6892 | 174.1457 | 5.5727  | 3394.4725 | 2411.5882  |
| 375.5598 | 181.8335 | 166.3886 | 5.3244  | 3346.2674 | 2404.0887  |
| 369.3635 | 187.7752 | 158.8875 | 5.0844  | 3299.6529 | 2396.1755  |
| 363.3683 | 193.5239 | 151.6298 | 4.8522  | 3254.5516 | 2387.8133  |
| 357.5646 | 199.0890 | 144.6041 | 4.6273  | 3210.8911 | 2378.9627  |
| 351.9434 | 204.4791 | 137.7992 | 4.4096  | 3168.6033 | 2369.5797  |
| 346.4962 | 209.7024 | 131.2050 | 4.1986  | 3127.6245 | 2359.6148  |
| 341.2150 | 214.7664 | 124.8117 | 3.9940  | 3087.8949 | 2349.0121  |
| 336.0924 | 219.6784 | 118.6105 | 3.7955  | 3049.3582 | 2337.7084  |
| 331.1214 | 224.4451 | 112.5927 | 3.6030  | 3011.9614 | 2325.6316  |
| 326.2952 | 229.0728 | 106.7503 | 3.4160  | 2975.6548 | 2312.6999  |
| 321.6077 | 233.5676 | 101.0757 | 3.2344  | 2940.3914 | 2298.8189  |
| 317.0530 | 237.9351 | 95.5619  | 3.0580  | 2906.1267 | 2283.8802  |
| 312.6255 | 242.1806 | 90.2021  | 2.8865  | 2872.8191 | 2267.7582  |
| 308.3200 | 246.3091 | 84.9899  | 2.7197  | 2840.4288 | 2250.3064  |
| 304.1314 | 250.3255 | 79.9194  | 2.5574  | 2808.9187 | 2231.3532  |
| 300.0551 | 254.2342 | 74.9847  | 2.3995  | 2778.2532 | 2210.6962  |
| 296.0867 | 258.0395 | 70.1806  | 2.2458  | 2748.3988 | 2188.0948  |
| 292.2218 | 261.7455 | 65.5019  | 2.0961  | 2719.3239 | 2163.2609  |
| 288.4565 | 265.3560 | 60.9438  | 1.9502  | 2690.9981 | 2135.8466  |
| 284.7871 | 268.8746 | 56.5017  | 1.8081  | 2663.3931 | 2105.4277  |
| 281.2098 | 272.3048 | 52.1711  | 1.6695  | 2636.4816 | 2071.4814  |

OPTIMUM Coke= 425.5298 Kg

OPTIMUM injectant= 133.9178 Kg

OPTIMUM Blast Oxygen= 226.8809 Kg

OPTIMUM Injected Oxygen= 7.2602 Kg

OPTIMUM TEMP=2449.4664 oK

OPTIMALCOST= 3716.1137 Naira

OPTIMALCOST of coke= 3582.9613 Naira

OPTIMALCOST of injectant = 131.2394 Naira

OPTIMALCOST of oxygen = 5.8082 Naira

Result computed for Oil at temperature 1250.000000

| QCK      | QINJECT  | QOB      | QOG     | COST      | FLAME TEMP |
|----------|----------|----------|---------|-----------|------------|
| 565.1891 | 0.0000   | 395.9484 | 12.6703 | 4772.8293 | 2544.1402  |
| 551.0472 | 13.3399  | 378.8007 | 12.1216 | 4666.2242 | 2540.7840  |
| 537.8133 | 26.0391  | 362.7813 | 11.6090 | 4566.6760 | 2537.3063  |
| 525.2001 | 38.1427  | 347.5132 | 11.1204 | 4471.7971 | 2533.7004  |
| 513.1650 | 49.6915  | 332.9450 | 10.6542 | 4381.2666 | 2529.9590  |
| 501.6691 | 60.7229  | 319.0294 | 10.2089 | 4294.7922 | 2526.0745  |
| 490.6770 | 71.2708  | 305.7236 | 9.7832  | 4212.1073 | 2522.0383  |
| 480.1563 | 81.3665  | 292.9885 | 9.3756  | 4132.9681 | 2517.8415  |
| 470.0772 | 91.0383  | 280.7880 | 8.9852  | 4057.1514 | 2513.4743  |
| 460.4126 | 100.3124 | 269.0891 | 8.6109  | 3984.4522 | 2508.9260  |
| 451.1374 | 109.2128 | 257.8616 | 8.2516  | 3914.6821 | 2504.1852  |
| 442.2285 | 117.7618 | 247.0776 | 7.9065  | 3847.6676 | 2499.2794  |
| 433.6646 | 125.9796 | 236.7112 | 7.5748  | 3783.2486 | 2494.0750  |
| 425.4262 | 133.8852 | 226.7387 | 7.2556  | 3721.2771 | 2488.6771  |
| 417.4949 | 141.4960 | 217.1380 | 6.9484  | 3661.6164 | 2483.0297  |
| 409.8539 | 148.8282 | 207.8887 | 6.6524  | 3604.1394 | 2477.1149  |
| 402.4876 | 155.8969 | 198.9719 | 6.3671  | 3548.7285 | 2470.9133  |
| 395.3814 | 162.7159 | 190.3700 | 6.0918  | 3495.2743 | 2464.4036  |
| 388.5218 | 169.2984 | 182.0666 | 5.8261  | 3443.6748 | 2457.5621  |
| 381.8962 | 175.6563 | 174.0463 | 5.5695  | 3393.8353 | 2450.3629  |
| 375.4927 | 181.8010 | 166.2951 | 5.3214  | 3345.6671 | 2442.7772  |
| 369.3004 | 187.7431 | 158.7994 | 5.0816  | 3299.0876 | 2434.7729  |
| 363.3091 | 193.4924 | 151.5470 | 4.8495  | 3254.0195 | 2426.3145  |
| 357.5090 | 199.0581 | 144.5262 | 4.6248  | 3210.3903 | 2417.3621  |
| 351.8913 | 204.4488 | 137.7259 | 4.4072  | 3168.1323 | 2407.8712  |
| 346.4473 | 209.6728 | 131.1361 | 4.1964  | 3127.1818 | 2397.7917  |
| 341.1692 | 214.7376 | 124.7471 | 3.9919  | 3087.4790 | 2387.0671  |
| 336.0496 | 219.6504 | 118.5499 | 3.7936  | 3048.9678 | 2375.6334  |
| 331.0813 | 224.4179 | 112.5358 | 3.6011  | 3011.5954 | 2363.4179  |
| 326.2578 | 229.0466 | 106.6971 | 3.4143  | 2975.3119 | 2350.3376  |
| 321.5728 | 233.5422 | 101.0260 | 3.2328  | 2940.0704 | 2336.2977  |
| 317.0205 | 237.9106 | 95.5154  | 3.0565  | 2905.8268 | 2321.1670  |
| 312.5952 | 242.1571 | 90.1587  | 2.8851  | 2872.5391 | 2304.8799  |
| 308.2918 | 246.2866 | 84.9495  | 2.7184  | 2840.1680 | 2287.2278  |
| 304.1053 | 250.3040 | 79.8818  | 2.5562  | 2808.6760 | 2268.0572  |
| 300.0309 | 254.2137 | 74.9499  | 2.3984  | 2778.0279 | 2247.1633  |
| 296.0643 | 258.0200 | 70.1484  | 2.2447  | 2748.1902 | 2224.3028  |
| 292.2012 | 261.7270 | 65.4721  | 2.0951  | 2719.1312 | 2199.1843  |
| 288.4376 | 265.3386 | 60.9164  | 1.9493  | 2690.8207 | 2171.4560  |
| 284.7697 | 268.8582 | 56.4765  | 1.8072  | 2663.2302 | 2140.6888  |
| 281.1940 | 272.2895 | 52.1481  | 1.6687  | 2636.3326 | 2106.3542  |

OPTIMUM Coke= 425.4262 Kg

OPTIMUM injectant= 133.8852 Kg

OPTIMUM Blast Oxygen= 226.7387 Kg

OPTIMUM Injected Oxygen= 7.2556 Kg

OPTIMUM TEMP=2488.6771 oK

OPTIMALCOST= 3715.2092 Naira

OPTIMALCOST of coke= 3582.0885 Naira

OPTIMALCOST of injectant = 131.2075 Naira

OPTIMALCOST of oxygen = 5.8045 Naira

Result computed for Oil at temperature 1300.000000

| QCK      | QINJECT  | QOB      | QOG     | COST      | FLAME TEMP |
|----------|----------|----------|---------|-----------|------------|
| 565.1891 | 0.0000   | 395.9484 | 12.6703 | 4772.8293 | 2583.9828  |
| 550.8232 | 13.3345  | 378.5016 | 12.1121 | 4664.3221 | 2580.5883  |
| 537.6039 | 26.0290  | 362.5011 | 11.6000 | 4564.8931 | 2577.0709  |
| 525.0042 | 38.1284  | 347.2505 | 11.1120 | 4470.1247 | 2573.4239  |
| 512.9816 | 49.6737  | 332.6985 | 10.6464 | 4379.6967 | 2569.6399  |
| 501.4974 | 60.7021  | 318.7980 | 10.2015 | 4293.3175 | 2565.7110  |
| 490.5160 | 71.2475  | 305.5062 | 9.7762  | 4210.7217 | 2561.6289  |
| 480.0053 | 81.3409  | 292.7841 | 9.3691  | 4131.6646 | 2557.3842  |
| 469.9356 | 91.0109  | 280.5950 | 8.9791  | 4055.9250 | 2552.9672  |
| 460.2796 | 100.2834 | 268.9083 | 8.6051  | 3983.2979 | 2548.3671  |
| 451.0125 | 109.1826 | 257.6915 | 8.2461  | 3913.5952 | 2543.5722  |
| 442.1112 | 117.7305 | 246.9174 | 7.9014  | 3846.6439 | 2538.5701  |
| 433.5545 | 125.9476 | 236.5604 | 7.5699  | 3782.2842 | 2533.3468  |
| 425.3226 | 133.8526 | 226.5966 | 7.2511  | 3720.3684 | 2527.8875  |
| 417.3976 | 141.4630 | 217.0042 | 6.9441  | 3660.7600 | 2522.1757  |
| 409.7625 | 148.7950 | 207.7627 | 6.6484  | 3603.3323 | 2516.1935  |
| 402.4017 | 155.8636 | 198.8532 | 6.3633  | 3547.9674 | 2509.9211  |
| 395.3006 | 162.6827 | 190.2582 | 6.0883  | 3494.5574 | 2503.3374  |
| 388.4419 | 169.2653 | 181.9612 | 5.8228  | 3442.9993 | 2496.4180  |
| 381.8248 | 175.6235 | 173.9471 | 5.5663  | 3393.1987 | 2489.1369  |
| 375.4256 | 181.7686 | 166.2016 | 5.3185  | 3345.0675 | 2481.4648  |
| 369.2375 | 187.7111 | 158.7115 | 5.0788  | 3298.5229 | 2473.3694  |
| 363.2500 | 193.4609 | 151.4643 | 4.8469  | 3253.4879 | 2464.8147  |
| 357.4535 | 199.0272 | 144.4483 | 4.6223  | 3209.8901 | 2455.7604  |
| 351.8392 | 204.4186 | 137.6528 | 4.4049  | 3167.6618 | 2446.1616  |
| 346.3985 | 209.6433 | 131.0674 | 4.1942  | 3126.7395 | 2435.9674  |
| 341.1235 | 214.7088 | 124.6826 | 3.9898  | 3087.0636 | 2425.1209  |
| 336.0068 | 219.6224 | 118.4893 | 3.7917  | 3048.5779 | 2413.5572  |
| 331.0413 | 224.3908 | 112.4791 | 3.5993  | 3011.2297 | 2401.2028  |
| 326.2204 | 229.0203 | 106.6439 | 3.4126  | 2974.9693 | 2387.9738  |
| 321.5379 | 233.5169 | 100.9762 | 3.2312  | 2939.7498 | 2373.7738  |
| 316.9879 | 237.8862 | 95.4690  | 3.0550  | 2905.5271 | 2358.4920  |
| 312.5649 | 242.1336 | 90.1154  | 2.8837  | 2872.2595 | 2341.9997  |
| 308.2636 | 246.2641 | 84.9092  | 2.7171  | 2839.9074 | 2324.1472  |
| 304.0791 | 250.2825 | 79.8443  | 2.5550  | 2808.4336 | 2304.7590  |
| 300.0067 | 254.1932 | 74.9151  | 2.3973  | 2777.8029 | 2283.6280  |
| 296.0419 | 258.0006 | 70.1161  | 2.2437  | 2747.9818 | 2260.5083  |
| 292.1806 | 261.7086 | 65.4424  | 2.0942  | 2718.9386 | 2235.1051  |
| 288.4187 | 265.3212 | 60.8890  | 1.9484  | 2690.6433 | 2207.0626  |
| 284.7524 | 268.8419 | 56.4513  | 1.8064  | 2663.0674 | 2175.9470  |
| 281.1782 | 272.2742 | 52.1251  | 1.6680  | 2636.1837 | 2141.2237  |

OPTIMUM Coke= 425.3226 Kg

OPTIMUM injectant= 133.8526 Kg

OPTIMUM Blast Oxygen= 226.5966 Kg

OPTIMUM Injected Oxygen= 7.2511 Kg

OPTIMUM TEMP=2527.8875 oK

OPTIMALCOST= 3714.3059 Naira

OPTIMALCOST of coke= 3581.2167 Naira

OPTIMALCOST of injectant = 131.1755 Naira

OPTIMALCOST of oxygen = 5.8009 Naira

Result computed for Oil at temperature 1350.000000

| QCK      | QINJECT  | QOB      | QOG     | COST      | FLAME TEMP |
|----------|----------|----------|---------|-----------|------------|
| 565.1891 | 0.0000   | 395.9484 | 12.6703 | 4772.8293 | 2623.8253  |
| 550.5995 | 13.3291  | 378.2029 | 12.1025 | 4662.4231 | 2620.3926  |
| 537.3948 | 26.0189  | 362.2213 | 11.5911 | 4563.1130 | 2616.8355  |
| 524.8087 | 38.1142  | 346.9882 | 11.1036 | 4468.4548 | 2613.1473  |
| 512.7986 | 49.6560  | 332.4523 | 10.6385 | 4378.1290 | 2609.3206  |
| 501.3258 | 60.6813  | 318.5669 | 10.1941 | 4291.8449 | 2605.3474  |
| 490.3553 | 71.2241  | 305.2891 | 9.7693  | 4209.3370 | 2601.2192  |
| 479.8545 | 81.3153  | 292.5800 | 9.3626  | 4130.3629 | 2596.9267  |
| 469.7941 | 90.9835  | 280.4039 | 8.9729  | 4054.7003 | 2592.4598  |
| 460.1468 | 100.2545 | 268.7278 | 8.5993  | 3982.1451 | 2587.8078  |
| 450.8878 | 109.1524 | 257.5216 | 8.2407  | 3912.5098 | 2582.9589  |
| 441.9941 | 117.6993 | 246.7574 | 7.8962  | 3845.6216 | 2577.9004  |
| 433.4444 | 125.9156 | 236.4097 | 7.5651  | 3781.3210 | 2572.6182  |
| 425.2192 | 133.8200 | 226.4547 | 7.2466  | 3719.4609 | 2567.0973  |
| 417.3004 | 141.4301 | 216.8705 | 6.9399  | 3659.9047 | 2561.3212  |
| 409.6711 | 148.7618 | 207.6368 | 6.6444  | 3602.5262 | 2555.2715  |
| 402.3158 | 155.8303 | 198.7346 | 6.3595  | 3547.2081 | 2548.9286  |
| 395.2199 | 162.6495 | 190.1464 | 6.0847  | 3493.8414 | 2542.2706  |
| 388.3700 | 169.2322 | 181.8560 | 5.8194  | 3442.3245 | 2535.2732  |
| 381.7535 | 175.5907 | 173.8480 | 5.5631  | 3392.5629 | 2527.9100  |
| 375.3587 | 181.7362 | 166.1083 | 5.3155  | 3344.4685 | 2520.1515  |
| 369.1746 | 187.6791 | 158.6236 | 5.0760  | 3297.9588 | 2511.9650  |
| 363.1909 | 193.4294 | 151.3816 | 4.8442  | 3252.9568 | 2503.3139  |
| 357.3981 | 198.9963 | 144.3706 | 4.6199  | 3209.3904 | 2494.1577  |
| 351.7872 | 204.3884 | 137.5797 | 4.4025  | 3167.1918 | 2484.4508  |
| 346.3498 | 209.6138 | 130.9967 | 4.1920  | 3126.2977 | 2474.1419  |
| 341.0779 | 214.6801 | 124.6181 | 3.9878  | 3086.6486 | 2463.1733  |
| 335.9640 | 219.5945 | 118.4288 | 3.7897  | 3048.1884 | 2451.4795  |
| 331.0013 | 224.3637 | 112.4224 | 3.5975  | 3010.8644 | 2438.9862  |
| 326.1830 | 228.9941 | 106.5908 | 3.4109  | 2974.6271 | 2425.6084  |
| 321.5030 | 233.4916 | 100.9266 | 3.2296  | 2939.4296 | 2411.2488  |
| 316.9554 | 237.8618 | 95.4226  | 3.0535  | 2905.2278 | 2395.7952  |
| 312.5346 | 242.1102 | 90.0721  | 2.8823  | 2871.9801 | 2379.1176  |
| 308.2355 | 246.2416 | 84.8688  | 2.7158  | 2839.6470 | 2361.0645  |
| 304.0530 | 250.2610 | 79.8068  | 2.5538  | 2808.1915 | 2341.4586  |
| 299.9825 | 254.1727 | 74.8803  | 2.3962  | 2777.5781 | 2320.0905  |
| 296.0196 | 257.9811 | 70.0839  | 2.2427  | 2747.7736 | 2296.7113  |
| 292.1600 | 261.6902 | 65.4126  | 2.0932  | 2718.7463 | 2271.0232  |
| 288.3998 | 265.3038 | 60.8616  | 1.9476  | 2690.4661 | 2242.6664  |
| 284.7351 | 268.8255 | 56.4262  | 1.8056  | 2662.9047 | 2211.2021  |
| 281.1624 | 272.2589 | 52.1021  | 1.6673  | 2636.0350 | 2176.0901  |

OPTIMUM Coke= 425.2192 Kg

OPTIMUM injectant= 133.8200 Kg

OPTIMUM Blast Oxygen= 226.4547 Kg

OPTIMUM Injected Oxygen= 7.2466 Kg

OPTIMUM TEMP=2567.0973 oK

OPTIMALCOST= 3713.4037 Naira

OPTIMALCOST of coke= 3580.3460 Naira

OPTIMALCOST of injectant = 131.1436 Naira

OPTIMALCOST of oxygen = 5.7972 Naira

## Result computed for Oil at temperature 1400.000000

| QCK      | QINJECT  | QOB      | QOG     | COST      | FLAME TEMP |
|----------|----------|----------|---------|-----------|------------|
| 565.1891 | 0.0000   | 395.9484 | 12.6703 | 4772.8293 | 2663.6679  |
| 550.3762 | 13.3237  | 377.9048 | 12.0930 | 4660.5270 | 2660.1968  |
| 537.1861 | 26.0088  | 361.9419 | 11.5821 | 4561.3357 | 2656.6000  |
| 524.6134 | 38.1000  | 346.7263 | 11.0952 | 4466.7874 | 2652.8706  |
| 512.6157 | 49.6383  | 332.2065 | 10.6306 | 4376.5637 | 2649.0012  |
| 501.1546 | 60.6606  | 318.3361 | 10.1868 | 4290.3744 | 2644.9837  |
| 490.1947 | 71.2008  | 305.0723 | 9.7623  | 4207.9549 | 2640.8094  |
| 479.7040 | 81.2898  | 292.3762 | 9.3560  | 4129.0631 | 2636.4689  |
| 469.6528 | 90.9561  | 280.2122 | 8.9668  | 4053.4772 | 2631.9522  |
| 460.0142 | 100.2256 | 268.5475 | 8.5935  | 3980.9939 | 2627.2483  |
| 450.7633 | 109.1223 | 257.3519 | 8.2353  | 3911.4258 | 2622.3453  |
| 441.8771 | 117.6682 | 246.5977 | 7.8911  | 3844.6005 | 2617.2303  |
| 433.3345 | 125.8837 | 236.2593 | 7.5603  | 3780.3591 | 2611.8892  |
| 425.1160 | 133.7875 | 226.3131 | 7.2420  | 3718.5544 | 2606.3067  |
| 417.2033 | 141.3972 | 216.7371 | 6.9356  | 3659.0505 | 2600.4661  |
| 409.5799 | 148.7287 | 207.5111 | 6.6404  | 3601.7211 | 2594.3490  |
| 402.2300 | 155.7971 | 198.6162 | 6.3557  | 3546.4493 | 2587.9354  |
| 395.1393 | 162.6163 | 190.0349 | 6.0811  | 3493.1262 | 2581.2031  |
| 388.2943 | 169.1992 | 181.7509 | 5.8160  | 3441.6505 | 2574.1277  |
| 381.6823 | 175.5580 | 173.7490 | 5.5600  | 3391.9279 | 2566.6825  |
| 375.2918 | 181.7038 | 166.0151 | 5.3125  | 3343.8703 | 2558.8375  |
| 369.1117 | 187.6472 | 158.5359 | 5.0731  | 3297.3954 | 2550.5597  |
| 363.1319 | 193.3980 | 151.2990 | 4.8416  | 3252.4264 | 2541.8122  |
| 357.3427 | 198.9655 | 144.2929 | 4.6174  | 3208.8912 | 2532.5540  |
| 351.7353 | 204.3582 | 137.5067 | 4.4002  | 3166.7223 | 2522.7390  |
| 346.3011 | 209.5843 | 130.9301 | 4.1898  | 3125.8564 | 2512.3153  |
| 341.0322 | 214.6514 | 124.5537 | 3.9857  | 3086.2340 | 2501.2245  |
| 335.9213 | 219.5666 | 118.3684 | 3.7878  | 3047.7992 | 2489.4005  |
| 330.9613 | 224.3366 | 112.3657 | 3.5957  | 3010.4995 | 2476.7681  |
| 326.1457 | 228.9678 | 106.5377 | 3.4092  | 2974.2851 | 2463.2415  |
| 321.4681 | 233.4662 | 100.8769 | 3.2281  | 2939.1096 | 2448.7221  |
| 316.9229 | 237.8374 | 95.3762  | 3.0520  | 2904.2287 | 2433.0966  |
| 312.5044 | 242.0867 | 90.0288  | 2.8809  | 2871.7009 | 2416.2336  |
| 308.2074 | 246.2192 | 84.8285  | 2.7145  | 2839.3869 | 2397.9799  |
| 304.0269 | 250.2395 | 79.7693  | 2.5526  | 2807.9495 | 2378.1561  |
| 299.9584 | 254.1523 | 74.8455  | 2.3951  | 2777.3535 | 2356.5506  |
| 295.9973 | 257.9617 | 70.0517  | 2.2417  | 2747.5656 | 2332.9119  |
| 292.1395 | 261.6718 | 65.3829  | 2.0923  | 2718.5541 | 2306.9387  |
| 288.3809 | 265.2864 | 60.8342  | 1.9467  | 2690.2891 | 2278.2673  |
| 284.7178 | 268.8092 | 56.4011  | 1.8048  | 2662.7422 | 2246.4542  |
| 281.1466 | 272.2436 | 52.0792  | 1.6665  | 2635.8864 | 2210.9531  |

OPTIMUM Coke= 425.1160 Kg

OPTIMUM injectant= 133.7875 Kg

OPTIMUM Blast Oxygen= 226.3131 Kg

OPTIMUM Injected Oxygen= 7.2420 Kg

OPTIMUM TEMP=2606.3067 oK

OPTIMALCOST= 3712.5027 Naira

OPTIMALCOST of coke= 3579.4764 Naira

OPTIMALCOST of injectant = 131.1118 Naira

OPTIMALCOST of oxygen = 5.7936 Naira

Result computed for Coal-Dust at temperature 1200.000000

| QCK      | QINJECT  | QOB      | QOG    | COST      | FLAME TEMP |
|----------|----------|----------|--------|-----------|------------|
| 565.1891 | 0.0000   | 427.6243 | 0.0000 | 4758.8920 | 2400.6617  |
| 551.3928 | 15.0545  | 409.1251 | 0.0000 | 4720.1071 | 2399.3243  |
| 538.2539 | 29.3915  | 391.5075 | 0.0000 | 4683.1705 | 2397.9342  |
| 525.7267 | 43.0612  | 374.7100 | 0.0000 | 4647.9533 | 2396.4880  |
| 513.7693 | 56.1090  | 358.6766 | 0.0000 | 4614.3380 | 2394.9823  |
| 502.3438 | 68.5765  | 343.3563 | 0.0000 | 4582.2179 | 2393.4135  |
| 491.4153 | 80.5016  | 328.7026 | 0.0000 | 4551.4954 | 2391.7773  |
| 480.9523 | 91.9188  | 314.6728 | 0.0000 | 4522.0810 | 2390.0695  |
| 470.9255 | 102.8600 | 301.2281 | 0.0000 | 4493.8932 | 2388.2852  |
| 461.3082 | 113.3544 | 288.3325 | 0.0000 | 4466.8566 | 2386.4191  |
| 452.0759 | 123.4286 | 275.9531 | 0.0000 | 4440.9023 | 2384.4654  |
| 443.2059 | 133.1076 | 264.0594 | 0.0000 | 4415.9664 | 2382.4180  |
| 434.6772 | 142.4140 | 252.6235 | 0.0000 | 4391.9902 | 2380.2697  |
| 426.4706 | 151.3690 | 241.6195 | 0.0000 | 4368.9193 | 2378.0131  |
| 418.5681 | 159.9922 | 231.0232 | 0.0000 | 4346.7034 | 2375.6397  |
| 410.9532 | 168.3016 | 220.8125 | 0.0000 | 4325.2959 | 2373.1402  |
| 403.6104 | 176.3140 | 210.9666 | 0.0000 | 4304.6534 | 2370.5043  |
| 396.5254 | 184.0452 | 201.4665 | 0.0000 | 4284.7356 | 2367.7204  |
| 389.6848 | 191.5096 | 192.2941 | 0.0000 | 4265.5050 | 2364.7758  |
| 383.0762 | 198.7208 | 183.4328 | 0.0000 | 4246.9267 | 2361.6562  |
| 376.6881 | 205.6915 | 174.8670 | 0.0000 | 4228.9680 | 2358.3454  |
| 370.5095 | 212.4336 | 166.5823 | 0.0000 | 4211.5984 | 2354.8254  |
| 364.5303 | 218.9580 | 158.5649 | 0.0000 | 4194.7895 | 2351.0755  |
| 358.7411 | 225.2752 | 150.8023 | 0.0000 | 4178.5144 | 2347.0727  |
| 353.1328 | 231.3949 | 143.2823 | 0.0000 | 4162.7482 | 2342.7904  |
| 347.6972 | 237.3262 | 135.9938 | 0.0000 | 4147.4674 | 2338.1982  |
| 342.4264 | 243.0777 | 128.9263 | 0.0000 | 4132.6498 | 2333.2613  |
| 337.3130 | 248.6574 | 122.0698 | 0.0000 | 4118.2748 | 2327.9393  |
| 332.3501 | 254.0729 | 115.4152 | 0.0000 | 4104.3228 | 2322.1854  |
| 327.5311 | 259.3314 | 108.9535 | 0.0000 | 4090.7754 | 2315.9447  |
| 322.8499 | 264.4395 | 102.6765 | 0.0000 | 4077.6152 | 2309.1527  |
| 318.3006 | 269.4037 | 96.5764  | 0.0000 | 4064.8259 | 2301.7330  |
| 313.8777 | 274.2300 | 90.6458  | 0.0000 | 4052.3921 | 2293.5945  |
| 309.5760 | 278.9239 | 84.8778  | 0.0000 | 4040.2990 | 2284.6272  |
| 305.3907 | 283.4909 | 79.2658  | 0.0000 | 4028.5330 | 2274.6978  |
| 301.3170 | 287.9361 | 73.8035  | 0.0000 | 4017.0808 | 2263.6428  |
| 297.3506 | 292.2643 | 68.4849  | 0.0000 | 4005.9302 | 2251.2591  |
| 293.4872 | 296.4800 | 63.3046  | 0.0000 | 3995.0693 | 2237.2921  |
| 289.7229 | 300.5875 | 58.2572  | 0.0000 | 3984.4870 | 2221.4171  |
| 286.0540 | 304.5911 | 53.3376  | 0.0000 | 3974.1727 | 2203.2147  |
| 282.4768 | 308.4944 | 48.5411  | 0.0000 | 3964.1164 | 2182.1325  |

OPTIMUM Coke= 428.8999 Kg

OPTIMUM injectant= 148.7182 Kg

OPTIMUM Blast Oxygen= 244.8768 Kg

OPTIMUM Injected Oxygen= 0.0000 Kg

OPTIMUM TEMP=2378.7020 oK

OPTIMALCOST= 4373.4635 Naira

OPTIMALCOST of coke= 3611.3370 Naira

OPTIMALCOST of injectant = 803.0783 Naira

OPTIMALCOST of oxygen = 0.0000 Naira

# APPENDIX III

## List of Symbols Appearing in Principal Equations

| SYMBOL       | MEANING                                                                                                                                                    | UNITS                                                                                  |
|--------------|------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------|
| $(C/Fe)^m$   | Molecular ratio: C/Fe in product metal                                                                                                                     | $\left\{ \frac{\text{Kg moles of dissolved C}}{\text{Kg mole of product Fe}} \right\}$ |
| $D^c$        | For heating and dissolving carbon in product                                                                                                               | KJ (kg mole of C in metal) <sup>-1</sup>                                               |
| $D^{CaCO_3}$ | For decomposing charged $CaCO_3$ to $CaO$ , C and $O_2$ at the thermal reserve temperature (extra heat demand due to charging $CaCO_3$ rather than $CaO$ ) | KJ (kg mole of $CaCO_3$ ) <sup>-1</sup>                                                |
| $D^{Fe}$     | For reducing $Fe_{0.947}O$ and for heating and melting Fe                                                                                                  | KJ (kg mole of product in Fe) <sup>-1</sup>                                            |
| $D^i$        | For decomposing 1 mole of tuyere injectant at its injection temperature to form its component elements at the thermal reserve temperature.                 | KJ (kg mole of injectant) <sup>-1</sup>                                                |
| $D^i_w$      | As above for 1 kg of injectant                                                                                                                             | KJ (kg mole of injectant) <sup>-1</sup>                                                |
| $D^{loss}$   | For convective and radiative heat loss per kg mole of product Fe                                                                                           | KJ (kg mole of product in Fe) <sup>-1</sup>                                            |
| $D^{Mn}$     | For reducing $MnO$ and for heating Mn and dissolving it in product metal                                                                                   | KJ (kg mole of Mn in metal) <sup>-1</sup>                                              |
| $D^{Si}$     | For reducing $SiO_2$ and for heating Si and dissolving it in product metal                                                                                 | KJ (kg mole of Si in metal) <sup>-1</sup>                                              |
| $D^{slag}$   | For heating slag oxides and forming 1 kg of liquid slag.                                                                                                   | KJ (kg of slag) <sup>-1</sup>                                                          |

| SYMBOL          | MEANING                                                                                                                     | UNITS                                                                                  |
|-----------------|-----------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------|
| $D^{wuz}$       | Sum of wustite reduction zone heat demands (excluding injectant demands), per kg mole of product Fe                         | KJ (kg mole of product Fe) <sup>-1</sup>                                               |
| $E^b$           | Enthalpy in blast air above that which it would have at the thermal reserve temperature.                                    | KJ (kg mole of O in dry blast air) <sup>-1</sup>                                       |
| $(Mn/Fe)^m$     | Molecular ratio: Mn/Fe in product metal                                                                                     | $\left\{ \frac{\text{Kg moles of dissolved C}}{\text{Kg mole of product Fe}} \right\}$ |
| $n_c^A$         | Carbon taking part in wustite reduction zone reduction reactions = carbon leaving wustite reduction zone in ascending gases | kg mole of C (kg mole of product in Fe) <sup>-1</sup>                                  |
| $n_c^{coke}$    | Carbon entering furnace in coke                                                                                             | kg mole of C (kg mole of product in Fe) <sup>-1</sup>                                  |
| $n_O^B$         | Oxygen entering furnace in dry blast air, i.e not including oxygen from humidity or tuyere injectants                       | kg mole of O (kg mole of product in Fe) <sup>-1</sup>                                  |
| $n_{CaCO_3}^A$  | Limestone charged to the furnace                                                                                            | kg mole of CaCO <sub>3</sub> (kg mole of product Fe) <sup>-1</sup>                     |
| $N^i$           | Quantity of tuyere injectant                                                                                                | kg mole of injectant (kg mole of product in Fe) <sup>-1</sup>                          |
| $(O/C)^g$       | Molecular ratio: O/C in carbonaceous portion of top gas                                                                     |                                                                                        |
| $(O/C)^{guz}$   | Molecular ratio: O/C in carbonaceous portion of the gas in chemical reserve                                                 |                                                                                        |
| $(O/H_2)^h$     | Molecular ratio: O/H <sub>2</sub> in hydrogenous portion of top gas                                                         |                                                                                        |
| $(O/H_2)^{guz}$ | Molecular ratio: O/H <sub>2</sub> in hydrogenous portion of the gas in the chemical reserve.                                |                                                                                        |

|                |                                                                                                       |                                                                                        |
|----------------|-------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------|
| $(O/Fe)^x$     | Molecular ratio: O/Fe in iron oxides charged to the furnace (=3/2 for $Fe_2O_3$ ; 4/3 for $Fe_3O_4$ ) | kg mole of O (kg mole of product in Fe)                                                |
| $(O/Fe)^{xyz}$ | Molecular ratio: O/Fe in iron oxide in the chemical reserve (=1.06 for $Fe_{0.947}O$ )                | kg mole of O (kg mole of product in Fe)                                                |
| $(Si/Fe)^m$    | Molecular ratio: Si/Fe in product metal                                                               | $\left\{ \frac{\text{Kg moles of dissolved C}}{\text{Kg mole of product Fe}} \right\}$ |
| $T_B T_g$      | Temperatures of blast and top gas                                                                     | K                                                                                      |
| $Wt_{slag}$    | Weight of product slag per mole of product Fe                                                         | kg mole of slag (kg mole of product Fe) <sup>-1</sup>                                  |
| $W^i$          | Weight of tuyere injectant per mole of product Fe                                                     | kg mole of injectant (kg mole of product in Fe) <sup>-1</sup>                          |
| $x,y,z$        | Moles of C, H <sub>2</sub> and O per mole of tuyere injectant                                         | kg moles (kg mole of injectant) <sup>-1</sup>                                          |

## APPENDIX IV

# Enthalpy Increment Equations for Elements and Compounds, $[H_T^\circ - H_{298}^\circ]$

Enthalpy values calculated with these equations are within  $\pm 500$  kJ of their published numerical equivalents. Sources are noted at the end of Appendix VII

| Substance                            | Units: kJ per kg mole of element or compound |              |                                |                            |                                |
|--------------------------------------|----------------------------------------------|--------------|--------------------------------|----------------------------|--------------------------------|
|                                      | Temperature range, K                         |              |                                |                            |                                |
|                                      | 298-800<br>Top gas                           | 800-1100     | 1100-1300<br>Wustite reduction | 1300-1900<br>Bosh & Hearth | 1800-2800<br>Flame temperature |
| $Al_2O_3$                            | 1077-32 000                                  | 1247-46 000  | 1287-50 000                    | 1327-55 000                | -                              |
| C                                    | 15.37- 4600                                  | 20.77- 8700  | 22.77-11 000                   | 23.57-11 800               | -                              |
| CO                                   | 30.27- 9100                                  | 32.57-10 800 | 34.27-12 600                   | 35.37-14 000               | 36.67-16 400                   |
| $CO_2$                               | 45.67-14 100                                 | 52.87-19 200 | 56.37-23 100                   | 58.67-26 000               | 61.07-30 500                   |
| CuO                                  | 48.57-14 500                                 | 51.67-17 000 | 54.27-19 800                   | 55.57-21 200               | -                              |
| $CaCO_3$                             | 1067-31 500                                  | 1237-45 100  | 1297-52 200                    | Decomposes above 1300 K    |                                |
| $CaO \cdot SiO_2$                    | 1087-32 300                                  | 1227-43 600  | 1287-49 500                    | 1287-50 000                | -                              |
| $(CaO)_2 \cdot SiO_2$                | 1587-47 000                                  | 1867-69 000  | 1897-73 000                    | 2187-105 000               | -                              |
| $(CaO)_3 \cdot P_2O_5$               | 2847-84 500                                  | 3567-142 000 | 4027-193 000                   | 4037-194 000               | -                              |
| $Fe_2$                               | 30.87- 9200                                  | 48.97-23 700 | -                              | 38.47-11 400               | -                              |
| $Fe_2^{(a)}$ (M.P. $\approx 1800$ K) | -                                            | -            | -                              | 44.07- 5800                | -                              |

|                              |              |              |                             |                             |              |
|------------------------------|--------------|--------------|-----------------------------|-----------------------------|--------------|
| $Fe_{0.94}O$                 | 52.27-15 600 | 56.47-18 900 | 58.67-21 400                | 61.17-24 100                | -            |
| $Fe_2O_3$                    | 1357-40 200  | 1587-58 800  | 1427-40 600                 | 1447-43 000                 | -            |
| $Fe_3O_4$                    | 2027-60 000  | 2277-82 000  | 2017-53 200                 | 2017-53 200                 | -            |
| $H_2$                        | 29.37- 8800  | 29.97- 9200  | 30.97-10 300                | 32.57-12 200                | 35.27-17 200 |
| $H_2O(g)$                    | 35.87-10 800 | 40.07-13 800 | 43.77-17 900                | 47.47-22 200                | -            |
| MgO                          | 45.67-13 600 | 50.97-17 800 | 52.27-19 300                | 55.07-22 300                | -            |
| $MgCO_3$                     | 1027-30 500  | 1267-49 500  | Decomposes below 1100 K     |                             |              |
| $Mn_2$                       | 31.07- 9200  | 44.37-19 900 | 38.27-13 200                | 48.67-24 600                | -            |
| $Mn_2^{(a)}$ (M.P. = 1517 K) | -            | -            | -                           | 48.67-10 000                | -            |
| MnO                          | 49.27-14 700 | 53.77-18 300 | 56.97-21 800                | 57.17-22 000                | -            |
| $MnO_2$                      | 68.27-20 300 | 77.37-27 600 | -                           | -                           | -            |
| $Mn_2O_3$                    | 1677-49 600  | 1827-61 900  | 1997-80 200                 | 2387-123 000                | -            |
| $N_2$                        | 30.07- 9000  | 32.17-10 500 | -                           | 34.47-13 000                | 36.47-16 500 |
| $O_2$                        | 31.67- 9600  | 34.37-11 500 | -                           | 36.27-13 500                | -            |
| $P_{2,8}$                    | 34.97-10 500 | 36.77-11 900 | 37.17-12 300                | 37.37-12 600                | -            |
| $S_{2,8}$                    | 35.27-10 600 | 36.97-11 900 | 37.27-12 300                | 37.47-12 500                | -            |
| $Si_2$                       | 23.67- 7000  | 26.47- 9300  | 27.27-10 200                | 27.17-10 100                | -            |
| $Si_2^{(a)}$ (M.P. = 1683 K) | -            | -            | -                           | 27.27+40 400                | -            |
| $SiO_2$                      | 61.17-18 200 | 71.07-25 900 | 71.47-24 300 <sup>(b)</sup> | 72.87-26 200 <sup>(b)</sup> | -            |

(a)  $[H_T^\circ - H_{298}^\circ]$   
 $M_1 \quad M_2$

(b)  $[H_T^\circ - H_{298}^\circ]$   
 cristobalite quartz

## APPENDIX V

# Enthalpies of Formation at Temperature T from Elements at Temperature T ( $H_T^f$ )

Values for compounds central to the analyses of this text (i.e.  $\text{CO}$ ,  $\text{CO}_2$ ,  $\text{H}_2\text{O}$ ,  $\text{Fe}_{0.94}\text{O}$ ) are accurate to within  $\pm 500$  kJ. Sources are noted at the end of the table.

| Compound                                                                                                   | Units: kJ per kg mole of compound |                         |                      |                                       |
|------------------------------------------------------------------------------------------------------------|-----------------------------------|-------------------------|----------------------|---------------------------------------|
|                                                                                                            | 298 K                             | 1100 K                  | 1200 K               | 1300 K                                |
| $\text{CH}_4$                                                                                              | -75 000                           | -91 000                 | -91 000              | -92 000                               |
| $\text{C}_2\text{H}_2$                                                                                     | -84 000                           | -102 000                | -101 000             | -100 000                              |
| $\text{C}_2\text{H}_4$                                                                                     | -105 000                          | -129 000                | -128 000             | -127 000                              |
| $\text{CO}$                                                                                                | -111 000                          | -113 000                | -113 000             | -114 000                              |
| $\text{CO}_2$                                                                                              | -394 000                          | -395 000                | -395 000             | -395 000                              |
| $\text{CaCO}_3$ (from $\text{CaO}$ , C and $\text{O}_2$ )                                                  | -572 000                          | -563 000                | -561 000             | -559 000                              |
| $\text{CaCO}_3 \cdot \text{MgCO}_3$ (from carbonates)                                                      | -12 000                           | decomposes below 1100 K |                      |                                       |
| $(\text{CaO})_2 \cdot \text{P}_2\text{O}_5$ (from $\text{CaO}$ , $\text{O}_2$ and $\text{P}_2\text{O}_5$ ) | -2 400 000                        | -2 364 000              | -2 353 000           | -2 341 000                            |
| $\text{CaO} \cdot \text{SiO}_2$ (from oxides)                                                              | -89 000                           | -91 000                 | -91 000              | -91 000                               |
| $(\text{CaO})_2 \cdot \text{SiO}_2$ (from oxides)                                                          | -126 000                          | -125 000                | -124 000             | -123 000                              |
|                                                                                                            |                                   |                         |                      |                                       |
| $\text{Fe}_{0.94}\text{O}$                                                                                 | -266 000                          | -265 000                | -265 000             | -265 000                              |
| $\text{Fe}_2\text{O}_3$                                                                                    | -1 121 000                        | -1 096 000              | -1 098 000           | -1 095 000                            |
| $\text{Fe}_3\text{O}_4$                                                                                    | -826 000                          | -810 000                | -811 000             | -809 000                              |
| $\text{H}_2\text{O}_l$ ( $\Delta H_{\text{vaporization}} = +44 000$ )                                      | -286 000                          |                         |                      |                                       |
| $\text{H}_2\text{O}_g$                                                                                     | -242 000                          | -248 000                | -249 000             | -250 000<br>(also -250 000 at 1500 K) |
| $\text{MgCO}_3$ (from $\text{MgO}$ , C and $\text{O}_2$ )                                                  | -511 000                          | decomposes below 1100 K |                      |                                       |
| $\text{MnO}$                                                                                               | -385 000                          | -386 000                | -386 000             | -386 000                              |
| $\text{Mn}_2\text{O}_3$                                                                                    | -1 387 000                        | -1 387 000              | -1 386 000           | -1 384 000                            |
| $\text{MnO}_2$                                                                                             | -521 000                          | -516 000                | decomposes at 1120 K |                                       |
| $\text{SO}_2$ (from gaseous $\text{S}_2$ )                                                                 | -362 000                          | -362 000                | -362 000             | -362 000                              |
| $\text{SiO}_2$                                                                                             | -911 000                          | -902 000                | -901 000             | -901 000                              |

The data are from:

Stull, D. R., Prophet, H. *et al.* (1970) *JANAF Thermochemical Tables*, 2nd edition, United States Department of Commerce, Document NSRDS-NBS 37, Washington, June 1971,

with the exception of:

(a)  $\text{CaO}$ ,  $\text{CaCO}_3$ ,  $\text{CaCO}_3 \cdot \text{MgCO}_3$ ,  $(\text{CaO})_2 \cdot \text{P}_2\text{O}_5$ ,  $\text{CaO} \cdot \text{SiO}_2$ ,  $(\text{CaO})_2 \cdot \text{SiO}_2$ ,  $\text{MgO}$ ,  $\text{MgCO}_3$ , which are from:

Robie, R. A. and Walther, D. R. (1968) *Thermodynamic Properties of Minerals*, United States Geological Survey Bulletin 1259, Washington.

(b)  $\text{C}_2\text{H}_2$ ,  $\text{C}_2\text{H}_4$ , which are from:

Scott, D. W. (1974) *Chemical Thermodynamic Properties of Hydrocarbons*, United States Bureau of Mines Bulletin 666, Washington.